Vector Mechanics for Engineers Statics and Dynamics 11th edition Beer Solutions Manual

SKU: 9780073398242-SOLUTIONS

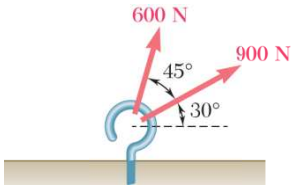
CHAPTER 2

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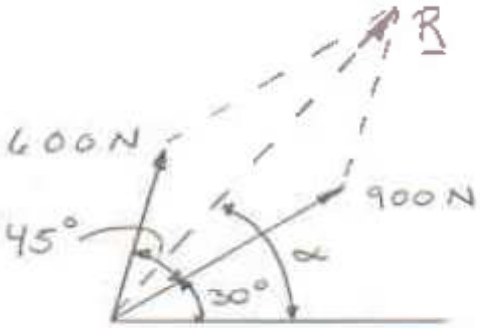


PROBLEM 2.1

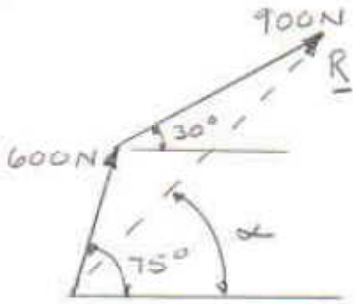
Two forces are applied as shown to a hook. Determine graphically the magnitude and direction of their resultant using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION

(*a*) Parallelogram law:

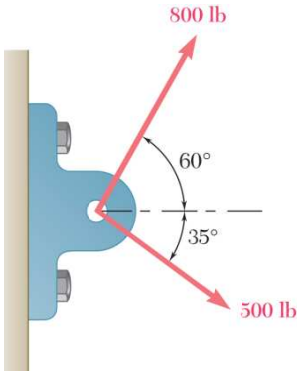


(*b*) Triangle rule:



We measure: $R = 1391$ kN, $\alpha = 47.8°$ $\mathbf{R} = 1391$ N ∠ $47.8°$ ◀

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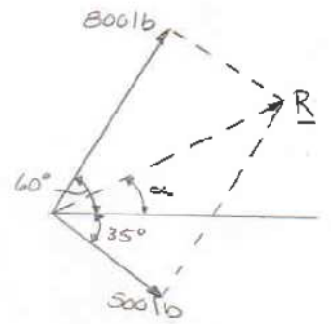


PROBLEM 2.2

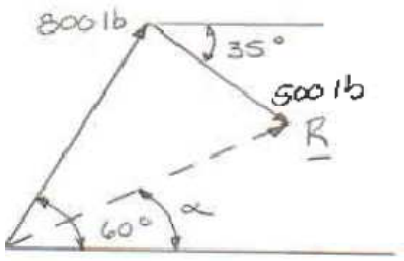
Two forces are applied as shown to a bracket support. Determine graphically the magnitude and direction of their resultant using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION

(*a*) Parallelogram law:

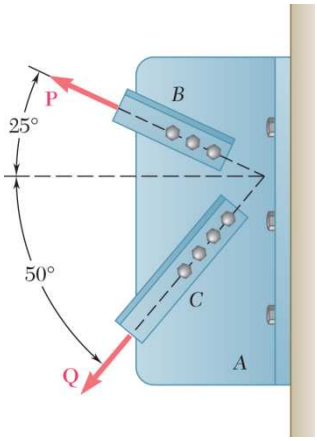


(*b*) Triangle rule:



We measure: $R = 906$ lb, $\alpha = 26.6°$ $R = 906$ lb ∠ $26.6°$ ◀

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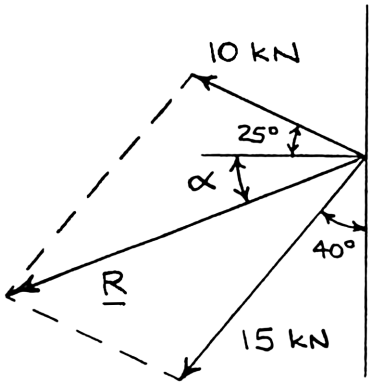


PROBLEM 2.3

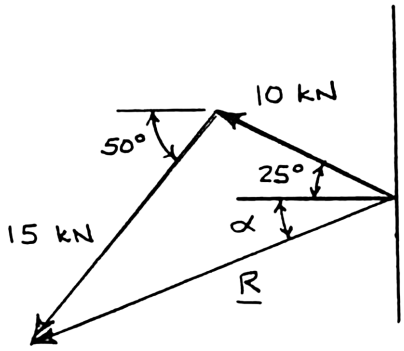
Two structural members B and C are bolted to bracket A. Knowing that both members are in tension and that $P = 10$ kN and $Q = 15$ kN, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (a) the parallelogram law, (b) the triangle rule.

SOLUTION

(a) Parallelogram law:

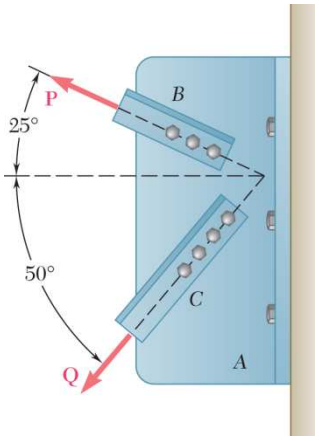


(b) Triangle rule:



We measure: $R = 20.1$ kN, $\alpha = 21.2°$ **R** = 20.1 kN ∠ 21.2° ◀

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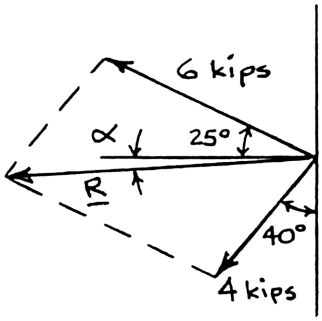


PROBLEM 2.4

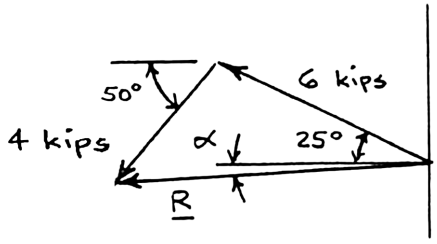
Two structural members B and C are bolted to bracket A. Knowing that both members are in tension and that $P = 6$ kips and $Q = 4$ kips, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (a) the parallelogram law, (b) the triangle rule.

SOLUTION

(a) Parallelogram law:

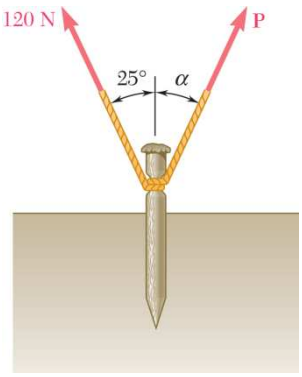


(b) Triangle rule:



We measure: $R = 8.03$ kips, $\alpha = 3.8°$ **R** = 8.03 kips ∠ 3.8° ◀

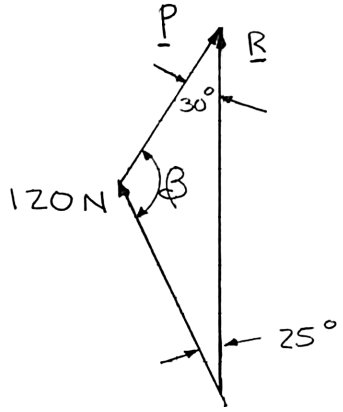
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PROBLEM 2.5

A stake is being pulled out of the ground by means of two ropes as shown. Knowing that $\alpha = 30°$, determine by trigonometry (*a*) the magnitude of the force **P** so that the resultant force exerted on the stake is vertical, (*b*) the corresponding magnitude of the resultant.

SOLUTION

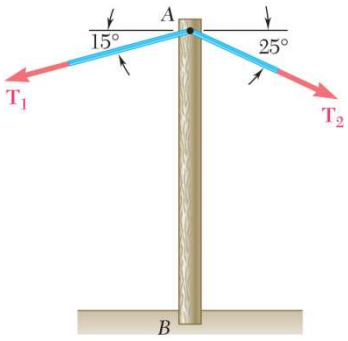


Using the triangle rule and the law of sines:

(*a*)
$$\frac{120\text{ N}}{\sin 30°} = \frac{P}{\sin 25°}$$
$$P = 101.4\text{ N} \blacktriangleleft$$

(*b*)
$$30° + \beta + 25° = 180°$$
$$\beta = 180° - 25° - 30°$$
$$= 125°$$
$$\frac{120\text{ N}}{\sin 30°} = \frac{R}{\sin 125°}$$
$$R = 196.6\text{ N} \blacktriangleleft$$

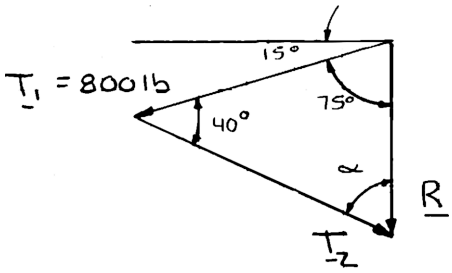
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PROBLEM 2.6

A telephone cable is clamped at A to the pole AB. Knowing that the tension in the left-hand portion of the cable is T_1 = 800 lb, determine by trigonometry (*a*) the required tension T_2 in the right-hand portion if the resultant **R** of the forces exerted by the cable at A is to be vertical, (*b*) the corresponding magnitude of **R**.

SOLUTION

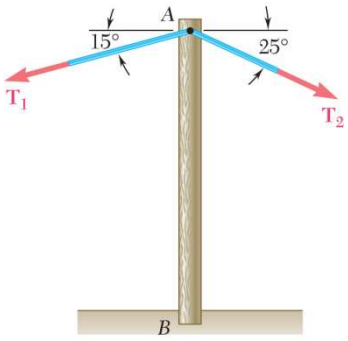


Using the triangle rule and the law of sines:

(*a*)
$$75° + 40° + \alpha = 180°$$
$$\alpha = 180° - 75° - 40°$$
$$= 65°$$
$$\frac{800 \text{ lb}}{\sin 65°} = \frac{T_2}{\sin 75°}$$
$$T_2 = 853 \text{ lb} \blacktriangleleft$$

(*b*)
$$\frac{800 \text{ lb}}{\sin 65°} = \frac{R}{\sin 40°}$$
$$R = 567 \text{ lb} \blacktriangleleft$$

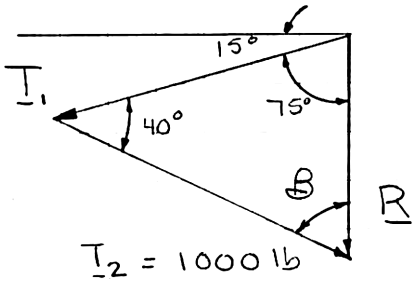
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PROBLEM 2.7

A telephone cable is clamped at A to the pole AB. Knowing that the tension in the right-hand portion of the cable is $T_2 = 1000$ lb, determine by trigonometry (*a*) the required tension T_1 in the left-hand portion if the resultant **R** of the forces exerted by the cable at A is to be vertical, (*b*) the corresponding magnitude of **R**.

SOLUTION



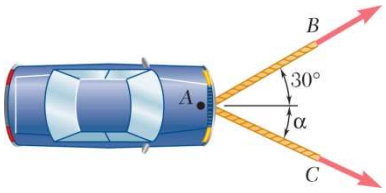
Using the triangle rule and the law of sines:

(*a*)
$$75° + 40° + \beta = 180°$$
$$\beta = 180° - 75° - 40°$$
$$= 65°$$
$$\frac{1000 \text{ lb}}{\sin 75°} = \frac{T_1}{\sin 65°}$$
$$T_1 = 938 \text{ lb} \blacktriangleleft$$

(*b*)
$$\frac{1000 \text{ lb}}{\sin 75°} = \frac{R}{\sin 40°}$$
$$R = 665 \text{ lb} \blacktriangleleft$$

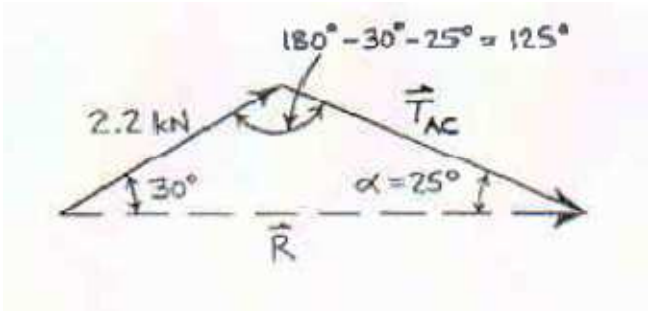
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PROBLEM 2.8



A disabled automobile is pulled by means of two ropes as shown. The tension in rope AB is 2.2 kN, and the angle α is 25°. Knowing that the resultant of the two forces applied at A is directed along the axis of the automobile, determine by trigonometry (*a*) the tension in rope AC, (*b*) the magnitude of the resultant of the two forces applied at A.

SOLUTION



Using the law of sines:

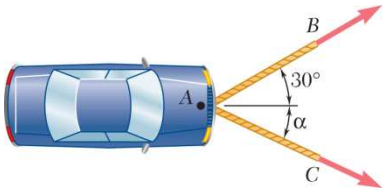
$$\frac{T_{AC}}{\sin 30^\circ} = \frac{R}{\sin 125^\circ} = \frac{2.2 \text{ kN}}{\sin 25^\circ}$$

$$T_{AC} = 2.603 \text{ kN}$$
$$R = 4.264 \text{ kN}$$

(*a*) $T_{AC} = 2.60$ kN ◀

(*b*) $R = 4.26$ kN ◀

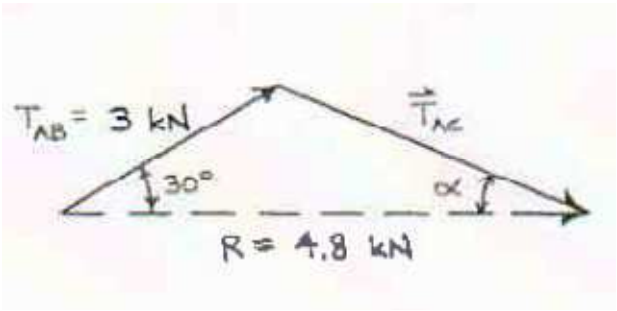
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PROBLEM 2.9

A disabled automobile is pulled by means of two ropes as shown. Knowing that the tension in rope *AB* is 3 kN, determine by trigonometry the tension in rope *AC* and the value of α so that the resultant force exerted at *A* is a 4.8-kN force directed along the axis of the automobile.

SOLUTION



Using the law of cosines:

$$T_{AC}^2 = (3\text{ kN})^2 + (4.8\text{ kN})^2 - 2(3\text{ kN})(4.8\text{ kN})\cos 30°$$

$$T_{AC} = 2.6643\text{ kN}$$

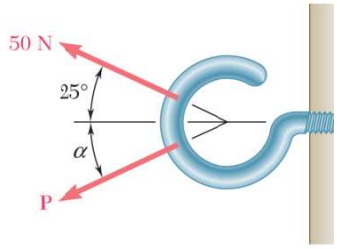
Using the law of sines:

$$\frac{\sin\alpha}{3\text{ kN}} = \frac{\sin 30°}{2.6643\text{ kN}}$$

$$\alpha = 34.3°$$

$$\mathbf{T}_{AC} = 2.66\text{ kN} \measuredangle 34.3° \blacktriangleleft$$

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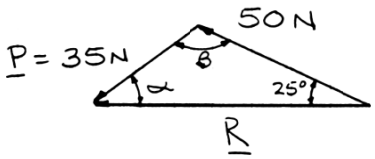


PROBLEM 2.10

Two forces are applied as shown to a hook support. Knowing that the magnitude of **P** is 35 N, determine by trigonometry (*a*) the required angle α if the resultant **R** of the two forces applied to the support is to be horizontal, (*b*) the corresponding magnitude of **R**.

SOLUTION

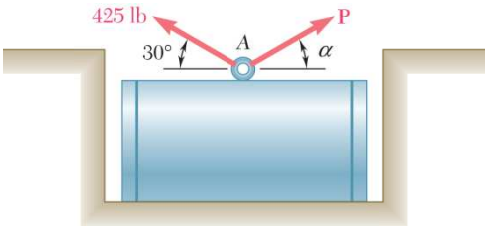
Using the triangle rule and law of sines:



(*a*)
$$\frac{\sin\alpha}{50\text{ N}} = \frac{\sin 25°}{35\text{ N}}$$
$$\sin\alpha = 0.60374$$
$$\alpha = 37.138°$$
$$\alpha = 37.1° \blacktriangleleft$$

(*b*)
$$\alpha + \beta + 25° = 180°$$
$$\beta = 180° - 25° - 37.138°$$
$$= 117.862°$$
$$\frac{R}{\sin 117.862°} = \frac{35\text{ N}}{\sin 25°}$$
$$R = 73.2\text{ N} \blacktriangleleft$$

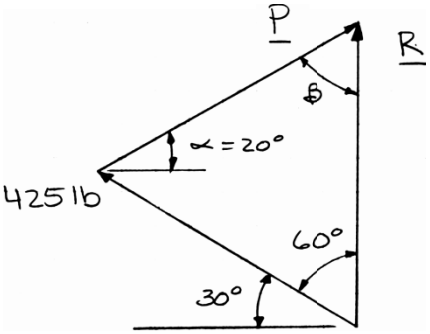
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PROBLEM 2.11

A steel tank is to be positioned in an excavation. Knowing that $\alpha = 20°$, determine by trigonometry (*a*) the required magnitude of the force **P** if the resultant **R** of the two forces applied at *A* is to be vertical, (*b*) the corresponding magnitude of **R**.

SOLUTION

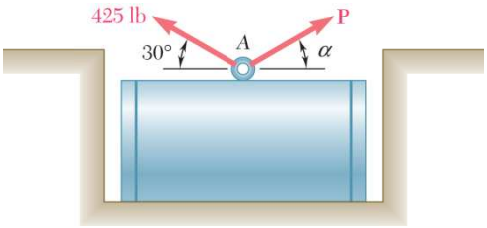


Using the triangle rule and the law of sines:

(*a*)
$$\beta + 50° + 60° = 180°$$
$$\beta = 180° - 50° - 60°$$
$$= 70°$$
$$\frac{425 \text{ lb}}{\sin 70°} = \frac{P}{\sin 60°}$$
$$P = 392 \text{ lb} \blacktriangleleft$$

(*b*)
$$\frac{425 \text{ lb}}{\sin 70°} = \frac{R}{\sin 50°}$$
$$R = 346 \text{ lb} \blacktriangleleft$$

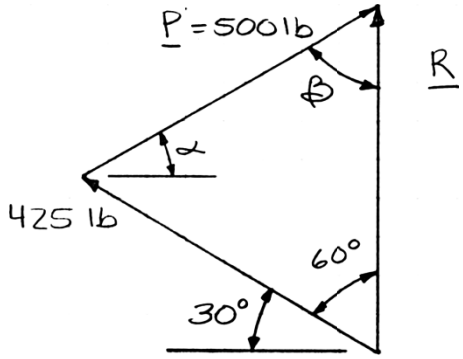
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PROBLEM 2.12

A steel tank is to be positioned in an excavation. Knowing that the magnitude of **P** is 500 lb, determine by trigonometry (*a*) the required angle α if the resultant **R** of the two forces applied at *A* is to be vertical, (*b*) the corresponding magnitude of **R**.

SOLUTION

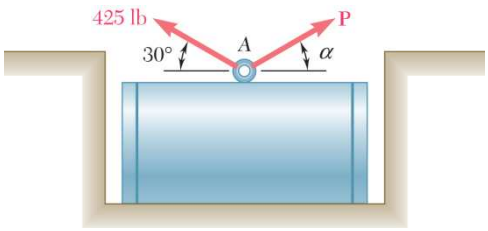


Using the triangle rule and the law of sines:

(*a*)
$$(\alpha + 30°) + 60° + \beta = 180°$$
$$\beta = 180° - (\alpha + 30°) - 60°$$
$$\beta = 90° - \alpha$$
$$\frac{\sin(90° - \alpha)}{425 \text{ lb}} = \frac{\sin 60°}{500 \text{ lb}}$$
$$90° - \alpha = 47.402° \qquad \alpha = 42.6° \blacktriangleleft$$

(*b*)
$$\frac{R}{\sin(42.598° + 30°)} = \frac{500 \text{ lb}}{\sin 60°} \qquad R = 551 \text{ lb} \blacktriangleleft$$

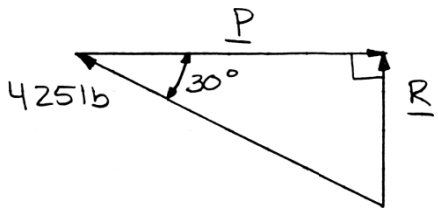
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PROBLEM 2.13

A steel tank is to be positioned in an excavation. Determine by trigonometry (*a*) the magnitude and direction of the smallest force **P** for which the resultant **R** of the two forces applied at *A* is vertical, (*b*) the corresponding magnitude of **R**.

SOLUTION

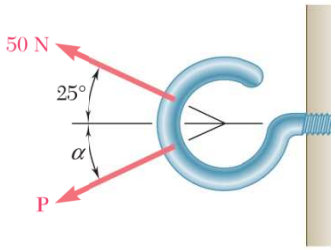


The smallest force *P* will be perpendicular to *R*.

(*a*) $P = (425\text{ lb})\cos 30°$ $\quad \mathbf{P} = 368\text{ lb} \rightarrow$

(*b*) $R = (425\text{ lb})\sin 30°$ $\quad R = 213\text{ lb}$

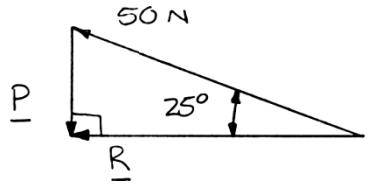
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PROBLEM 2.14

For the hook support of Prob. 2.10, determine by trigonometry (*a*) the magnitude and direction of the smallest force **P** for which the resultant **R** of the two forces applied to the support is horizontal, (*b*) the corresponding magnitude of **R**.

SOLUTION

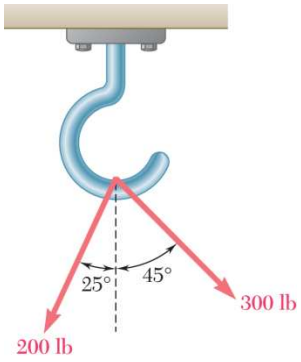


The smallest force P will be perpendicular to R.

(*a*) $P = (50\text{ N})\sin 25°$ $\quad \mathbf{P} = 21.1\text{ N}\downarrow$ ◀

(*b*) $R = (50\text{ N})\cos 25°$ $\quad R = 45.3\text{ N}$ ◀

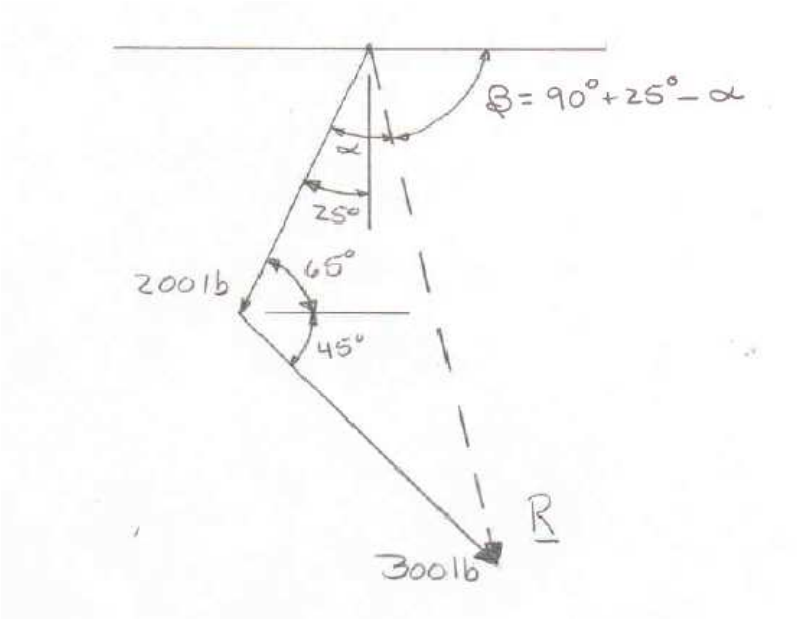
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PROBLEM 2.15

For the hook support shown, determine by trigonometry the magnitude and direction of the resultant of the two forces applied to the support.

SOLUTION



Using the law of cosines:

$$R^2 = (200\text{ lb})^2 + (300\text{ lb})^2 - 2(200\text{ lb})(300\text{ lb})\cos(45^\circ + 65^\circ)$$

$$R = 413.57\text{ lb}$$

Using the law of sines:

$$\frac{\sin\alpha}{300\text{ lb}} = \frac{\sin(45^\circ + 65^\circ)}{413.57\text{ lb}}$$

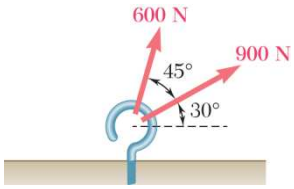
$$\alpha = 42.972^\circ$$

$$\beta = 90^\circ + 25^\circ - 42.972^\circ$$

$$\mathbf{R} = 414\text{ lb} \measuredangle 72.0^\circ \blacktriangleleft$$

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PROBLEM 2.16

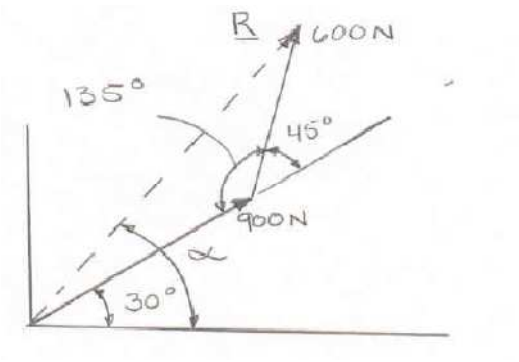


Solve Prob. 2.1 by trigonometry.

PROBLEM 2.1

Two forces are applied as shown to a hook. Determine graphically the magnitude and direction of their resultant using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION



Using the law of cosines:

$$R^2 = (900\,\text{N})^2 + (600\,\text{N})^2 - 2(900\,\text{N})(600\,\text{N})\cos(135°)$$

$$R = 1390.57\,\text{N}$$

Using the law of sines:

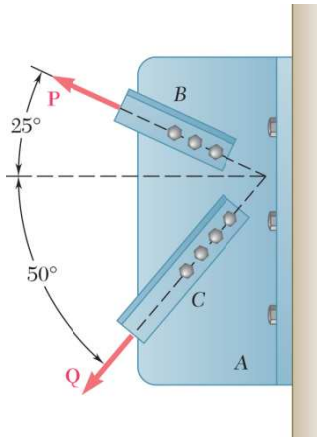
$$\frac{\sin(\alpha - 30^\circ)}{600\,\text{N}} = \frac{\sin(135°)}{1390.57\,\text{N}}$$

$$\alpha - 30^\circ = 17.7642°$$

$$\alpha = 47.764^\circ$$

$$\mathbf{R} = 1391\,\text{N} \nearrow 47.8° \blacktriangleleft$$

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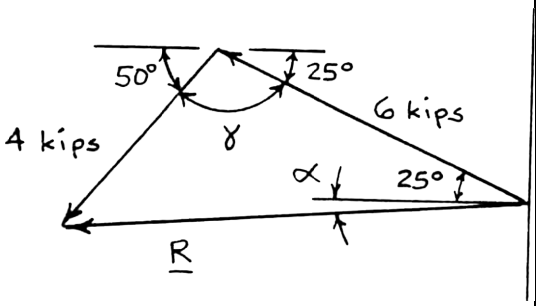
PROBLEM 2.17

Solve Problem 2.4 by trigonometry.

PROBLEM 2.4 Two structural members B and C are bolted to bracket A. Knowing that both members are in tension and that $P = 6$ kips and $Q = 4$ kips, determine graphically the magnitude and direction of the resultant force exerted on the bracket using (*a*) the parallelogram law, (*b*) the triangle rule.

SOLUTION

Using the force triangle and the laws of cosines and sines:



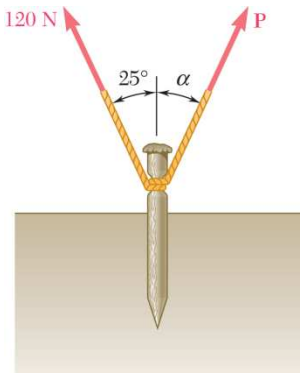
We have:
$$\gamma = 180° - (50° + 25°)$$
$$= 105°$$

Then
$$R^2 = (4 \text{ kips})^2 + (6 \text{ kips})^2 - 2(4 \text{ kips})(6 \text{ kips})\cos 105°$$
$$= 64.423 \text{ kips}^2$$
$$R = 8.0264 \text{ kips}$$

And
$$\frac{4 \text{ kips}}{\sin(25° + \alpha)} = \frac{8.0264 \text{ kips}}{\sin 105°}$$
$$\sin(25° + \alpha) = 0.48137$$
$$25° + \alpha = 28.775°$$
$$\alpha = 3.775°$$

$$\mathbf{R} = 8.03 \text{ kips} \measuredangle 3.8° \blacktriangleleft$$

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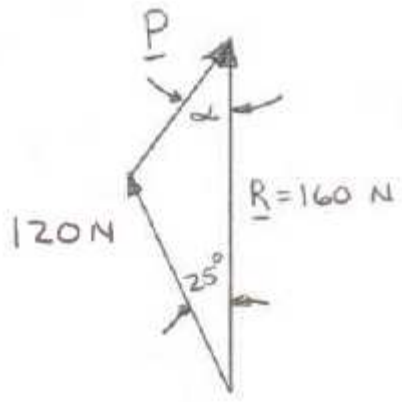


PROBLEM 2.18

For the stake of Prob. 2.5, knowing that the tension in one rope is 120 N, determine by trigonometry the magnitude and direction of the force **P** so that the resultant is a vertical force of 160 N.

PROBLEM 2.5 A stake is being pulled out of the ground by means of two ropes as shown. Knowing that $\alpha = 30°$, determine by trigonometry (*a*) the magnitude of the force **P** so that the resultant force exerted on the stake is vertical, (*b*) the corresponding magnitude of the resultant.

SOLUTION



Using the laws of cosines and sines:

$$P^2 = (120\text{ N})^2 + (160\text{ N})^2 - 2(120\text{ N})(160\text{ N})\cos 25°$$

$$P = 72.096\text{ N}$$

And

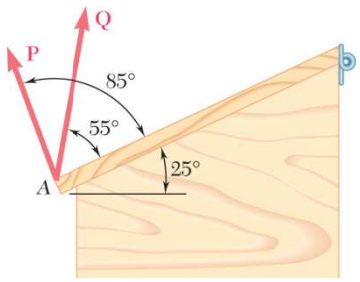
$$\frac{\sin\alpha}{120\text{ N}} = \frac{\sin 25°}{72.096\text{ N}}$$

$$\sin\alpha = 0.70343$$

$$\alpha = 44.703°$$

$$\mathbf{P} = 72.1\text{ N} \measuredangle 44.7° \blacktriangleleft$$

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PROBLEM 2.19

Two forces **P** and **Q** are applied to the lid of a storage bin as shown. Knowing that $P = 48$ N and $Q = 60$ N, determine by trigonometry the magnitude and direction of the resultant of the two forces.

SOLUTION

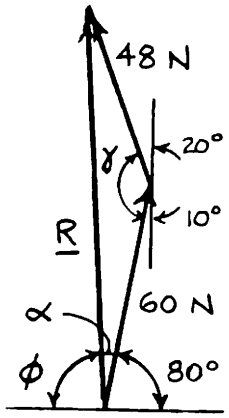
Using the force triangle and the laws of cosines and sines:

We have
$$\gamma = 180° - (20° + 10°)$$
$$= 150°$$

Then
$$R^2 = (48\text{ N})^2 + (60\text{ N})^2 - 2(48\text{ N})(60\text{ N})\cos 150°$$
$$R = 104.366\text{ N}$$

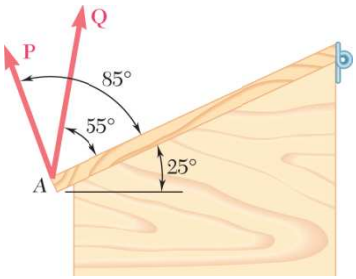
and
$$\frac{48\text{ N}}{\sin\alpha} = \frac{104.366\text{ N}}{\sin 150°}$$
$$\sin\alpha = 0.22996$$
$$\alpha = 13.2947°$$

Hence:
$$\phi = 180° - \alpha - 80°$$
$$= 180° - 13.2947° - 80°$$
$$= 86.705°$$



$\mathbf{R} = 104.4\text{ N} \measuredangle 86.7°$ ◀

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PROBLEM 2.20

Two forces **P** and **Q** are applied to the lid of a storage bin as shown. Knowing that $P = 60$ N and $Q = 48$ N, determine by trigonometry the magnitude and direction of the resultant of the two forces.

SOLUTION

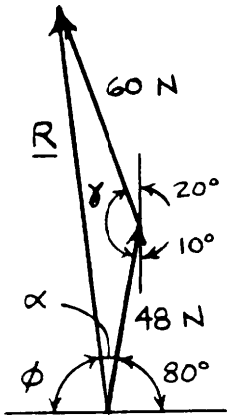
Using the force triangle and the laws of cosines and sines:

We have
$$\gamma = 180° - (20° + 10°)$$
$$= 150°$$

Then
$$R^2 = (60\text{ N})^2 + (48\text{ N})^2 - 2(60\text{ N})(48\text{ N})\cos 150°$$
$$R = 104.366\text{ N}$$

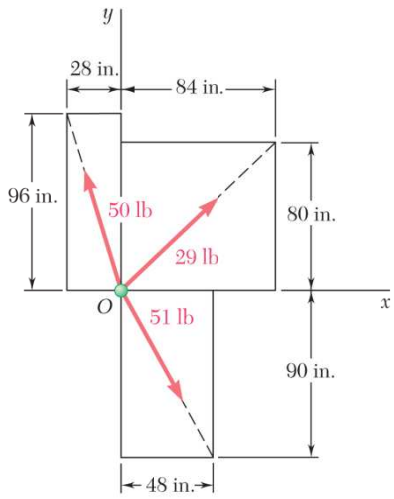
and
$$\frac{60\text{ N}}{\sin\alpha} = \frac{104.366\text{ N}}{\sin 150°}$$
$$\sin\alpha = 0.28745$$
$$\alpha = 16.7054°$$

Hence:
$$\phi = 180° - \alpha - 180°$$
$$= 180° - 16.7054° - 80°$$
$$= 83.295°$$



$\mathbf{R} = 104.4\text{ N} \measuredangle 83.3°$ ◀

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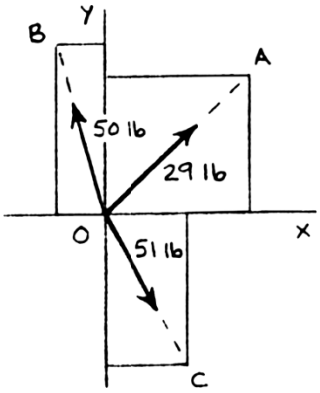


PROBLEM 2.21

Determine the x and y components of each of the forces shown.

SOLUTION

Compute the following distances:



$$OA = \sqrt{(84)^2 + (80)^2}$$
$$= 116 \text{ in.}$$
$$OB = \sqrt{(28)^2 + (96)^2}$$
$$= 100 \text{ in.}$$
$$OC = \sqrt{(48)^2 + (90)^2}$$
$$= 102 \text{ in.}$$

29-lb Force:

$$F_x = +(29 \text{ lb})\frac{84}{116} \qquad F_x = +21.0 \text{ lb} \blacktriangleleft$$

$$F_y = +(29 \text{ lb})\frac{80}{116} \qquad F_y = +20.0 \text{ lb} \blacktriangleleft$$

50-lb Force:

$$F_x = -(50 \text{ lb})\frac{28}{100} \qquad F_x = -14.00 \text{ lb} \blacktriangleleft$$

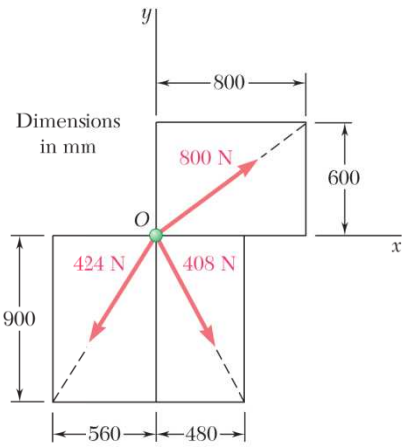
$$F_y = +(50 \text{ lb})\frac{96}{100} \qquad F_y = +48.0 \text{ lb} \blacktriangleleft$$

51-lb Force:

$$F_x = +(51 \text{ lb})\frac{48}{102} \qquad F_x = +24.0 \text{ lb} \blacktriangleleft$$

$$F_y = -(51 \text{ lb})\frac{90}{102} \qquad F_y = -45.0 \text{ lb} \blacktriangleleft$$

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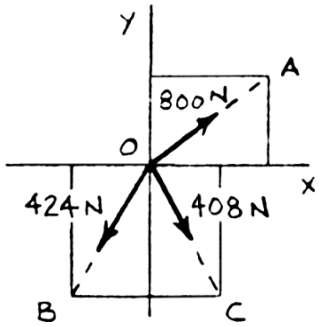


PROBLEM 2.22

Determine the x and y components of each of the forces shown.

SOLUTION

Compute the following distances:



$$OA = \sqrt{(600)^2 + (800)^2} = 1000 \text{ mm}$$

$$OB = \sqrt{(560)^2 + (900)^2} = 1060 \text{ mm}$$

$$OC = \sqrt{(480)^2 + (900)^2} = 1020 \text{ mm}$$

800-N Force:

$$F_x = +(800 \text{ N})\frac{800}{1000} \qquad F_x = +640 \text{ N} \blacktriangleleft$$

$$F_y = +(800 \text{ N})\frac{600}{1000} \qquad F_y = +480 \text{ N} \blacktriangleleft$$

424-N Force:

$$F_x = -(424 \text{ N})\frac{560}{1060} \qquad F_x = -224 \text{ N} \blacktriangleleft$$

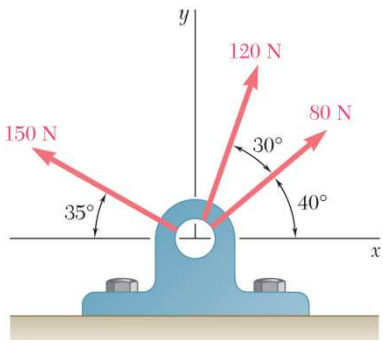
$$F_y = -(424 \text{ N})\frac{900}{1060} \qquad F_y = -360 \text{ N} \blacktriangleleft$$

408-N Force:

$$F_x = +(408 \text{ N})\frac{480}{1020} \qquad F_x = +192.0 \text{ N} \blacktriangleleft$$

$$F_y = -(408 \text{ N})\frac{900}{1020} \qquad F_y = -360 \text{ N} \blacktriangleleft$$

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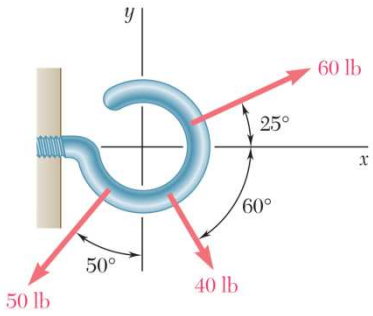
PROBLEM 2.23

Determine the x and y components of each of the forces shown.

SOLUTION

80-N Force:	$F_x = +(80\text{ N})\cos 40°$	$F_x = 61.3\text{ N}$ ◀
	$F_y = +(80\text{ N})\sin 40°$	$F_y = 51.4\text{ N}$ ◀
120-N Force:	$F_x = +(120\text{ N})\cos 70°$	$F_x = 41.0\text{ N}$ ◀
	$F_y = +(120\text{ N})\sin 70°$	$F_y = 112.8\text{ N}$ ◀
150-N Force:	$F_x = -(150\text{ N})\cos 35°$	$F_x = -122.9\text{ N}$ ◀
	$F_y = +(150\text{ N})\sin 35°$	$F_y = 86.0\text{ N}$ ◀

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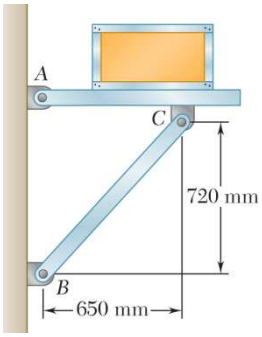
PROBLEM 2.24

Determine the x and y components of each of the forces shown.

SOLUTION

40-lb Force:	$F_x = +(40\text{ lb})\cos 60°$	$F_x = 20.0\text{ lb}$ ◀
	$F_y = -(40\text{ lb})\sin 60°$	$F_y = -34.6\text{ lb}$ ◀
50-lb Force:	$F_x = -(50\text{ lb})\sin 50°$	$F_x = -38.3\text{ lb}$ ◀
	$F_y = -(50\text{ lb})\cos 50°$	$F_y = -32.1\text{ lb}$ ◀
60-lb Force:	$F_x = +(60\text{ lb})\cos 25°$	$F_x = 54.4\text{ lb}$ ◀
	$F_y = +(60\text{ lb})\sin 25°$	$F_y = 25.4\text{ lb}$ ◀

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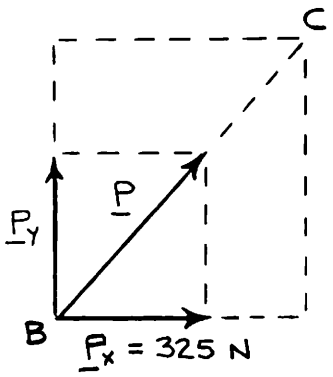


PROBLEM 2.25

Member BC exerts on member AC a force **P** directed along line BC. Knowing that **P** must have a 325-N horizontal component, determine (a) the magnitude of the force **P**, (b) its vertical component.

SOLUTION

$$BC = \sqrt{(650\text{ mm})^2 + (720\text{ mm})^2}$$
$$= 970\text{ mm}$$



(a)
$$P_x = P\left(\frac{650}{970}\right)$$

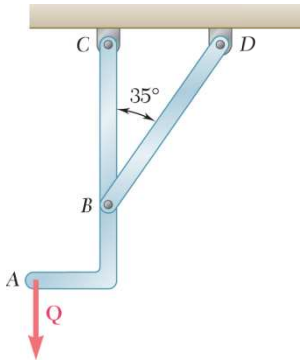
or
$$P = P_x\left(\frac{970}{650}\right)$$
$$= 325\text{ N}\left(\frac{970}{650}\right)$$
$$= 485\text{ N}$$

$P = 485\text{ N}$ ◀

(b)
$$P_y = P\left(\frac{720}{970}\right)$$
$$= 485\text{ N}\left(\frac{720}{970}\right)$$
$$= 360\text{ N}$$

$P_y = 970\text{ N}$ ◀

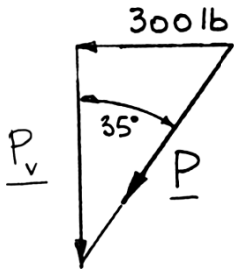
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PROBLEM 2.26

Member *BD* exerts on member *ABC* a force **P** directed along line *BD*. Knowing that **P** must have a 300-lb horizontal component, determine (*a*) the magnitude of the force **P**, (*b*) its vertical component.

SOLUTION



(*a*) $P\sin 35° = 300 \text{ lb}$

$$P = \frac{300 \text{ lb}}{\sin 35°}$$

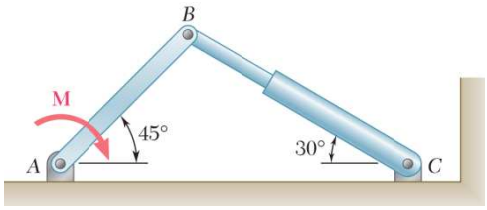
$$P = 523 \text{ lb} \blacktriangleleft$$

(*b*) Vertical component $P_v = P\cos 35°$

$$= (523 \text{ lb})\cos 35°$$

$$P_v = 428 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.27

The hydraulic cylinder *BC* exerts on member *AB* a force **P** directed along line *BC*. Knowing that **P** must have a 600-N component perpendicular to member *AB*, determine (*a*) the magnitude of the force **P**, (*b*) its component along line *AB*.

SOLUTION

$$180° = 45° + \alpha + 90° + 30°$$

$$\alpha = 180° - 45° - 90° - 30°$$

$$= 15°$$

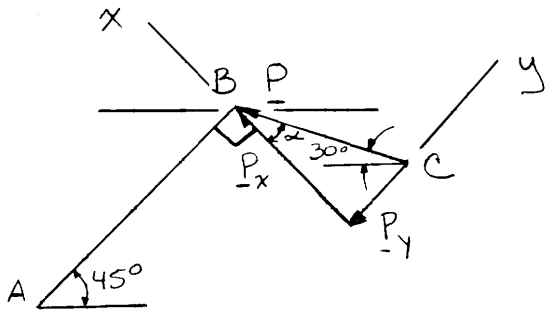
(*a*)

$$\cos\alpha = \frac{P_x}{P}$$

$$P = \frac{P_x}{\cos\alpha}$$

$$= \frac{600\text{ N}}{\cos 15°}$$

$$= 621.17\text{ N}$$



$$P = 621\text{ N} \blacktriangleleft$$

(*b*)

$$\tan\alpha = \frac{P_y}{P_x}$$

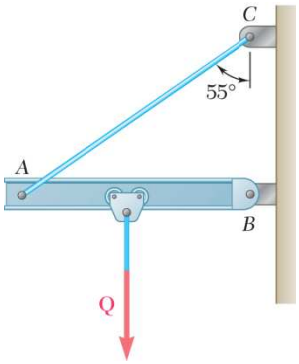
$$P_y = P_x \tan\alpha$$

$$= (600\text{ N})\tan 15°$$

$$= 160.770\text{ N}$$

$$P_y = 160.8\text{ N} \blacktriangleleft$$

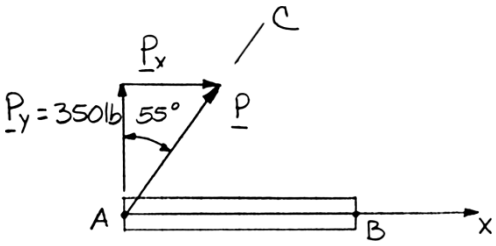
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PROBLEM 2.28

Cable AC exerts on beam AB a force **P** directed along line AC. Knowing that **P** must have a 350-lb vertical component, determine (a) the magnitude of the force **P**, (b) its horizontal component.

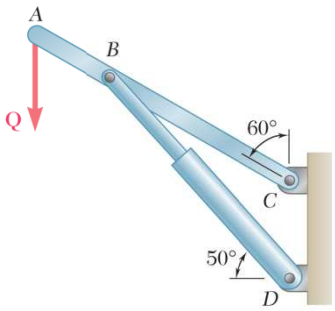
SOLUTION



(a)
$$P = \frac{P_y}{\cos 55°}$$
$$= \frac{350 \text{ lb}}{\cos 55°}$$
$$= 610.21 \text{ lb}$$
$$P = 610 \text{ lb} \blacktriangleleft$$

(b)
$$P_x = P \sin 55°$$
$$= (610.21 \text{ lb}) \sin 55°$$
$$= 499.85 \text{ lb}$$
$$P_x = 500 \text{ lb} \blacktriangleleft$$

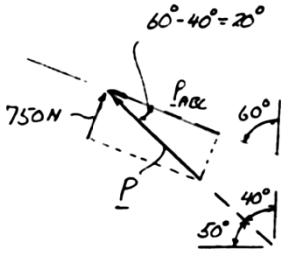
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PROBLEM 2.29

The hydraulic cylinder *BD* exerts on member *ABC* a force **P** directed along line *BD*. Knowing that **P** must have a 750-N component perpendicular to member *ABC*, determine (*a*) the magnitude of the force **P**, (*b*) its component parallel to *ABC*.

SOLUTION



(*a*) $750\text{ N} = P\sin 20°$

$$P = 2192.9\text{ N}$$

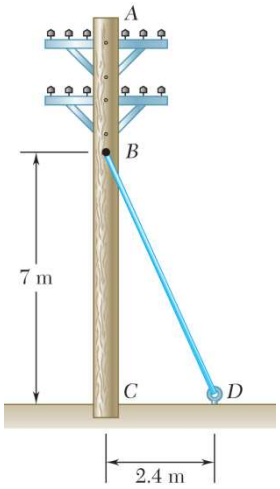
$$P = 2190\text{ N} \blacktriangleleft$$

(*b*) $P_{ABC} = P\cos 20°$

$$= (2192.9\text{ N})\cos 20°$$

$$P_{ABC} = 2060\text{ N} \blacktriangleleft$$

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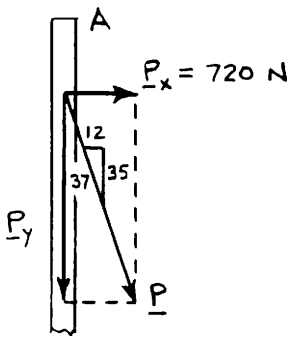
PROBLEM 2.30

The guy wire *BD* exerts on the telephone pole *AC* a force **P** directed along *BD*. Knowing that **P** must have a 720-N component perpendicular to the pole *AC*, determine (*a*) the magnitude of the force **P**, (*b*) its component along line *AC*.

SOLUTION

(*a*)

$$P = \frac{37}{12} P_x$$
$$= \frac{37}{12}(720 \text{ N})$$
$$= 2220 \text{ N}$$



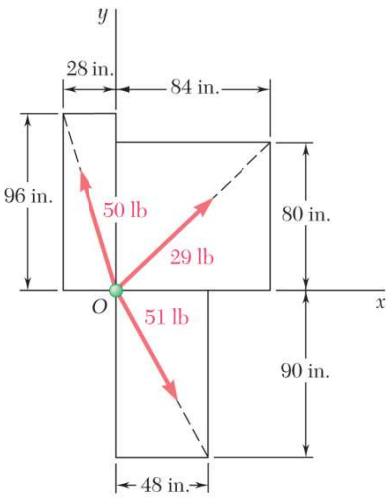
$P = 2.22$ kN ◀

(*b*)

$$P_y = \frac{35}{12} P_x$$
$$= \frac{35}{12}(720 \text{ N})$$
$$= 2100 \text{ N}$$

$P_y = 2.10$ kN ◀

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PROBLEM 2.31

Determine the resultant of the three forces of Problem 2.21.

PROBLEM 2.21 Determine the x and y components of each of the forces shown.

SOLUTION

Components of the forces were determined in Problem 2.21:

Force	x Comp. (lb)	y Comp. (lb)
29 lb	+21.0	+20.0
50 lb	–14.00	+48.0
51 lb	+24.0	–45.0
	$R_x = +31.0$	$R_y = +23.0$

$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$

$$= (31.0 \text{ lb})\mathbf{i} + (23.0 \text{ lb})\mathbf{j}$$

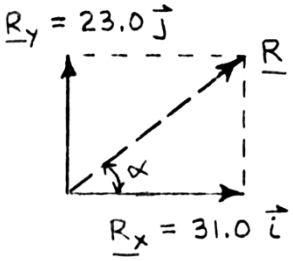
$$\tan\alpha = \frac{R_y}{R_x}$$

$$= \frac{23.0}{31.0}$$

$$\alpha = 36.573°$$

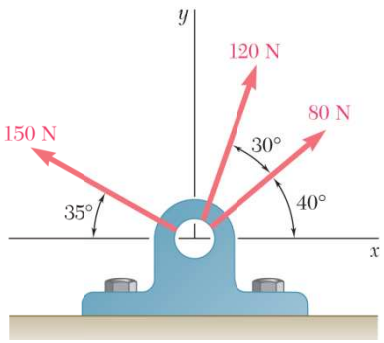
$$R = \frac{23.0 \text{ lb}}{\sin(36.573°)}$$

$$= 38.601 \text{ lb}$$



$\mathbf{R} = 38.6 \text{ lb} \angle 36.6°$ ◀

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PROBLEM 2.32

Determine the resultant of the three forces of Problem 2.23.

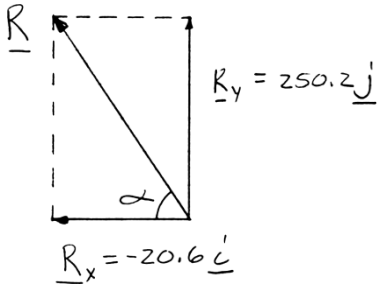
PROBLEM 2.23 Determine the x and y components of each of the forces shown.

SOLUTION

Components of the forces were determined in Problem 2.23:

Force	x Comp. (N)	y Comp. (N)
80 N	+61.3	+51.4
120 N	+41.0	+112.8
150 N	−122.9	+86.0
	$R_x = -20.6$	$R_y = +250.2$

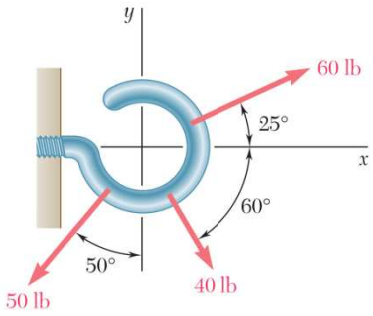
$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$
$$= (-20.6\text{ N})\mathbf{i} + (250.2\text{ N})\mathbf{j}$$



$$\tan\alpha = \frac{R_y}{R_x}$$
$$\tan\alpha = \frac{250.2\text{ N}}{20.6\text{ N}}$$
$$\tan\alpha = 12.1456$$
$$\alpha = 85.293°$$
$$R = \frac{250.2\text{ N}}{\sin 85.293°}$$

$$\mathbf{R} = 251\text{ N} \measuredangle 85.3° \blacktriangleleft$$

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PROBLEM 2.33

Determine the resultant of the three forces of Problem 2.24.

PROBLEM 2.24 Determine the x and y components of each of the forces shown.

SOLUTION

Force	x Comp. (lb)	y Comp. (lb)
40 lb	+20.00	–34.64
50 lb	–38.30	–32.14
60 lb	+54.38	+25.36
	$R_x = +36.08$	$R_y = -41.42$

$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$

$$= (+36.08 \text{ lb})\mathbf{i} + (-41.42 \text{ lb})\mathbf{j}$$

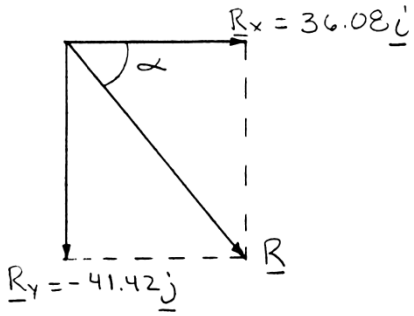
$$\tan\alpha = \frac{R_y}{R_x}$$

$$\tan\alpha = \frac{41.42 \text{ lb}}{36.08 \text{ lb}}$$

$$\tan\alpha = 1.14800$$

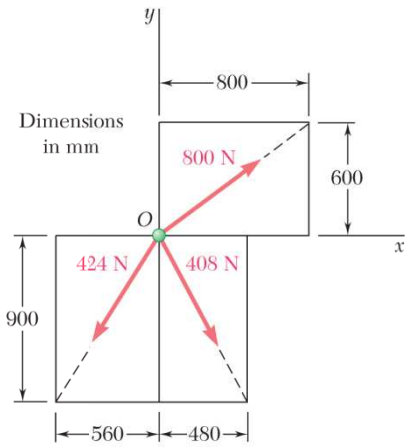
$$\alpha = 48.942°$$

$$R = \frac{41.42 \text{ lb}}{\sin 48.942°}$$



$\mathbf{R} = 54.9$ lb $\measuredangle$ 48.9° ◀

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PROBLEM 2.34

Determine the resultant of the three forces of Problem 2.22.

PROBLEM 2.22 Determine the x and y components of each of the forces shown.

SOLUTION

Components of the forces were determined in Problem 2.22:

Force	x Comp. (N)	y Comp. (N)
800 lb	+640	+480
424 lb	–224	–360
408 lb	+192	–360
	$R_x = +608$	$R_y = -240$

$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$

$$= (608 \text{ lb})\mathbf{i} + (-240 \text{ lb})\mathbf{j}$$

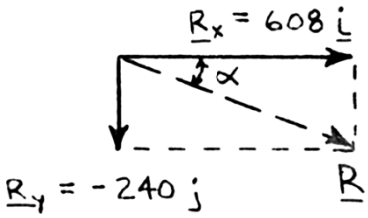
$$\tan\alpha = \frac{R_y}{R_x}$$

$$= \frac{240}{608}$$

$$\alpha = 21.541°$$

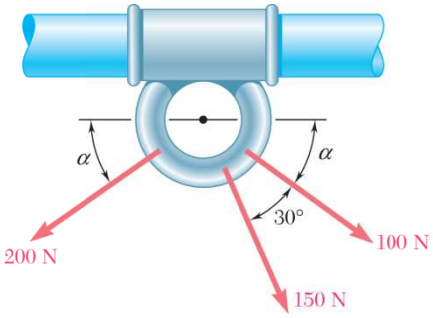
$$R = \frac{240 \text{ N}}{\sin(21.541°)}$$

$$= 653.65 \text{ N}$$



$\mathbf{R} = 654 \text{ N} \searrow 21.5°$ ◀

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PROBLEM 2.35

Knowing that $\alpha = 35°$, determine the resultant of the three forces shown.

SOLUTION

100-N Force:

$$F_x = +(100\text{ N})\cos 35° = +81.915\text{ N}$$
$$F_y = -(100\text{ N})\sin 35° = -57.358\text{ N}$$

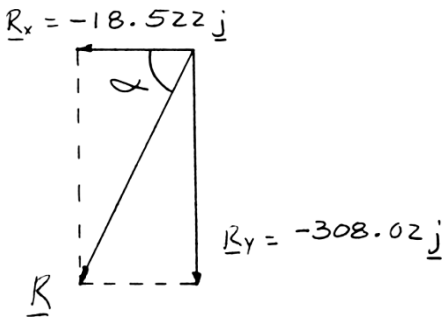
150-N Force:

$$F_x = +(150\text{ N})\cos 65° = +63.393\text{ N}$$
$$F_y = -(150\text{ N})\sin 65° = -135.946\text{ N}$$

200-N Force:

$$F_x = -(200\text{ N})\cos 35° = -163.830\text{ N}$$
$$F_y = -(200\text{ N})\sin 35° = -114.715\text{ N}$$

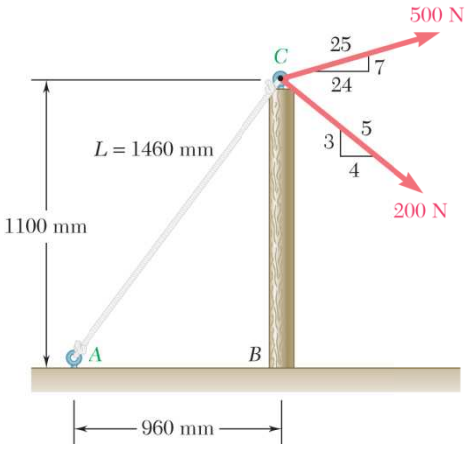
Force	x Comp. (N)	y Comp. (N)
100 N	+81.915	−57.358
150 N	+63.393	−135.946
200 N	−163.830	−114.715
	$R_x = -18.522$	$R_y = -308.02$



$$\mathbf{R} = R_x\mathbf{i} + R_y\mathbf{j}$$
$$= (-18.522\text{ N})\mathbf{i} + (-308.02\text{ N})\mathbf{j}$$
$$\tan\alpha = \frac{R_y}{R_x}$$
$$= \frac{308.02}{18.522}$$
$$\alpha = 86.559°$$
$$R = \frac{308.02\text{ N}}{\sin 86.559}$$

$$\mathbf{R} = 309\text{ N} \measuredangle 86.6° \blacktriangleleft$$

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PROBLEM 2.36

Knowing that the tension in rope AC is 365 N, determine the resultant of the three forces exerted at point C of post BC.

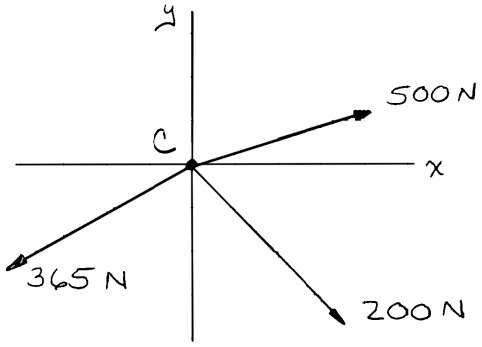
SOLUTION

Determine force components:

Cable force AC:

$$F_x = -(365\text{ N})\frac{960}{1460} = -240\text{ N}$$

$$F_y = -(365\text{ N})\frac{1100}{1460} = -275\text{ N}$$



500-N Force:

$$F_x = (500\text{ N})\frac{24}{25} = 480\text{ N}$$

$$F_y = (500\text{ N})\frac{7}{25} = 140\text{ N}$$

200-N Force:

$$F_x = (200\text{ N})\frac{4}{5} = 160\text{ N}$$

$$F_y = -(200\text{ N})\frac{3}{5} = -120\text{ N}$$

and

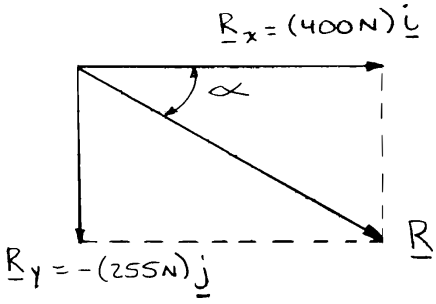
$$R_x = \Sigma F_x = -240\text{ N} + 480\text{ N} + 160\text{ N} = 400\text{ N}$$

$$R_y = \Sigma F_y = -275\text{ N} + 140\text{ N} - 120\text{ N} = -255\text{ N}$$

$$R = \sqrt{R_x^2 + R_y^2}$$

$$= \sqrt{(400\text{ N})^2 + (-255\text{ N})^2}$$

$$= 474.37\text{ N}$$



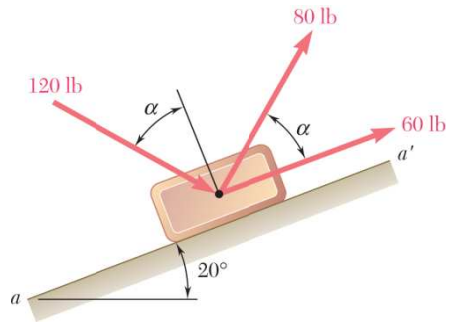
Further:

$$\tan\alpha = \frac{255}{400}$$

$$\alpha = 32.5°$$

R = 474 N ∠ 32.5° ◀

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PROBLEM 2.37

Knowing that $\alpha = 40°$, determine the resultant of the three forces shown.

SOLUTION

60-lb Force:

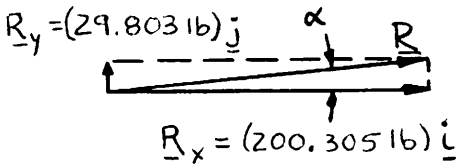
$$F_x = (60 \text{ lb})\cos 20° = 56.382 \text{ lb}$$
$$F_y = (60 \text{ lb})\sin 20° = 20.521 \text{ lb}$$

80-lb Force:

$$F_x = (80 \text{ lb})\cos 60° = 40.000 \text{ lb}$$
$$F_y = (80 \text{ lb})\sin 60° = 69.282 \text{ lb}$$

120-lb Force:

$$F_x = (120 \text{ lb})\cos 30° = 103.923 \text{ lb}$$
$$F_y = -(120 \text{ lb})\sin 30° = -60.000 \text{ lb}$$



and

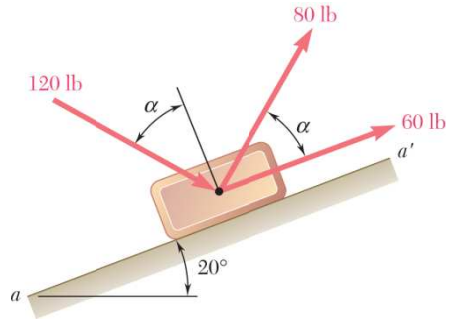
$$R_x = \Sigma F_x = 200.305 \text{ lb}$$
$$R_y = \Sigma F_y = 29.803 \text{ lb}$$
$$R = \sqrt{(200.305 \text{ lb})^2 + (29.803 \text{ lb})^2}$$
$$= 202.510 \text{ lb}$$

Further:

$$\tan\alpha = \frac{29.803}{200.305}$$
$$\alpha = \tan^{-1}\frac{29.803}{200.305}$$
$$= 8.46°$$

R = 203 lb ∠ 8.46° ◀

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PROBLEM 2.38

Knowing that $\alpha = 75°$, determine the resultant of the three forces shown.

SOLUTION

60-lb Force:

$$F_x = (60 \text{ lb}) \cos 20° = 56.382 \text{ lb}$$
$$F_y = (60 \text{ lb}) \sin 20° = 20.521 \text{ lb}$$

80-lb Force:

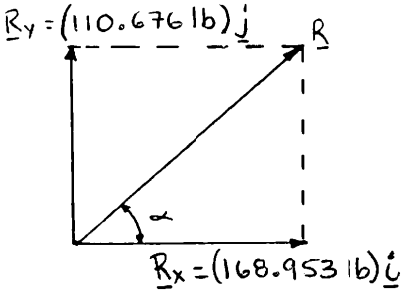
$$F_x = (80 \text{ lb}) \cos 95° = -6.9725 \text{ lb}$$
$$F_y = (80 \text{ lb}) \sin 95° = 79.696 \text{ lb}$$

120-lb Force:

$$F_x = (120 \text{ lb}) \cos 5° = 119.543 \text{ lb}$$
$$F_y = (120 \text{ lb}) \sin 5° = 10.459 \text{ lb}$$

Then

$$R_x = \Sigma F_x = 168.953 \text{ lb}$$
$$R_y = \Sigma F_y = 110.676 \text{ lb}$$



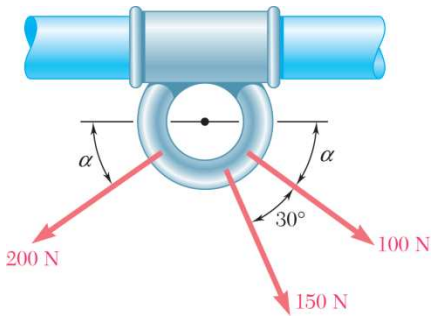
and

$$R = \sqrt{(168.953 \text{ lb})^2 + (110.676 \text{ lb})^2}$$
$$= 201.976 \text{ lb}$$

$$\tan \alpha = \frac{110.676}{168.953}$$
$$\tan \alpha = 0.65507$$
$$\alpha = 33.228°$$

R = 202 lb ∠ 33.2° ◀

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PROBLEM 2.39

For the collar of Problem 2.35, determine (*a*) the required value of α if the resultant of the three forces shown is to be vertical, (*b*) the corresponding magnitude of the resultant.

SOLUTION

$$R_x = \Sigma F_x$$
$$= (100\text{ N})\cos\alpha + (150\text{ N})\cos(\alpha + 30°) - (200\text{ N})\cos\alpha$$
$$R_x = -(100\text{ N})\cos\alpha + (150\text{ N})\cos(\alpha + 30°) \qquad (1)$$

$$R_y = \Sigma F_y$$
$$= -(100\text{ N})\sin\alpha - (150\text{ N})\sin(\alpha + 30°) - (200\text{ N})\sin\alpha$$
$$R_y = -(300\text{ N})\sin\alpha - (150\text{ N})\sin(\alpha + 30°) \qquad (2)$$

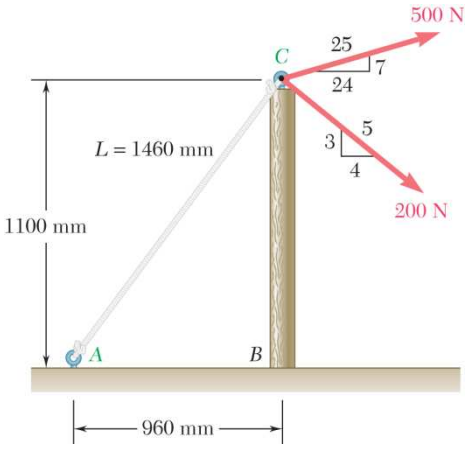
(*a*) For **R** to be vertical, we must have $R_x = 0$. We make $R_x = 0$ in Eq. (1):

$$-100\cos\alpha + 150\cos(\alpha + 30°) = 0$$
$$-100\cos\alpha + 150(\cos\alpha\cos 30° - \sin\alpha\sin 30°) = 0$$
$$29.904\cos\alpha = 75\sin\alpha$$
$$\tan\alpha = \frac{29.904}{75}$$
$$= 0.39872$$
$$\alpha = 21.738° \qquad \alpha = 21.7° \blacktriangleleft$$

(*b*) Substituting for α in Eq. (2):

$$R_y = -300\sin 21.738° - 150\sin 51.738°$$
$$= -228.89\text{ N}$$
$$R = |R_y| = 228.89\text{ N} \qquad R = 229\text{ N} \blacktriangleleft$$

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PROBLEM 2.40

For the post of Prob. 2.36, determine (*a*) the required tension in rope *AC* if the resultant of the three forces exerted at point *C* is to be horizontal, (*b*) the corresponding magnitude of the resultant.

SOLUTION

$$R_x = \Sigma F_x = -\frac{960}{1460}T_{AC} + \frac{24}{25}(500\text{ N}) + \frac{4}{5}(200\text{ N})$$

$$R_x = -\frac{48}{73}T_{AC} + 640\text{ N} \qquad (1)$$

$$R_y = \Sigma F_y = -\frac{1100}{1460}T_{AC} + \frac{7}{25}(500\text{ N}) - \frac{3}{5}(200\text{ N})$$

$$R_y = -\frac{55}{73}T_{AC} + 20\text{ N} \qquad (2)$$

(*a*) For **R** to be horizontal, we must have $R_y = 0$.

Set $R_y = 0$ in Eq. (2): $-\frac{55}{73}T_{AC} + 20\text{ N} = 0$

$$T_{AC} = 26.545\text{ N} \qquad T_{AC} = 26.5\text{ N} \blacktriangleleft$$

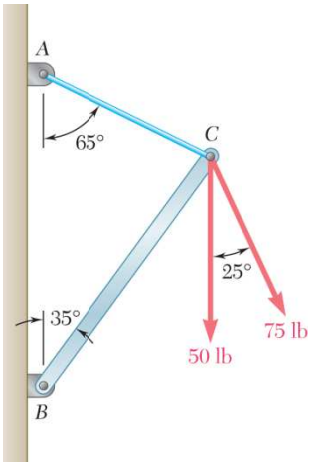
(*b*) Substituting for T_{AC} into Eq. (1) gives

$$R_x = -\frac{48}{73}(26.545\text{ N}) + 640\text{ N}$$

$$R_x = 622.55\text{ N}$$

$$R = R_x = 623\text{ N} \qquad R = 623\text{ N} \blacktriangleleft$$

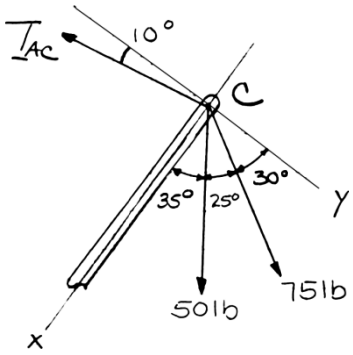
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PROBLEM 2.41

Determine (*a*) the required tension in cable *AC*, knowing that the resultant of the three forces exerted at Point *C* of boom *BC* must be directed along *BC*, (*b*) the corresponding magnitude of the resultant.

SOLUTION



Using the *x* and *y* axes shown:

$$R_x = \Sigma F_x = T_{AC}\sin 10° + (50\text{ lb})\cos 35° + (75\text{ lb})\cos 60°$$
$$= T_{AC}\sin 10° + 78.458\text{ lb} \qquad (1)$$

$$R_y = \Sigma F_y = (50\text{ lb})\sin 35° + (75\text{ lb})\sin 60° - T_{AC}\cos 10°$$
$$R_y = 93.631\text{ lb} - T_{AC}\cos 10° \qquad (2)$$

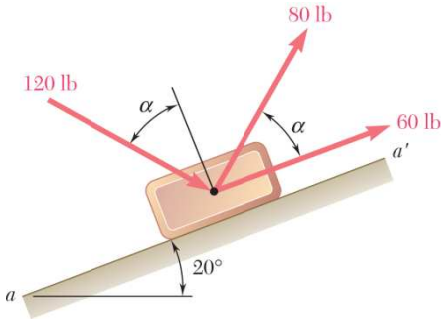
(*a*) Set $R_y = 0$ in Eq. (2):

$$93.631\text{ lb} - T_{AC}\cos 10° = 0$$
$$T_{AC} = 95.075\text{ lb} \qquad T_{AC} = 95.1\text{ lb} \blacktriangleleft$$

(*b*) Substituting for T_{AC} in Eq. (1):

$$R_x = (95.075\text{ lb})\sin 10° + 78.458\text{ lb}$$
$$= 94.968\text{ lb}$$
$$R = R_x \qquad R = 95.0\text{ lb} \blacktriangleleft$$

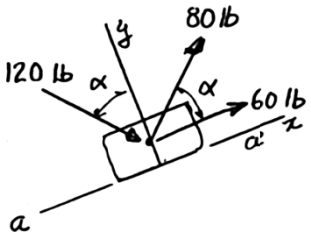
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PROBLEM 2.42

For the block of Problems 2.37 and 2.38, determine (*a*) the required value of α if the resultant of the three forces shown is to be parallel to the incline, (*b*) the corresponding magnitude of the resultant.

SOLUTION



Select the x axis to be along $a\,a'$.

Then

$$R_x = \Sigma F_x = (60\text{ lb}) + (80\text{ lb})\cos\alpha + (120\text{ lb})\sin\alpha \tag{1}$$

and

$$R_y = \Sigma F_y = (80\text{ lb})\sin\alpha - (120\text{ lb})\cos\alpha \tag{2}$$

(*a*) Set $R_y = 0$ in Eq. (2).

$$(80\text{ lb})\sin\alpha - (120\text{ lb})\cos\alpha = 0$$

Dividing each term by $\cos\alpha$ gives:

$$(80\text{ lb})\tan\alpha = 120\text{ lb}$$

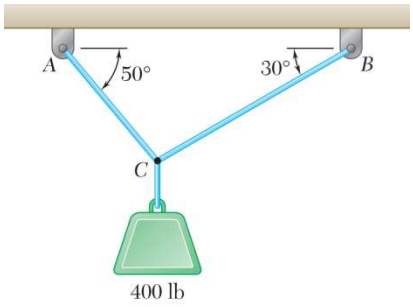
$$\tan\alpha = \frac{120\text{ lb}}{80\text{ lb}}$$

$$\alpha = 56.310° \qquad \alpha = 56.3° \blacktriangleleft$$

(*b*) Substituting for α in Eq. (1) gives:

$$R_x = 60\text{ lb} + (80\text{ lb})\cos 56.31° + (120\text{ lb})\sin 56.31° = 204.22\text{ lb} \qquad R_x = 204\text{ lb} \blacktriangleleft$$

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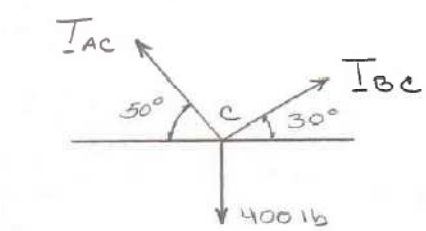


PROBLEM 2.43

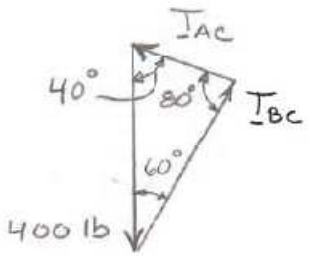
Two cables are tied together at C and are loaded as shown. Determine the tension (*a*) in cable AC, (*b*) in cable BC.

SOLUTION

Free-Body Diagram



Force Triangle



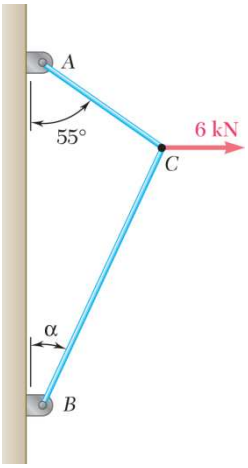
Law of sines:

$$\frac{T_{AC}}{\sin 60^\circ} = \frac{T_{BC}}{\sin 40^\circ} = \frac{400 \text{ lb}}{\sin 80^\circ}$$

(*a*) $$T_{AC} = \frac{400 \text{ lb}}{\sin 80^\circ}(\sin 60^\circ)$$ $$T_{AC} = 352 \text{ lb} \blacktriangleleft$$

(*b*) $$T_{BC} = \frac{400 \text{ lb}}{\sin 80^\circ}(\sin 40^\circ)$$ $$T_{BC} = 261 \text{ lb} \blacktriangleleft$$

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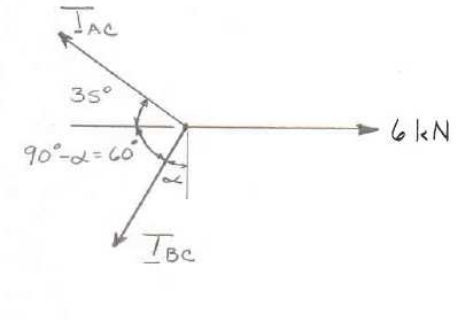


PROBLEM 2.44

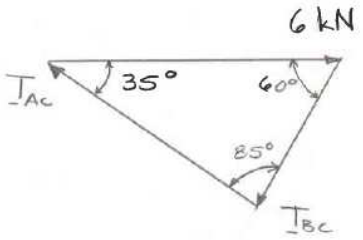
Two cables are tied together at C and are loaded as shown. Knowing that $\alpha = 30°$, determine the tension (*a*) in cable AC, (*b*) in cable BC.

SOLUTION

Free-Body Diagram



Force Triangle



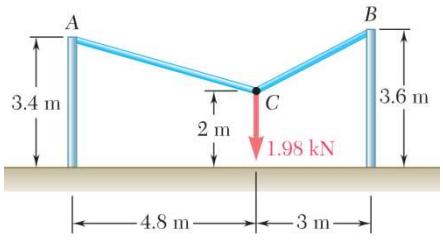
Law of sines:

$$\frac{T_{AC}}{\sin 60°} = \frac{T_{BC}}{\sin 35°} = \frac{6\text{ kN}}{\sin 85°}$$

(*a*) $$T_{AC} = \frac{6\text{ kN}}{\sin 85°}(\sin 60°) \qquad T_{AC} = 5.22\text{ kN} \blacktriangleleft$$

(*b*) $$T_{BC} = \frac{6\text{ kN}}{\sin 85°}(\sin 35°) \qquad T_{BC} = 3.45\text{ kN} \blacktriangleleft$$

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PROBLEM 2.45

Two cables are tied together at C and loaded as shown. Determine the tension (*a*) in cable AC, (*b*) in cable BC.

SOLUTION

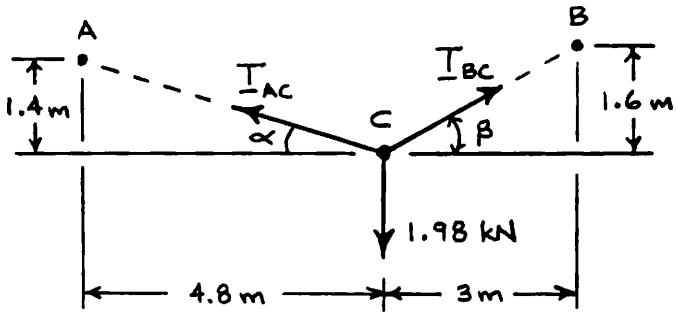
Free-Body Diagram

$$\tan\alpha = \frac{1.4}{4.8}$$

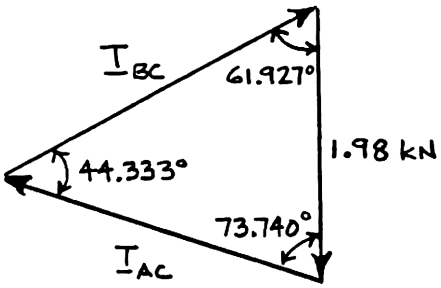
$$\alpha = 16.2602°$$

$$\tan\beta = \frac{1.6}{3}$$

$$\beta = 28.073°$$



Force Triangle



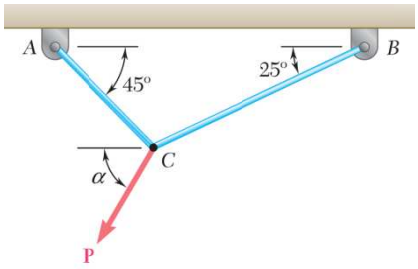
Law of sines:

$$\frac{T_{AC}}{\sin 61.927°} = \frac{T_{BC}}{\sin 73.740°} = \frac{1.98\text{ kN}}{\sin 44.333°}$$

(*a*) $$T_{AC} = \frac{1.98\text{ kN}}{\sin 44.333°}\sin 61.927°$$ $$T_{AC} = 2.50\text{ kN}$$ ◀

(*b*) $$T_{BC} = \frac{1.98\text{ kN}}{\sin 44.333°}\sin 73.740°$$ $$T_{BC} = 2.72\text{ kN}$$ ◀

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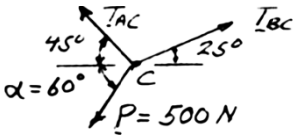


PROBLEM 2.46

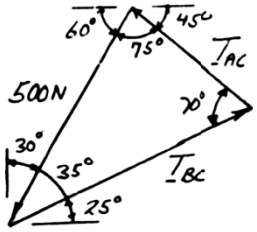
Two cables are tied together at C and are loaded as shown. Knowing that **P** = 500 N and $\alpha = 60°$, determine the tension in (*a*) in cable *AC*, (*b*) in cable *BC*.

SOLUTION

Free-Body Diagram



Force Triangle

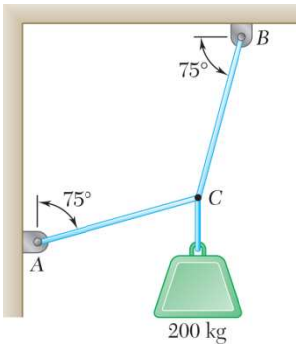


Law of sines:
$$\frac{T_{AC}}{\sin 35°} = \frac{T_{BC}}{\sin 75°} = \frac{500\text{ N}}{\sin 70°}$$

(*a*)
$$T_{AC} = \frac{500\text{ N}}{\sin 70°}\sin 35° \qquad T_{AC} = 305\text{ N} \blacktriangleleft$$

(*b*)
$$T_{BC} = \frac{500\text{ N}}{\sin 70°}\sin 75° \qquad T_{BC} = 514\text{ N} \blacktriangleleft$$

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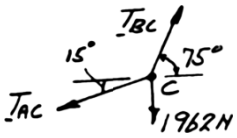


PROBLEM 2.47

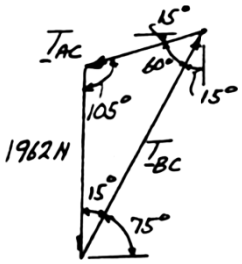
Two cables are tied together at C and are loaded as shown. Determine the tension (*a*) in cable AC, (*b*) in cable BC.

SOLUTION

Free-Body Diagram



Force Triangle



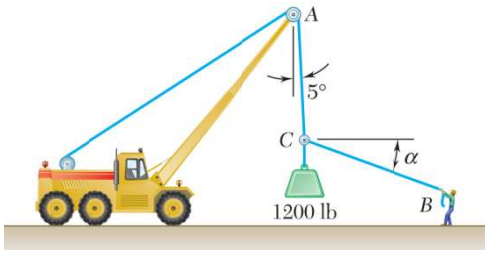
$$W = mg$$
$$= (200\text{ kg})(9.81\text{ m/s}^2)$$
$$= 1962\text{ N}$$

Law of sines: $$\frac{T_{AC}}{\sin 15^\circ} = \frac{T_{BC}}{\sin 105^\circ} = \frac{1962\text{ N}}{\sin 60^\circ}$$

(*a*) $$T_{AC} = \frac{(1962\text{ N})\ \sin 15^\circ}{\sin\ 60^\circ}$$ $$T_{AC} = 586\text{ N} \blacktriangleleft$$

(*b*) $$T_{BC} = \frac{(1962\text{ N})\sin 105^\circ}{\sin\ 60^\circ}$$ $$T_{BC} = 2190\text{ N} \blacktriangleleft$$

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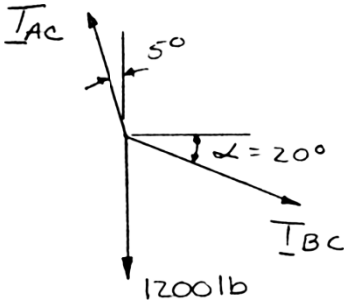


PROBLEM 2.48

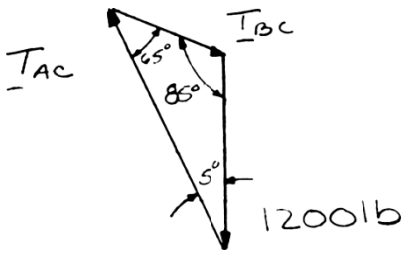
Knowing that $\alpha = 20°$, determine the tension (*a*) in cable *AC*, (*b*) in rope *BC*.

SOLUTION

Free-Body Diagram



Force Triangle

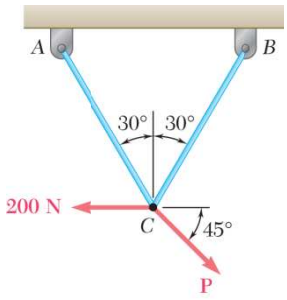


Law of sines:
$$\frac{T_{AC}}{\sin 110°} = \frac{T_{BC}}{\sin 5°} = \frac{1200 \text{ lb}}{\sin 65°}$$

(*a*)
$$T_{AC} = \frac{1200 \text{ lb}}{\sin 65°} \sin 110° \qquad T_{AC} = 1244 \text{ lb} \blacktriangleleft$$

(*b*)
$$T_{BC} = \frac{1200 \text{ lb}}{\sin 65°} \sin 5° \qquad T_{BC} = 115.4 \text{ lb} \blacktriangleleft$$

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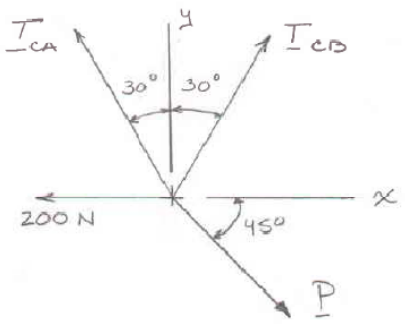


PROBLEM 2.49

Two cables are tied together at C and are loaded as shown. Knowing that P = 300 N, determine the tension in cables AC and BC.

SOLUTION

Free-Body Diagram



$\pm\rightarrow \Sigma F_x = 0 \qquad -T_{CA}\sin 30^\circ + T_{CB}\sin 30^\circ - P\cos 45^\circ - 200\text{N} = 0$

For $P = 200\text{N}$ we have,

$$-0.5T_{CA} + 0.5T_{CB} + 212.13 - 200 = 0 \quad (1)$$

$+\uparrow \Sigma F_y = 0 \qquad T_{CA}\cos 30^\circ - T_{CB}\cos 30^\circ - P\sin 45^\circ = 0$

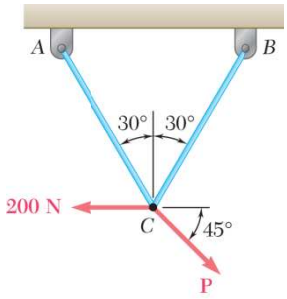
$$0.86603T_{CA} + 0.86603T_{CB} - 212.13 = 0 \quad (2)$$

Solving equations (1) and (2) simultaneously gives,

$T_{CA} = 134.6\text{ N}$ ◀

$T_{CB} = 110.4\text{ N}$ ◀

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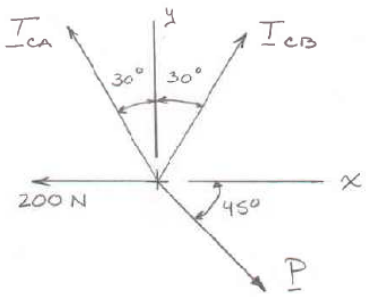


PROBLEM 2.50

Two cables are tied together at C and are loaded as shown. Determine the range of values of **P** for which both cables remain taut.

SOLUTION

Free-Body Diagram



$\pm\rightarrow \Sigma F_x = 0 \qquad -T_{CA}\sin 30^\circ + T_{CB}\sin 30^\circ - P\cos 45^\circ - 200\text{N} = 0$

For $T_{CA} = 0$ we have,

$$0.5T_{CB} + 0.70711P - 200 = 0 \quad (1)$$

$+\uparrow \Sigma F_y = 0 \qquad T_{CA}\cos 30^\circ - T_{CB}\cos 30^\circ - P\sin 45^\circ = 0$; again setting $T_{CA} = 0$ yields,

$$0.86603T_{CB} - 0.70711P = 0 \quad (2)$$

Adding equations (1) and (2) gives, $1.36603T_{CB} = 200$ hence $T_{CB} = 146.410\text{N}$ and $P = 179.315\text{N}$

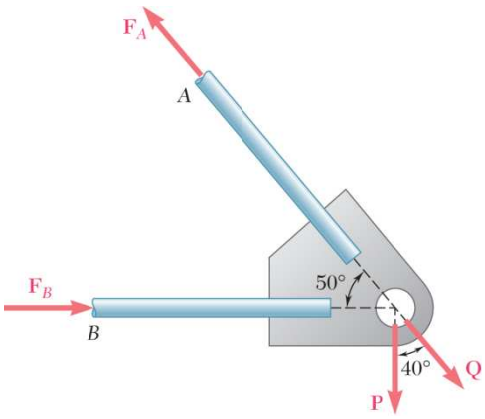
Substituting for $T_{CB} = 0$ into the equilibrium equations and solving simultaneously gives,

$$-0.5T_{CA} + 0.70711P - 200 = 0$$
$$0.86603T_{CA} - 0.70711P = 0$$

And $T_{CA} = 546.40\text{N}$, $P = 669.20\text{N}$ Thus for both cables to remain taut, load P must be within the range of 179.315 N and 669.20 N.

179.3 N <P< 669 N ◀

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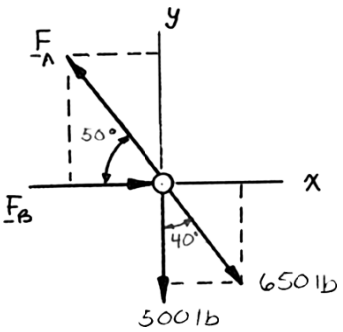


PROBLEM 2.51

Two forces **P** and **Q** are applied as shown to an aircraft connection. Knowing that the connection is in equilibrium and that $P = 500$ lb and $Q = 650$ lb, determine the magnitudes of the forces exerted on the rods A and B.

SOLUTION

Free-Body Diagram



Resolving the forces into x- and y-directions:

$$\mathbf{R} = \mathbf{P} + \mathbf{Q} + \mathbf{F}_A + \mathbf{F}_B = 0$$

Substituting components:

$$\begin{aligned}\mathbf{R} &= -(500\text{ lb})\mathbf{j} + [(650\text{ lb})\cos 50°]\mathbf{i} \\ &\quad -[(650\text{ lb})\sin 50°]\mathbf{j} \\ &\quad + F_B\mathbf{i} - (F_A\cos 50°)\mathbf{i} + (F_A\sin 50°)\mathbf{j} = 0\end{aligned}$$

In the y-direction (one unknown force):

$$-500\text{ lb} - (650\text{ lb})\sin 50° + F_A\sin 50° = 0$$

Thus,

$$F_A = \frac{500\text{ lb} + (650\text{ lb})\sin 50°}{\sin 50°}$$

$$= 1302.70\text{ lb}$$

$$F_A = 1303\text{ lb} \blacktriangleleft$$

In the x-direction:

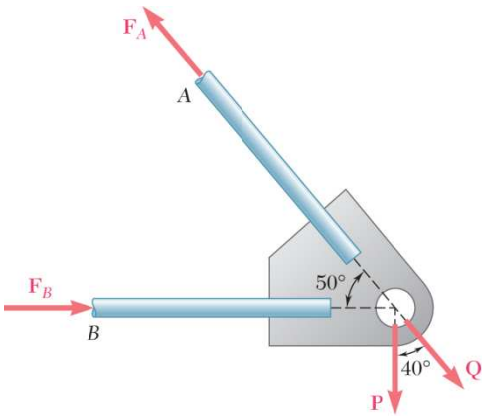
$$(650\text{ lb})\cos 50° + F_B - F_A\cos 50° = 0$$

Thus,

$$\begin{aligned}F_B &= F_A\cos 50° - (650\text{ lb})\cos 50° \\ &= (1302.70\text{ lb})\cos 50° - (650\text{ lb})\cos 50° \\ &= 419.55\text{ lb}\end{aligned}$$

$$F_B = 420\text{ lb} \blacktriangleleft$$

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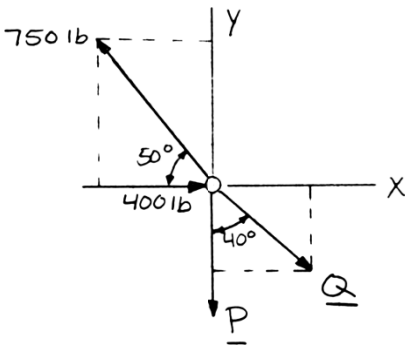


PROBLEM 2.52

Two forces **P** and **Q** are applied as shown to an aircraft connection. Knowing that the connection is in equilibrium and that the magnitudes of the forces exerted on rods A and B are $F_A = 750\,\text{lb}$ and $F_B = 400\,\text{lb}$, determine the magnitudes of **P** and **Q**.

SOLUTION

Free-Body Diagram



Resolving the forces into x- and y-directions:

$$\mathbf{R} = \mathbf{P} + \mathbf{Q} + \mathbf{F}_A + \mathbf{F}_B = 0$$

Substituting components:

$$\mathbf{R} = -P\mathbf{j} + Q\cos 50°\mathbf{i} - Q\sin 50°\mathbf{j} - [(750\text{ lb})\cos 50°]\mathbf{i} + [(750\text{ lb})\sin 50°]\mathbf{j} + (400\text{ lb})\mathbf{i}$$

In the x-direction (one unknown force):

$$Q\cos 50° - [(750\text{ lb})\cos 50°] + 400\text{ lb} = 0$$

$$Q = \frac{(750\text{ lb})\cos 50° - 400\text{ lb}}{\cos 50°}$$

$$= 127.710\text{ lb}$$

In the y-direction:

$$-P - Q\sin 50° + (750\text{ lb})\sin 50° = 0$$

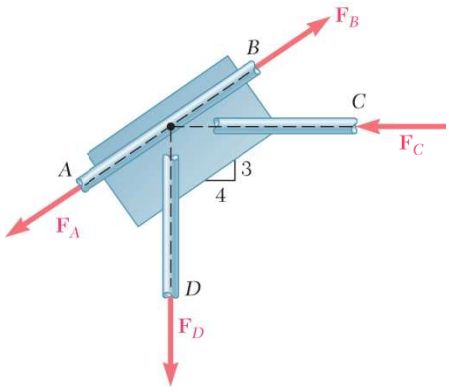
$$P = -Q\sin 50° + (750\text{ lb})\sin 50°$$

$$= -(127.710\text{ lb})\sin 50° + (750\text{ lb})\sin 50°$$

$$= 476.70\text{ lb}$$

$P = 477\text{ lb}$; $Q = 127.7\text{ lb}$ ◀

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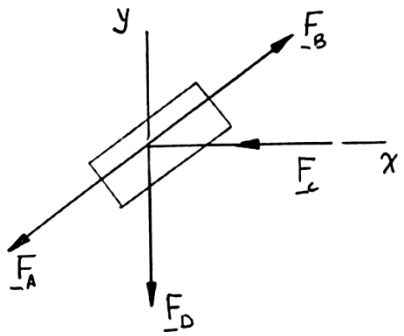


PROBLEM 2.53

A welded connection is in equilibrium under the action of the four forces shown. Knowing that $F_A = 8$ kN and $F_B = 16$ kN, determine the magnitudes of the other two forces.

SOLUTION

Free-Body Diagram of Connection



$$\Sigma F_x = 0: \quad \frac{3}{5}F_B - F_C - \frac{3}{5}F_A = 0$$

With $F_A = 8$ kN

$F_B = 16$ kN

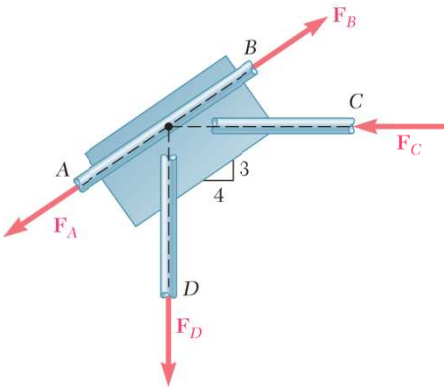
$$F_C = \frac{4}{5}(16\text{ kN}) - \frac{4}{5}(8\text{ kN}) \qquad F_C = 6.40\text{ kN} \blacktriangleleft$$

$$\Sigma F_y = 0: \quad -F_D + \frac{3}{5}F_B - \frac{3}{5}F_A = 0$$

With F_A and F_B as above:

$$F_D = \frac{3}{5}(16\text{ kN}) - \frac{3}{5}(8\text{ kN}) \qquad F_D = 4.80\text{ kN} \blacktriangleleft$$

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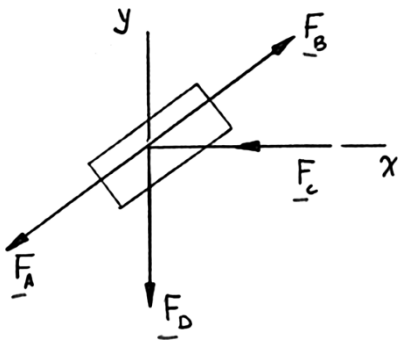


PROBLEM 2.54

A welded connection is in equilibrium under the action of the four forces shown. Knowing that $F_A = 5$ kN and $F_D = 6$ kN, determine the magnitudes of the other two forces.

SOLUTION

Free-Body Diagram of Connection



$$\Sigma F_y = 0: \quad -F_D - \frac{3}{5}F_A + \frac{3}{5}F_B = 0$$

or $$F_B = F_D + \frac{3}{5}F_A$$

With $$F_A = 5 \text{ kN}, \quad F_D = 8 \text{ kN}$$

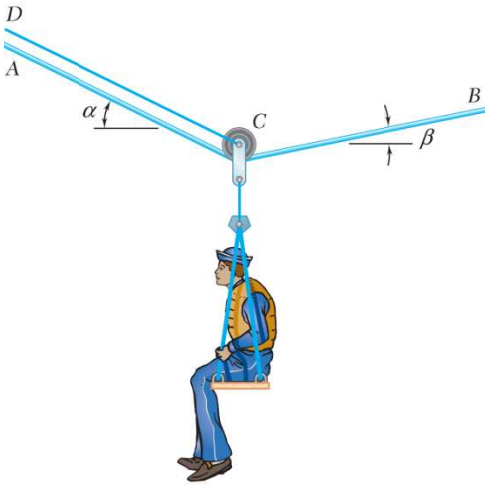
$$F_B = \frac{5}{3}\left[6 \text{ kN} + \frac{3}{5}(5 \text{ kN})\right] \qquad F_B = 15.00 \text{ kN} \blacktriangleleft$$

$$\Sigma F_x = 0: \quad -F_C + \frac{4}{5}F_B - \frac{4}{5}F_A = 0$$

$$F_C = \frac{4}{5}(F_B - F_A)$$

$$= \frac{4}{5}(15 \text{ kN} - 5 \text{ kN}) \qquad F_C = 8.00 \text{ kN} \blacktriangleleft$$

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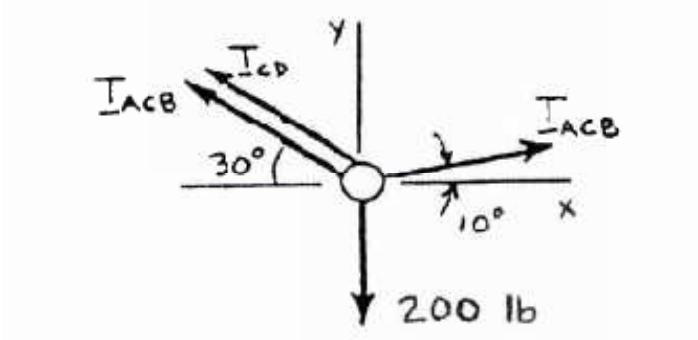


PROBLEM 2.55

A sailor is being rescued using a boatswain's chair that is suspended from a pulley that can roll freely on the support cable ACB and is pulled at a constant speed by cable CD. Knowing that $\alpha = 30°$ and $\beta = 10°$ and that the combined weight of the boatswain's chair and the sailor is 200 lb, determine the tension (*a*) in the support cable ACB, (*b*) in the traction cable CD.

SOLUTION

Free-Body Diagram



$$\stackrel{+}{\rightarrow} \Sigma F_x = 0: \quad T_{ACB}\cos 10° - T_{ACB}\cos 30° - T_{CD}\cos 30° = 0$$

$$T_{CD} = 0.137158\,T_{ACB} \tag{1}$$

$$+\uparrow \Sigma F_y = 0: \quad T_{ACB}\sin 10° + T_{ACB}\sin 30° + T_{CD}\sin 30° - 200 = 0$$

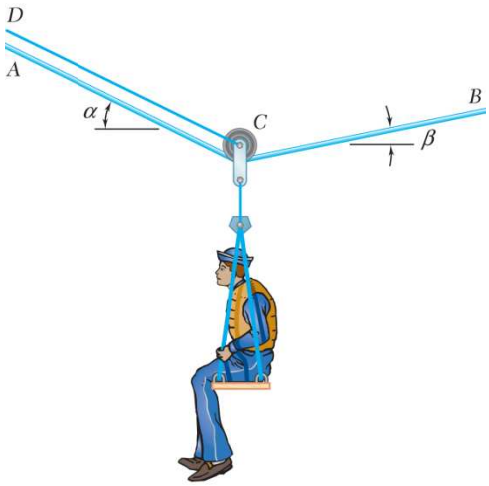
$$0.67365\,T_{ACB} + 0.5\,T_{CD} = 200 \tag{2}$$

(*a*) Substitute (1) into (2): $0.67365\,T_{ACB} + 0.5(0.137158\,T_{ACB}) = 200$

$$T_{ACB} = 269.46 \text{ lb} \qquad T_{ACB} = 269 \text{ lb} \blacktriangleleft$$

(*b*) From (1): $T_{CD} = 0.137158(269.46 \text{ lb})$ $\qquad T_{CD} = 37.0 \text{ lb} \blacktriangleleft$

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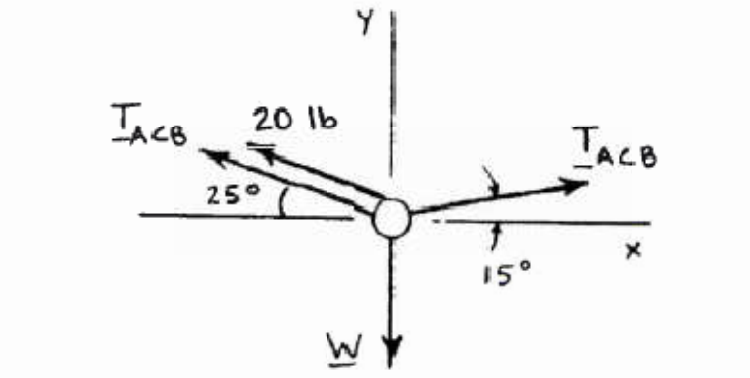


PROBLEM 2.56

A sailor is being rescued using a boatswain's chair that is suspended from a pulley that can roll freely on the support cable *ACB* and is pulled at a constant speed by cable *CD*. Knowing that $\alpha = 25°$ and $\beta = 15°$ and that the tension in cable *CD* is 20 lb, determine (*a*) the combined weight of the boatswain's chair and the sailor, (*b*) the tension in the support cable *ACB*.

SOLUTION

Free-Body Diagram



$$\stackrel{+}{\rightarrow} \Sigma F_x = 0: \quad T_{ACB}\cos 15° - T_{ACB}\cos 25° - (20\text{ lb})\cos 25° = 0$$

$$T_{ACB} = 304.04\text{ lb}$$

$$+\uparrow \Sigma F_y = 0: \quad (304.04\text{ lb})\sin 15° + (304.04\text{ lb})\sin 25°$$

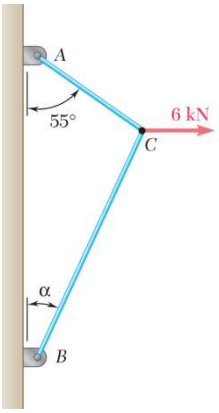
$$+(20\text{ lb})\sin 25° - W = 0$$

$$W = 215.64\text{ lb}$$

(*a*) $W = 216\text{ lb}$ ◀

(*b*) $T_{ACB} = 304\text{ lb}$ ◀

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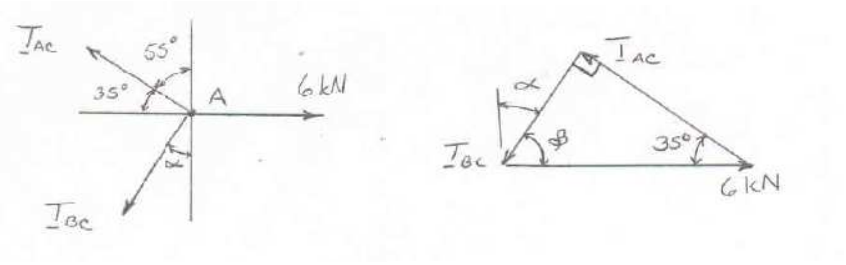


PROBLEM 2.57

For the cables of prob. 2.44, find the value of α for which the tension is as small as possible (*a*) in cable *bc*, (*b*) in both cables simultaneously. In each case determine the tension in each cable.

SOLUTION

Free-Body Diagram **Force Triangle**



(*a*) For a minimum tension in cable *BC,* set angle between cables to 90 degrees.

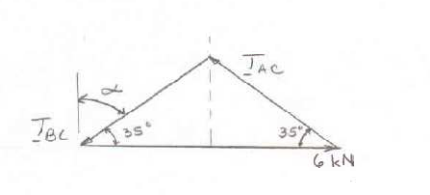
By inspection, $\alpha = 35.0^\circ$ ◀

$$T_{AC} = (6\text{ kN})\cos 35^\circ \qquad T_{AC} = 4.91\text{ kN}$$ ◀

$$T_{BC} = (6\text{ kN})\sin 35^\circ \qquad T_{BC} = 3.44\text{ kN}$$ ◀

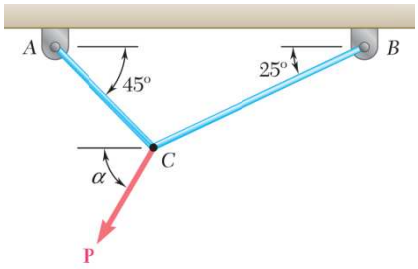
(*b*) For equal tension in both cables, the force triangle will be an isosceles.

Therefore, by inspection, $\alpha = 55.0^\circ$ ◀



$$T_{AC} = T_{BC} = (1/2)\frac{6\text{ kN}}{\cos 35^\circ} \qquad T_{AC} = T_{BC} = 3.66\text{ kN}$$ ◀

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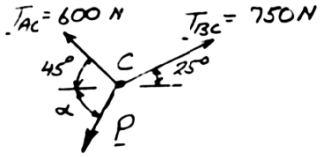


PROBLEM 2.58

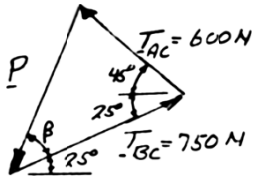
For the cables of Problem 2.46, it is known that the maximum allowable tension is 600 N in cable *AC* and 750 N in cable *BC*. Determine (*a*) the maximum force **P** that can be applied at *C*, (*b*) the corresponding value of α.

SOLUTION

Free-Body Diagram



Force Triangle



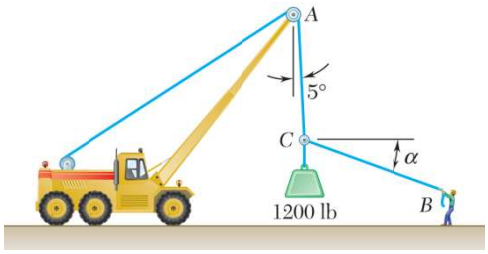
(*a*) Law of cosines $P^2 = (600)^2 + (750)^2 - 2(600)(750)\cos(25° + 45°)$

$P = 784.02$ N $\qquad P = 784$ N ◀

(*b*) Law of sines $\dfrac{\sin\beta}{600\text{ N}} = \dfrac{\sin(25° + 45°)}{784.02\text{ N}}$

$\beta = 46.0° \qquad \therefore \quad \alpha = 46.0° + 25°$ $\qquad \alpha = 71.0°$ ◀

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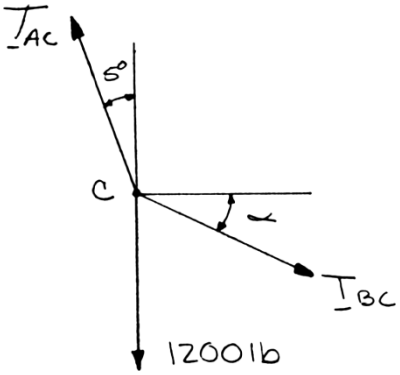


PROBLEM 2.59

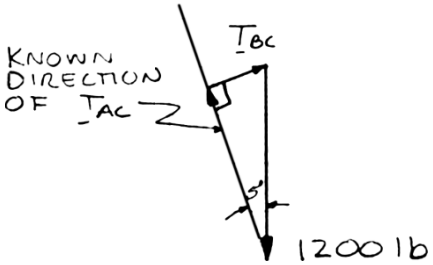
For the situation described in Figure P2.48, determine (*a*) the value of α for which the tension in rope *BC* is as small as possible, (*b*) the corresponding value of the tension.

SOLUTION

Free-Body Diagram



Force Triangle

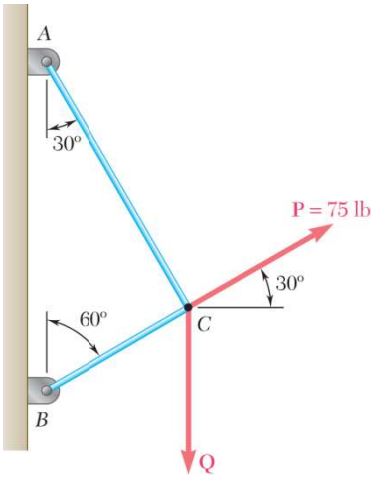


To be smallest, T_{BC} must be perpendicular to the direction of T_{AC}.

(*a*) Thus, $\alpha = 5.00°$ $\alpha = 5.00°$ ◀

(*b*) $T_{BC} = (1200 \text{ lb}) \sin 5°$ $T_{BC} = 104.6 \text{ lb}$ ◀

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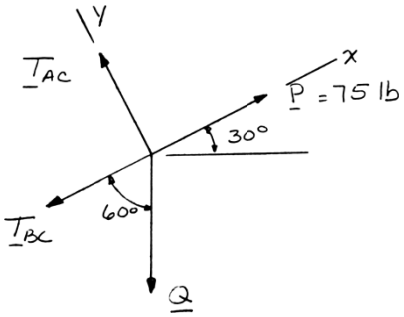


PROBLEM 2.60

Two cables tied together at C are loaded as shown. Determine the range of values of Q for which the tension will not exceed 60 lb in either cable.

SOLUTION

Free-Body Diagram



$$\Sigma F_x = 0: \quad -T_{BC} - Q\cos 60° + 75 \text{ lb} = 0$$

$$T_{BC} = 75 \text{ lb} - Q\cos 60° \tag{1}$$

$$\Sigma F_y = 0: \quad T_{AC} - Q\sin 60° = 0$$

$$T_{AC} = Q\sin 60° \tag{2}$$

Requirement: $T_{AC} = 60$ lb:

From Eq. (2): $Q\sin 60° = 60$ lb

$$Q = 69.3 \text{ lb}$$

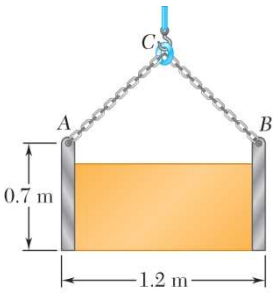
Requirement: $T_{BC} = 60$ lb:

From Eq. (1): $75 \text{ lb} - Q\cos 60° = 60$ lb

$$Q = 30.0 \text{ lb}$$

$30.0 \text{ lb} \le Q \le 69.3 \text{ lb}$ ◀

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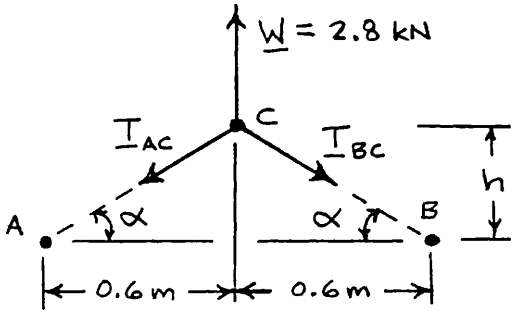


PROBLEM 2.61

A movable bin and its contents have a combined weight of 2.8 kN. Determine the shortest chain sling *ACB* that can be used to lift the loaded bin if the tension in the chain is not to exceed 5 kN.

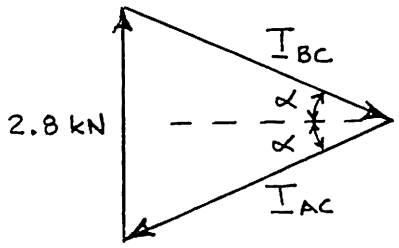
SOLUTION

Free-Body Diagram



$$\tan\alpha = \frac{h}{0.6\text{ m}} \qquad (1)$$

Isosceles Force Triangle



Law of sines: $\sin\alpha = \dfrac{\frac{1}{2}(2.8\text{ kN})}{T_{AC}}$

$$T_{AC} = 5\text{ kN}$$

$$\sin\alpha = \frac{\frac{1}{2}(2.8\text{ kN})}{5\text{ kN}}$$

$$\alpha = 16.2602^\circ$$

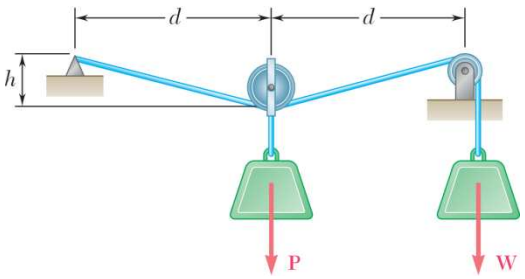
From Eq. (1): $\tan 16.2602^\circ = \dfrac{h}{0.6\text{ m}} \qquad \therefore \quad h = 0.175000\text{ m}$

Half-length of chain $= AC = \sqrt{(0.6\text{ m})^2 + (0.175\text{ m})^2}$

$$= 0.625\text{ m}$$

Total length: $= 2 \times 0.625\text{ m}$ 1.250 m ◀

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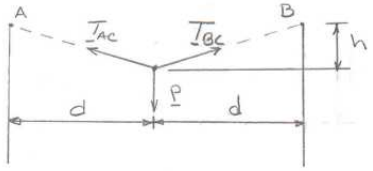


PROBLEM 2.62

For $W = 800$ N, $P = 200$ N, and $d = 600$ mm, determine the value of h consistent with equilibrium.

SOLUTION

Free-Body Diagram



$$T_{AC} = T_{BC} = 800 \text{ N}$$

$$AC = BC = \sqrt{\left(h^2 + d^2\right)}$$

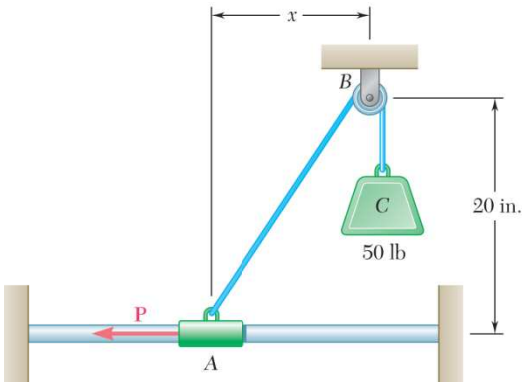
$$\Sigma F_y = 0: \quad 2(800 \text{ N})\frac{h}{\sqrt{h^2 + d^2}} - P = 0$$

$$800 = \frac{P}{2}\sqrt{1 + \left(\frac{d}{h}\right)^2}$$

Data: $P = 200$ N, $d = 600$ mm and solving for h

$$800 \text{ N} = \frac{200 \text{ N}}{2}\sqrt{1 + \left(\frac{600 \text{ mm}}{h}\right)^2}$$

$$h = 75.6 \text{ mm} \blacktriangleleft$$

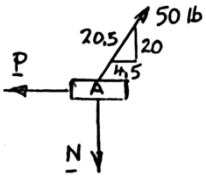


PROBLEM 2.63

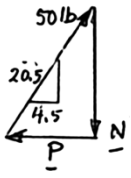
Collar A is connected as shown to a 50-lb load and can slide on a frictionless horizontal rod. Determine the magnitude of the force **P** required to maintain the equilibrium of the collar when (*a*) $x = 4.5$ in., (*b*) $x = 15$ in.

SOLUTION

(*a*) **Free Body: Collar *A***



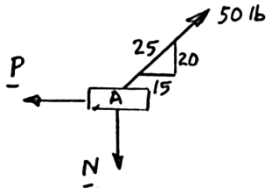
Force Triangle



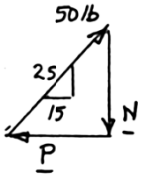
$$\frac{P}{4.5} = \frac{50 \text{ lb}}{20.5}$$

$$P = 10.98 \text{ lb} \blacktriangleleft$$

(*b*) **Free Body: Collar *A***



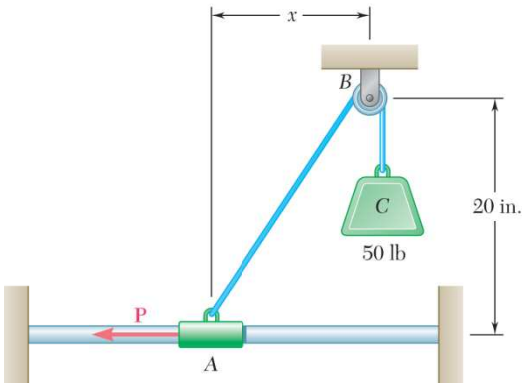
Force Triangle



$$\frac{P}{15} = \frac{50 \text{ lb}}{25}$$

$$P = 30.0 \text{ lb} \blacktriangleleft$$

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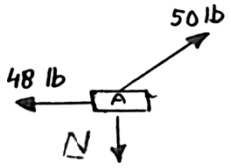


PROBLEM 2.64

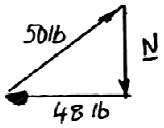
Collar A is connected as shown to a 50-lb load and can slide on a frictionless horizontal rod. Determine the distance x for which the collar is in equilibrium when $P = 48$ lb.

SOLUTION

Free Body: Collar *A*



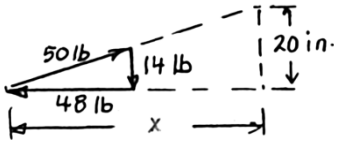
Force Triangle



$$N^2 = (50)^2 - (48)^2 = 196$$

$$N = 14.00 \text{ lb}$$

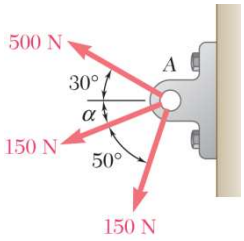
Similar Triangles



$$\frac{x}{20 \text{ in.}} = \frac{48 \text{ lb}}{14 \text{ lb}}$$

$x = 68.6$ in. ◀

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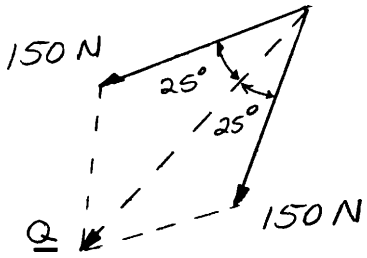


PROBLEM 2.65

Three forces are applied to a bracket as shown. The directions of the two 150-N forces may vary, but the angle between these forces is always 50°. Determine the range of values of α for which the magnitude of the resultant of the forces acting at A is less than 600 N.

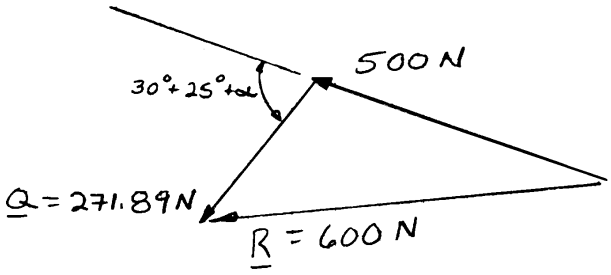
SOLUTION

Combine the two 150-N forces into a resultant force Q:



$$Q = 2(150\text{ N})\cos 25°$$
$$= 271.89\text{ N}$$

Equivalent loading at A:



Using the law of cosines:

$$(600\text{ N})^2 = (500\text{ N})^2 + (271.89\text{ N})^2 + 2(500\text{ N})(271.89\text{ N})\cos(55° + \alpha)$$
$$\cos(55° + \alpha) = 0.132685$$

Two values for α: $55° + \alpha = 82.375$

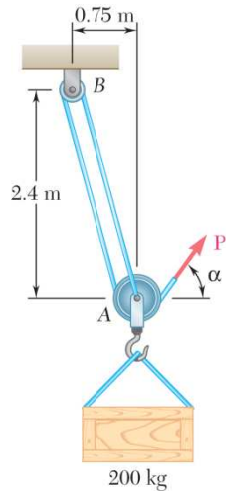
$$\alpha = 27.4°$$

$$55° + \alpha = -82.375°$$
$$55° + \alpha = 360° - 82.375°$$

or $\alpha = 222.6°$

For $R < 600$ lb: $27.4° < \alpha < 222.6°$ ◀

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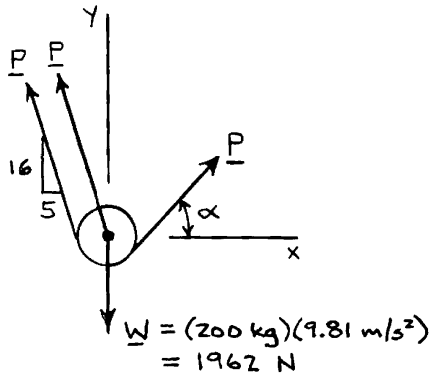


PROBLEM 2.66

A 200-kg crate is to be supported by the rope-and-pulley arrangement shown. Determine the magnitude and direction of the force **P** that must be exerted on the free end of the rope to maintain equilibrium. (*Hint:* The tension in the rope is the same on each side of a simple pulley. This can be proved by the methods of Ch. 4.)

SOLUTION

Free-Body Diagram: Pulley *A*



$$\stackrel{+}{\rightarrow}\Sigma F_x = 0: \quad -2P\left(\frac{5}{\sqrt{281}}\right) + P\cos\alpha = 0$$

$$\cos\alpha = 0.59655$$

$$\alpha = \pm 53.377°$$

For $\alpha = +53.377°$:

$$+\uparrow \Sigma F_y = 0: \quad 2P\left(\frac{16}{\sqrt{281}}\right) + P\sin 53.377° - 1962\ \text{N} = 0$$

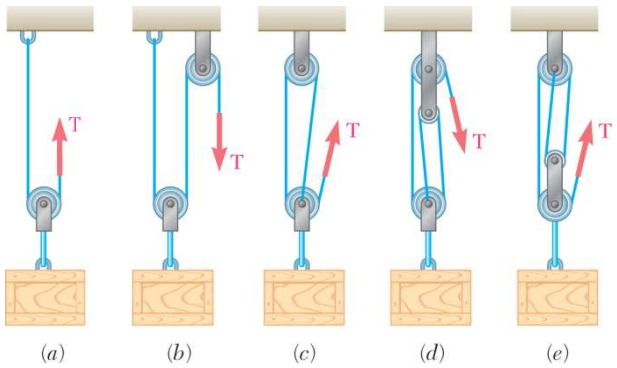
$$\mathbf{P} = 724\ \text{N} \measuredangle 53.4° \blacktriangleleft$$

For $\alpha = -53.377°$:

$$+\uparrow \Sigma F_y = 0: \quad 2P\left(\frac{16}{\sqrt{281}}\right) + P\sin(-53.377°) - 1962\ \text{N} = 0$$

$$\mathbf{P} = 1773 \measuredangle 53.4° \blacktriangleleft$$

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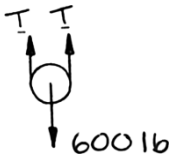
PROBLEM 2.67

A 600-lb crate is supported by several rope-and-pulley arrangements as shown. Determine for each arrangement the tension in the rope. (See the hint for Problem 2.66.)

SOLUTION

Free-Body Diagram of Pulley

(*a*)

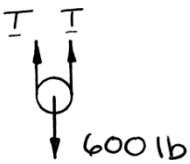


$$+\uparrow \Sigma F_y = 0: \quad 2T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{2}(600 \text{ lb})$$

$$T = 300 \text{ lb} \blacktriangleleft$$

(*b*)

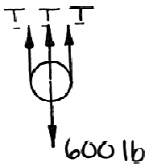


$$+\uparrow \Sigma F_y = 0: \quad 2T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{2}(600 \text{ lb})$$

$$T = 300 \text{ lb} \blacktriangleleft$$

(*c*)

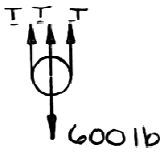


$$+\uparrow \Sigma F_y = 0: \quad 3T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{3}(600 \text{ lb})$$

$$T = 200 \text{ lb} \blacktriangleleft$$

(*d*)

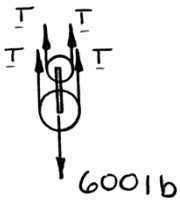


$$+\uparrow \Sigma F_y = 0: \quad 3T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{3}(600 \text{ lb})$$

$$T = 200 \text{ lb} \blacktriangleleft$$

(*e*)

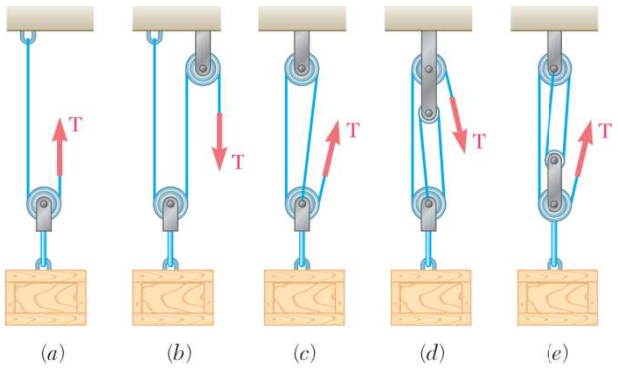


$$+\uparrow \Sigma F_y = 0: \quad 4T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{4}(600 \text{ lb})$$

$$T = 150.0 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.68

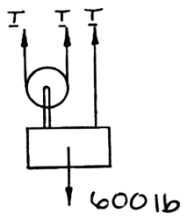
Solve Parts *b* and *d* of Problem 2.67, assuming that the free end of the rope is attached to the crate.

PROBLEM 2.67 A 600-lb crate is supported by several rope-and-pulley arrangements as shown. Determine for each arrangement the tension in the rope. (See the hint for Problem 2.66.)

SOLUTION

Free-Body Diagram of Pulley and Crate

(*b*)

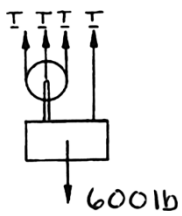


$$+\uparrow \Sigma F_y = 0: \quad 3T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{3}(600 \text{ lb})$$

$$T = 200 \text{ lb} \blacktriangleleft$$

(*d*)

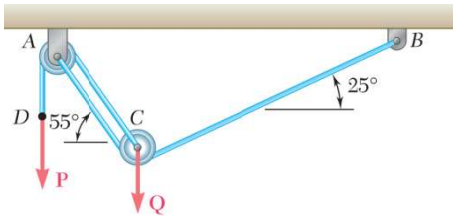


$$+\uparrow \Sigma F_y = 0: \quad 4T - (600 \text{ lb}) = 0$$

$$T = \frac{1}{4}(600 \text{ lb})$$

$$T = 150.0 \text{ lb} \blacktriangleleft$$

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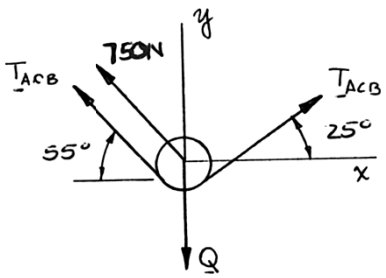


PROBLEM 2.69

A load **Q** is applied to the pulley *C*, which can roll on the cable *ACB*. The pulley is held in the position shown by a second cable *CAD*, which passes over the pulley *A* and supports a load **P**. Knowing that $P = 750$ N, determine (*a*) the tension in cable *ACB*, (*b*) the magnitude of load **Q**.

SOLUTION

Free-Body Diagram: Pulley *C*



(*a*) $\pm\rightarrow \Sigma F_x = 0$: $T_{ACB}(\cos 25° - \cos 55°) - (750\text{ N})\cos 55° = 0$

Hence: $T_{ACB} = 1292.88$ N

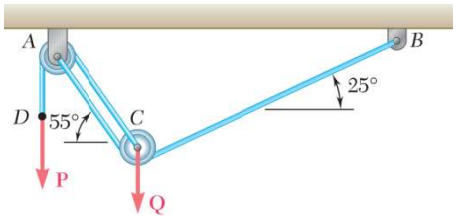
$T_{ACB} = 1293$ N ◀

(*b*) $+\uparrow \Sigma F_y = 0$: $T_{ACB}(\sin 25° + \sin 55°) + (750\text{ N})\sin 55° - Q = 0$

$(1292.88\text{ N})(\sin 25° + \sin 55°) + (750\text{ N})\sin 55° - Q = 0$

or $Q = 2219.8$ N $\quad Q = 2220$ N ◀

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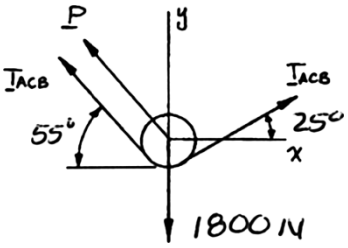


PROBLEM 2.70

An 1800-N load **Q** is applied to the pulley *C*, which can roll on the cable *ACB*. The pulley is held in the position shown by a second cable *CAD*, which passes over the pulley *A* and supports a load **P**. Determine (*a*) the tension in cable *ACB*, (*b*) the magnitude of load **P**.

SOLUTION

Free-Body Diagram: Pulley *C*



$$\overset{+}{\rightarrow}\Sigma F_x = 0: \quad T_{ACB}(\cos 25° - \cos 55°) - P\cos 55° = 0$$

or
$$P = 0.58010T_{ACB} \quad (1)$$

$$+\uparrow \Sigma F_y = 0: \quad T_{ACB}(\sin 25° + \sin 55°) + P\sin 55° - 1800\text{ N} = 0$$

or
$$1.24177T_{ACB} + 0.81915P = 1800\text{ N} \quad (2)$$

(*a*) Substitute Equation (1) into Equation (2):

$$1.24177T_{ACB} + 0.81915(0.58010T_{ACB}) = 1800\text{ N}$$

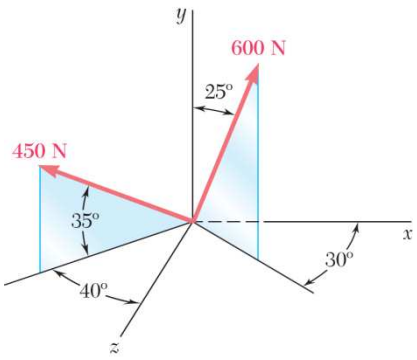
Hence:
$$T_{ACB} = 1048.37\text{ N}$$

$$T_{ACB} = 1048\text{ N} \blacktriangleleft$$

(*b*) Using (1), $P = 0.58010(1048.37\text{ N}) = 608.16\text{ N}$

$$P = 608\text{ N} \blacktriangleleft$$

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PROBLEM 2.71

Determine (*a*) the *x*, *y*, and *z* components of the 600-N force, (*b*) the angles θ_x, θ_y, and θ_z that the force forms with the coordinate axes.

SOLUTION

(*a*)

$$F_x = (600\text{ N})\sin 25^\circ \cos 30^\circ$$

$$F_x = 219.60\text{ N} \qquad F_x = 220\text{ N} \blacktriangleleft$$

$$F_y = (600\text{ N})\cos 25^\circ$$

$$F_y = 543.78\text{ N} \qquad F_y = 544\text{ N} \blacktriangleleft$$

$$F_z = (380.36\text{ N})\sin 25^\circ \sin 30^\circ$$

$$F_z = 126.785\text{ N} \qquad F_z = 126.8\text{ N} \blacktriangleleft$$

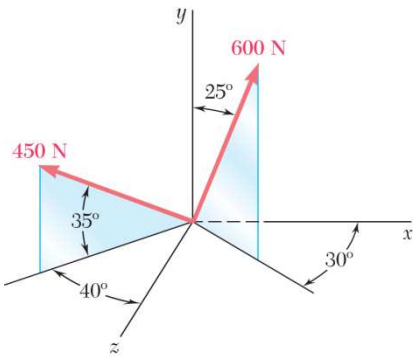
(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{219.60\text{ N}}{600\text{ N}} \qquad \theta_x = 68.5^\circ \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{543.78\text{ N}}{600\text{ N}} \qquad \theta_y = 25.0^\circ \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{126.785\text{ N}}{600\text{ N}} \qquad \theta_z = 77.8^\circ \blacktriangleleft$$

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PROBLEM 2.72

Determine (*a*) the *x*, *y*, and *z* components of the 450-N force, (*b*) the angles θ_x, θ_y, and θ_z that the force forms with the coordinate axes.

SOLUTION

(*a*)

$$F_x = -(450\text{ N})\cos 35^\circ \sin 40^\circ$$

$$F_x = -236.94\text{ N} \qquad F_x = -237\text{ N} \blacktriangleleft$$

$$F_y = (450\text{ N})\sin 35^\circ$$

$$F_y = 258.11\text{ N} \qquad F_y = 258\text{ N} \blacktriangleleft$$

$$F_z = (450\text{ N})\cos 35^\circ \cos 40^\circ$$

$$F_z = 282.38\text{ N} \qquad F_z = 282\text{ N} \blacktriangleleft$$

(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{-236.94\text{ N}}{450\text{ N}} \qquad \theta_x = 121.8^\circ \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{258.11\text{ N}}{450\text{ N}} \qquad \theta_y = 55.0^\circ \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{282.38\text{ N}}{450\text{ N}} \qquad \theta_z = 51.1^\circ \blacktriangleleft$$

Note: From the given data, we could have computed directly $\theta_y = 90^\circ - 35^\circ = 55^\circ$, which checks with the answer obtained.

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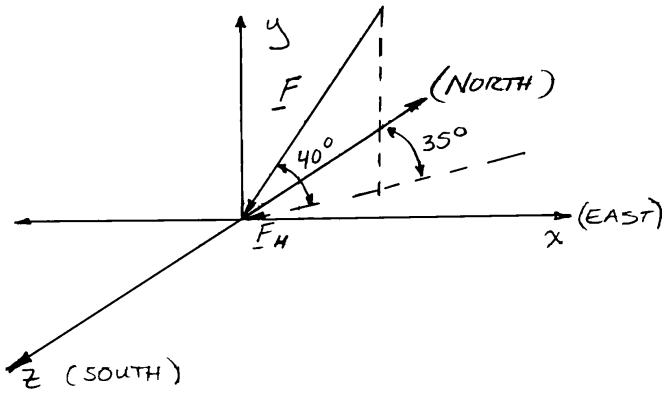
PROBLEM 2.73

A gun is aimed at a point A located 35° east of north. Knowing that the barrel of the gun forms an angle of 40° with the horizontal and that the maximum recoil force is 400 N, determine (*a*) the x, y, and z components of that force, (*b*) the values of the angles θ_x, θ_y, and θ_z defining the direction of the recoil force. (Assume that the x, y, and z axes are directed, respectively, east, up, and south.)

SOLUTION

Recoil force $F = 400 \text{ N}$

$$\therefore \quad F_H = (400 \text{ N}) \cos 40° = 306.42 \text{ N}$$



(*a*)

$$F_x = -F_H \sin 35° = -(306.42 \text{ N}) \sin 35° = -175.755 \text{ N}$$

$F_x = -175.8 \text{ N}$ ◀

$$F_y = -F \sin 40° = -(400 \text{ N}) \sin 40° = -257.12 \text{ N}$$

$F_y = -257 \text{ N}$ ◀

$$F_z = +F_H \cos 35° = +(306.42 \text{ N}) \cos 35° = +251.00 \text{ N}$$

$F_z = +251 \text{ N}$ ◀

(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{-175.755 \text{ N}}{400 \text{ N}}$$

$\theta_x = 116.1°$ ◀

$$\cos\theta_y = \frac{F_y}{F} = \frac{-257.12 \text{ N}}{400 \text{ N}}$$

$\theta_y = 130.0°$ ◀

$$\cos\theta_z = \frac{F_z}{F} = \frac{251.00 \text{ N}}{400 \text{ N}}$$

$\theta_z = 51.1°$ ◀

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PROBLEM 2.74

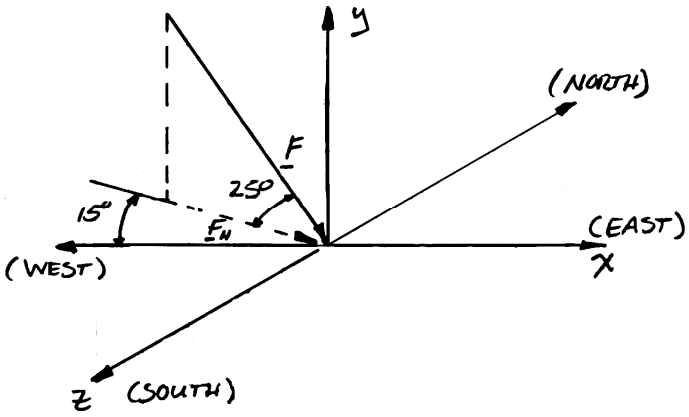
Solve Problem 2.73, assuming that point A is located 15° north of west and that the barrel of the gun forms an angle of 25° with the horizontal.

PROBLEM 2.73 A gun is aimed at a point A located 35° east of north. Knowing that the barrel of the gun forms an angle of 40° with the horizontal and that the maximum recoil force is 400 N, determine (*a*) the x, y, and z components of that force, (*b*) the values of the angles θ_x, θ_y, and θ_z defining the direction of the recoil force. (Assume that the x, y, and z axes are directed, respectively, east, up, and south.)

SOLUTION

Recoil force $F = 400 \text{ N}$

$$\therefore \quad F_H = (400 \text{ N})\cos 25° = 362.52 \text{ N}$$



(*a*)

$$F_x = +F_H \cos 15° = +(362.52 \text{ N})\cos 15° = +350.17 \text{ N}$$

$$F_x = +350 \text{ N} \blacktriangleleft$$

$$F_y = -F \sin 25° = -(400 \text{ N})\sin 25° = -169.047 \text{ N}$$

$$F_y = -169.0 \text{ N} \blacktriangleleft$$

$$F_z = +F_H \sin 15° = +(362.52 \text{ N})\sin 15° = +93.827 \text{ N}$$

$$F_z = +93.8 \text{ N} \blacktriangleleft$$

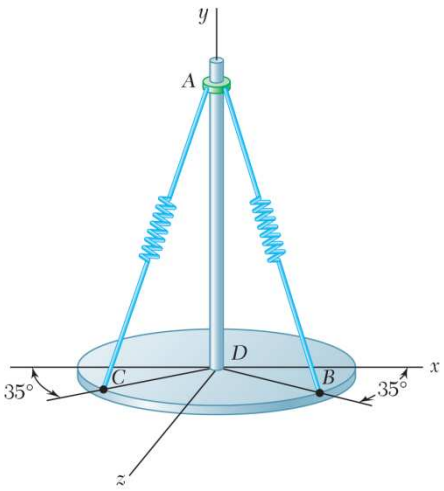
(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{+350.17 \text{ N}}{400 \text{ N}} \qquad \theta_x = 28.9° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{-169.047 \text{ N}}{400 \text{ N}} \qquad \theta_y = 115.0° \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{+93.827 \text{ N}}{400 \text{ N}} \qquad \theta_z = 76.4° \blacktriangleleft$$

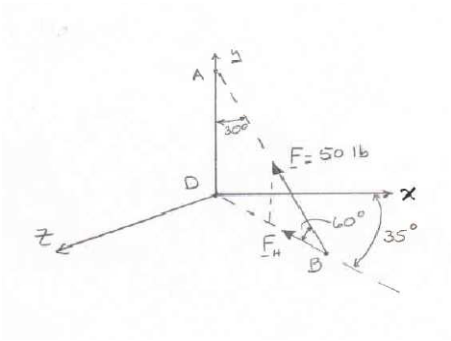
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PROBLEM 2.75

The angle between spring *AB* and the post *DA* is 30°. Knowing that the tension in the spring is 50 lb, determine (*a*) the *x*, *y*, and *z* components of the force exerted on the circular plate at *B*, (*b*) the angles θ_x, θ_y, and θ_z defining the direction of the force at *B*.

SOLUTION



$$F_h = F\cos 60°$$
$$= (50\text{ lb})\cos 60°$$
$$F_h = 25.0\text{ lb}$$

$$F_x = -F_h\cos 35° \qquad F_y = F\sin 60° \qquad F_z = -F_h\sin 35°$$
$$F_x = (-25.0\text{ lb})\cos 35° \qquad F_y = (50.0\text{ lb})\sin 60° \qquad F_z = (-25.0\text{ lb})\sin 35°$$
$$F_x = -20.479\text{ lb} \qquad F_y = 43.301\text{ lb} \qquad F_z = -14.3394\text{ lb}$$

(*a*)

$$F_x = -20.5\text{ lb} \blacktriangleleft$$
$$F_y = 43.3\text{ lb} \blacktriangleleft$$
$$F_z = -14.33\text{ lb} \blacktriangleleft$$

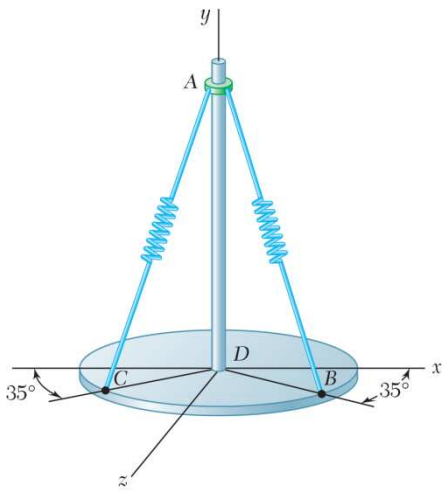
(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{-20.479\text{ lb}}{50\text{ lb}} \qquad \theta_x = 114.2° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{43.301\text{ lb}}{50\text{ lb}} \qquad \theta_y = 30.0° \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{-14.3394\text{ lb}}{50\text{ lb}} \qquad \theta_z = 106.7° \blacktriangleleft$$

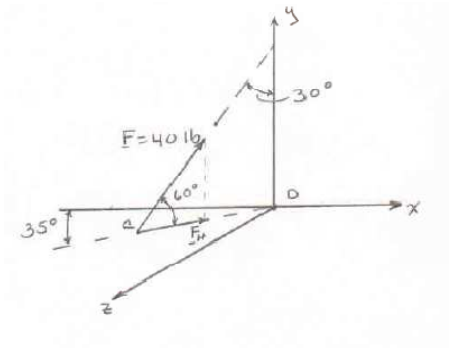
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PROBLEM 2.76

The angle between spring AC and the post DA is 30°. Knowing that the tension in the spring is 40 lb, determine (*a*) the x, y, and z components of the force exerted on the circular plate at C, (*b*) the angles θ_x, θ_y, and θ_z defining the direction of the force at C.

SOLUTION



$$F_h = F\cos 60°$$
$$= (40\text{ lb})\cos 60°$$
$$F_h = 20.0\text{ lb}$$

(*a*)

$$F_x = F_h \cos 35° \qquad F_y = F\sin 60° \qquad F_z = -F_h \sin 35°$$
$$= (20.0\text{ lb})\cos\ 35° \qquad = (40\text{ lb})\sin\ 60° \qquad = -(20.0\text{ lb})\sin 35°$$
$$F_x = 16.3830\text{ lb} \qquad F_y = 34.641\text{ lb} \qquad F_z = -11.4715\text{ lb}$$

$$F_x = 16.38\text{ lb} \blacktriangleleft$$
$$F_y = 34.6\text{ lb} \blacktriangleleft$$
$$F_z = -11.47\text{ lb} \blacktriangleleft$$

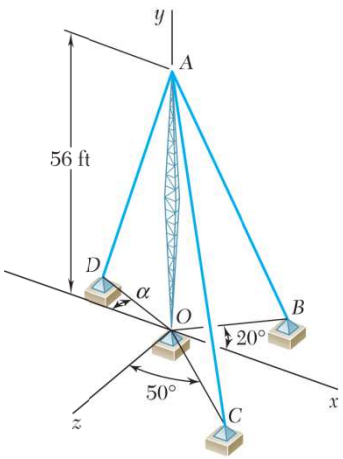
(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{16.3830\text{ lb}}{40\text{ lb}} \qquad \theta_x = 65.8° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{34.641\text{ lb}}{40\text{ lb}} \qquad \theta_y = 30.0° \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{-11.4715\text{ lb}}{40\text{ lb}} \qquad \theta_z = 106.7° \blacktriangleleft$$

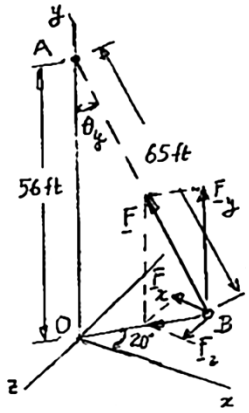
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PROBLEM 2.77

Cable AB is 65 ft long, and the tension in that cable is 3900 lb. Determine (a) the x, y, and z components of the force exerted by the cable on the anchor B, (b) the angles θ_x, θ_y, and θ_z defining the direction of that force.

SOLUTION



From triangle AOB:

$$\cos\theta_y = \frac{56\text{ ft}}{65\text{ ft}} = 0.86154$$

$$\theta_y = 30.51^\circ$$

(a)

$$F_x = -F\sin\theta_y\cos 20^\circ = -(3900\text{ lb})\sin 30.51^\circ\cos 20^\circ$$

$$F_x = -1861\text{ lb} \blacktriangleleft$$

$$F_y = +F\cos\theta_y = (3900\text{ lb})(0.86154) \qquad F_y = +3360\text{ lb} \blacktriangleleft$$

$$F_z = +(3900\text{ lb})\sin 30.51^\circ\sin 20^\circ \qquad F_z = +677\text{ lb} \blacktriangleleft$$

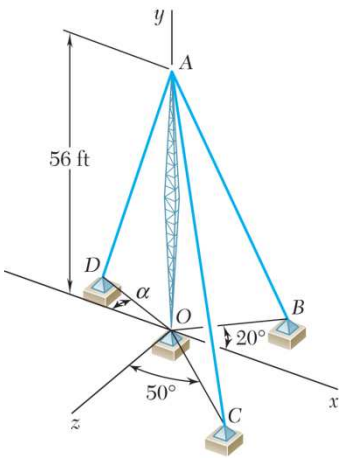
(b)

$$\cos\theta_x = \frac{F_x}{F} = -\frac{1861\text{ lb}}{3900\text{ lb}} = -0.4771 \qquad \theta_x = 118.5^\circ \blacktriangleleft$$

From above: $\theta_y = 30.51^\circ$ $\qquad \theta_y = 30.5^\circ \blacktriangleleft$

$$\cos\theta_z = \frac{F_z}{F} = +\frac{677\text{ lb}}{3900\text{ lb}} = +0.1736 \qquad \theta_z = 80.0^\circ \blacktriangleleft$$

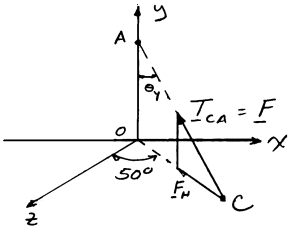
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PROBLEM 2.78

Cable AC is 70 ft long, and the tension in that cable is 5250 lb. Determine (a) the x, y, and z components of the force exerted by the cable on the anchor C, (b) the angles θ_x, θ_y, and θ_z defining the direction of that force.

SOLUTION



In triangle AOB:

$$AC = 70 \text{ ft}$$
$$OA = 56 \text{ ft}$$
$$F = 5250 \text{ lb}$$

$$\cos\theta_y = \frac{56 \text{ ft}}{70 \text{ ft}}$$
$$\theta_y = 36.870°$$
$$F_H = F\sin\theta_y$$
$$= (5250 \text{ lb})\sin 36.870°$$
$$= 3150.0 \text{ lb}$$

(a) $F_x = -F_H \sin 50° = -(3150.0 \text{ lb})\sin 50° = -2413.0 \text{ lb}$

$$F_x = -2410 \text{ lb} \blacktriangleleft$$

$F_y = +F\cos\theta_y = +(5250 \text{ lb})\cos 36.870° = +4200.0 \text{ lb}$

$$F_y = +4200 \text{ lb} \blacktriangleleft$$

$F_z = -F_H \cos 50° = -3150\cos 50° = -2024.8 \text{ lb}$ $\quad F_z = -2025 \text{ lb} \blacktriangleleft$

(b) $\cos\theta_x = \dfrac{F_x}{F} = \dfrac{-2413.0 \text{ lb}}{5250 \text{ lb}}$ $\quad \theta_x = 117.4° \blacktriangleleft$

From above: $\theta_y = 36.870°$ $\quad \theta_y = 36.9° \blacktriangleleft$

$$\theta_z = \frac{F_z}{F} = \frac{-2024.8 \text{ lb}}{5250 \text{ lb}} \qquad \theta_z = 112.7° \blacktriangleleft$$

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PROBLEM 2.79

Determine the magnitude and direction of the force $\mathbf{F} = (240\text{ N})\mathbf{i} - (270\text{ N})\mathbf{j} + (680\text{ N})\mathbf{k}$.

SOLUTION

$$F = \sqrt{F_x^2 + F_y^2 + F_z^2}$$

$$F = \sqrt{(240\text{ N})^2 + (-270\text{ N})^2 + (-680\text{ N})^2} \qquad F = 770\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{F_x}{F} = \frac{240\text{ N}}{770\text{ N}} \qquad \theta_x = 71.8° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{-270\text{ N}}{770\text{ N}} \qquad \theta_y = 110.5° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_z}{F} = \frac{680\text{ N}}{770\text{ N}} \qquad \theta_z = 28.0° \blacktriangleleft$$

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PROBLEM 2.80

Determine the magnitude and direction of the force $\mathbf{F} = (320\text{ N})\mathbf{i} + (400\text{ N})\mathbf{j} - (250\text{ N})\mathbf{k}$.

SOLUTION

$$F = \sqrt{F_x^2 + F_y^2 + F_z^2}$$

$$F = \sqrt{(320\text{ N})^2 + (400\text{ N})^2 + (-250\text{ N})^2} \qquad F = 570\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{F_x}{F} = \frac{320\text{ N}}{570\text{ N}} \qquad \theta_x = 55.8° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{400\text{ N}}{570\text{ N}} \qquad \theta_y = 45.4° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_z}{F} = \frac{-250\text{ N}}{570\text{ N}} \qquad \theta_z = 116.0° \blacktriangleleft$$

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PROBLEM 2.81

A force acts at the origin of a coordinate system in a direction defined by the angles $\theta_x = 69.3°$ and $\theta_z = 57.9°$. Knowing that the y component of the force is –174.0 lb, determine (*a*) the angle θ_y, (*b*) the other components and the magnitude of the force.

SOLUTION

$$\cos^2\theta_x + \cos^2\theta_y + \cos^2\theta_z = 1$$

$$\cos^2(69.3°) + \cos^2\theta_y + \cos^2(57.9°) = 1$$

$$\cos\theta_y = \pm 0.7699$$

(*a*) Since $F_y < 0$, we choose $\cos\theta_y = -0.7699$ $\quad \therefore \quad \theta_y = 140.3°$ ◀

(*b*)
$$F_y = F\cos\theta_y$$

$$-174.0 \text{ lb} = F(-0.7699)$$

$$F = 226.0 \text{ lb} \qquad F = 226 \text{ lb} \blacktriangleleft$$

$$F_x = F\cos\theta_x = (226.0 \text{ lb})\cos 69.3° \qquad F_x = 79.9 \text{ lb} \blacktriangleleft$$

$$F_z = F\cos\theta_z = (226.0 \text{ lb})\cos 57.9° \qquad F_z = 120.1 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.82

A force acts at the origin of a coordinate system in a direction defined by the angles $\theta_x = 70.9°$ and $\theta_y = 144.9°$. Knowing that the z component of the force is -52.0 lb, determine (*a*) the angle θ_z, (*b*) the other components and the magnitude of the force.

SOLUTION

$$\cos^2\theta_x + \cos^2\theta_y + \cos^2\theta_z = 1$$

$$\cos^2 70.9^\circ + \cos^2 144.9° + \cos^2\theta_z ° = 1$$

$$\cos\theta_z = \pm 0.47282$$

(*a*) Since $F_z < 0$, we choose $\cos\theta_z = -0.47282$ $\quad \therefore \quad \theta_z = 118.2°$ ◀

(*b*)

$$F_z = F\cos\theta_z$$

$$-52.0\ lb = F(-0.47282)$$

$$F = 110.0 \text{ lb} \qquad F = 110.0 \text{ lb} \blacktriangleleft$$

$$F_x = F\cos\theta_x = (110.0 \text{ lb})\cos 70.9° \qquad F_x = 36.0 \text{ lb} \blacktriangleleft$$

$$F_y = F\cos\theta_y = (110.0 \text{ lb})\cos 144.9° \qquad F_y = -90.0 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.83

A force **F** of magnitude 210 N acts at the origin of a coordinate system. Knowing that F_x = 80 N, $\theta_z = 151.2°$, and $F_y < 0$, determine (*a*) the components F_y and F_z, (*b*) the angles θ_x and θ_y.

SOLUTION

(*a*)
$$F_z = F\cos\theta_z = (210\text{ N})\cos 151.2°$$
$$= -184.024\text{ N} \qquad F_z = -184.0\text{ N} \blacktriangleleft$$

Then:
$$F^2 = F_x^2 + F_y^2 + F_z^2$$

So:
$$(210\text{ N})^2 = (80\text{ N})^2 + (F_y)^2 + (184.024\text{ N})^2$$

Hence:
$$F_y = -\sqrt{(210\text{ N})^2 - (80\text{ N})^2 - (184.024\text{ N})^2}$$
$$= -61.929\text{ N} \qquad F_y = -62.0\text{ lb} \blacktriangleleft$$

(*b*)
$$\cos\theta_x = \frac{F_x}{F} = \frac{80\text{ N}}{210\text{ N}} = 0.38095 \qquad \theta_x = 67.6° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{61.929\text{ N}}{210\text{ N}} = -0.29490$$
$$\theta_y = 107.2° \blacktriangleleft$$

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PROBLEM 2.84

A force **F** of magnitude 1200 N acts at the origin of a coordinate system. Knowing that $\theta_x = 65°$, $\theta_y = 40°$, and $F_z > 0$, determine (*a*) the components of the force, (*b*) the angle θ_z.

SOLUTION

$$\cos^2\theta_x + \cos^2\theta_y + \cos^2\theta_z = 1$$

$$\cos^2 65^\circ + \cos^2 40° + \cos^2\theta_z° = 1$$

$$\cos\theta_z = \pm 0.48432$$

(*b*) Since $F_z > 0$, we choose $\cos\theta_z = 0.48432$, or $\theta_z = 61.032^\circ$ $\therefore$ $\theta_z = 61.0°$ ◀

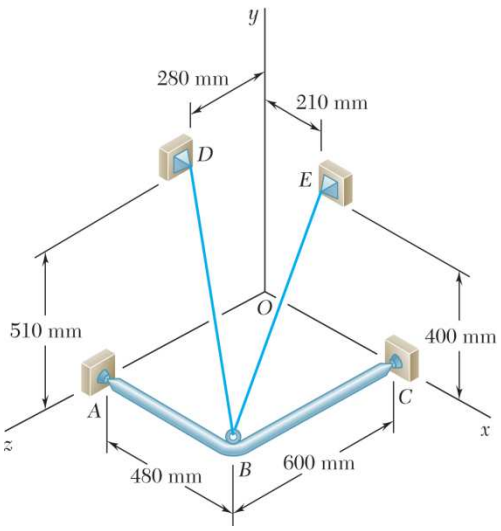
(*a*) $F = 1200$ N

$$F_x = F\cos\theta_x = (1200\text{ N})\cos 65^\circ \qquad F_x = 507\text{ N} \blacktriangleleft$$

$$F_y = F\cos\theta_y = (1200\text{ N})\cos 40° \qquad F_y = 919\text{ N} \blacktriangleleft$$

$$F_z = F\cos\theta_z = (1200\text{ N})\cos 61.032° \qquad F_z = 582\text{ N} \blacktriangleleft$$

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PROBLEM 2.85

A frame *ABC* is supported in part by cable *DBE* that passes through a frictionless ring at *B*. Knowing that the tension in the cable is 385 N, determine the components of the force exerted by the cable on the support at *D*.

SOLUTION

$$\overrightarrow{DB} = (480\text{ mm})\mathbf{i} - (510\text{ mm})\mathbf{j} + (320\text{ mm})\mathbf{k}$$

$$DB = \sqrt{(480\text{ mm})^2 + (510\text{ mm}^2) + (320\text{ mm})^2}$$

$$= 770\text{ mm}$$

$$\mathbf{F} = F\boldsymbol{\lambda}_{DB}$$

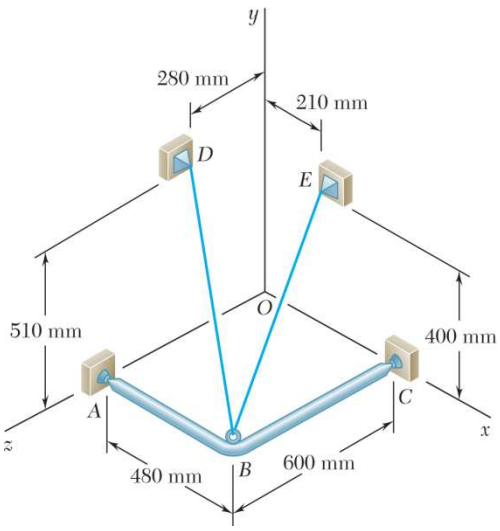
$$= F\frac{\overrightarrow{DB}}{DB}$$

$$= \frac{385\text{ N}}{770\text{ mm}}[(480\text{ mm})\mathbf{i} - (510\text{ mm})\mathbf{j} + (320\text{ mm})\mathbf{k}]$$

$$= (240\text{ N})\mathbf{i} - (255\text{ N})\mathbf{j} + (160\text{ N})\mathbf{k}$$

$$F_x = +240\text{ N}, \quad F_y = -255\text{ N}, \quad F_z = +160.0\text{ N} \blacktriangleleft$$

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PROBLEM 2.86

For the frame and cable of Problem 2.85, determine the components of the force exerted by the cable on the support at *E*.

PROBLEM 2.85 A frame *ABC* is supported in part by cable *DBE* that passes through a frictionless ring at *B*. Knowing that the tension in the cable is 385 N, determine the components of the force exerted by the cable on the support at *D*.

SOLUTION

$$\overrightarrow{EB} = (270 \text{ mm})\mathbf{i} - (400 \text{ mm})\mathbf{j} + (600 \text{ mm})\mathbf{k}$$

$$EB = \sqrt{(270 \text{ mm})^2 + (400 \text{ mm})^2 + (600 \text{ mm})^2}$$

$$= 770 \text{ mm}$$

$$\mathbf{F} = F\boldsymbol{\lambda}_{EB}$$

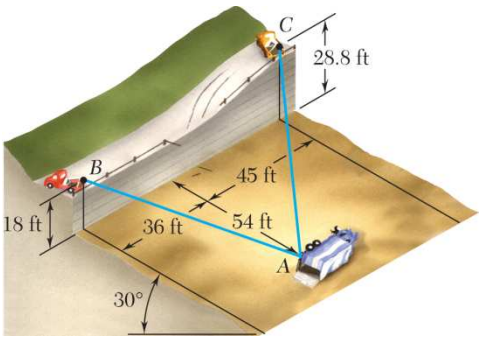
$$= F\frac{\overrightarrow{EB}}{EB}$$

$$= \frac{385 \text{ N}}{770 \text{ mm}}[(270 \text{ mm})\mathbf{i} - (400 \text{ mm})\mathbf{j} + (600 \text{ mm})\mathbf{k}]$$

$$\mathbf{F} = (135 \text{ N})\mathbf{i} - (200 \text{ N})\mathbf{j} + (300 \text{ N})\mathbf{k}$$

$$F_x = +135.0 \text{ N}, \quad F_y = -200 \text{ N}, \quad F_z = +300 \text{ N} \blacktriangleleft$$

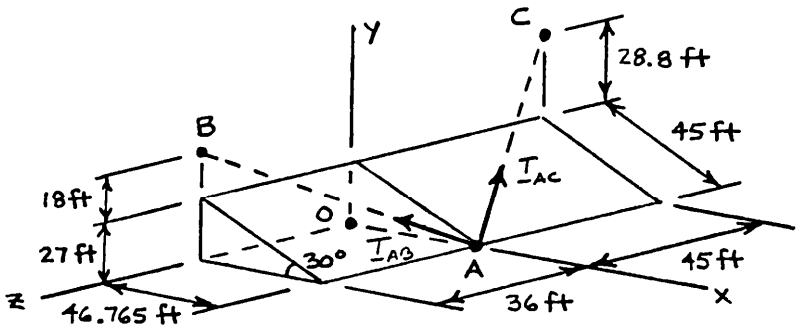
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PROBLEM 2.87

In order to move a wrecked truck, two cables are attached at A and pulled by winches B and C as shown. Knowing that the tension in cable AB is 2 kips, determine the components of the force exerted at A by the cable.

SOLUTION



$AB = 74.216$ ft $AC = 85.590$ ft

Cable AB:

$$\boldsymbol{\lambda}_{AB} = \frac{\overrightarrow{AB}}{AB} = \frac{(-46.765\text{ ft})\mathbf{i} + (45\text{ ft})\mathbf{j} + (36\text{ ft})\mathbf{k}}{74.216\text{ ft}}$$

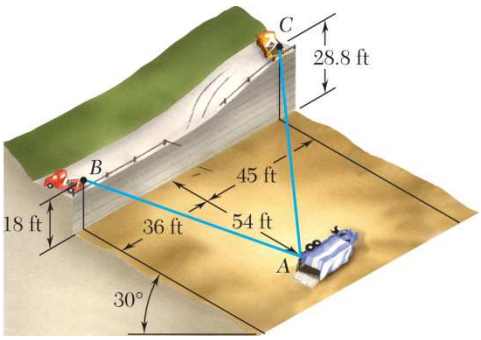
$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = \frac{-46.765\mathbf{i} + 45\mathbf{j} + 36\mathbf{k}}{74.216}$$

$$(T_{AB})_x = -1.260\text{ kips} \blacktriangleleft$$

$$(T_{AB})_y = +1.213\text{ kips} \blacktriangleleft$$

$$(T_{AB})_z = +0.970\text{ kips} \blacktriangleleft$$

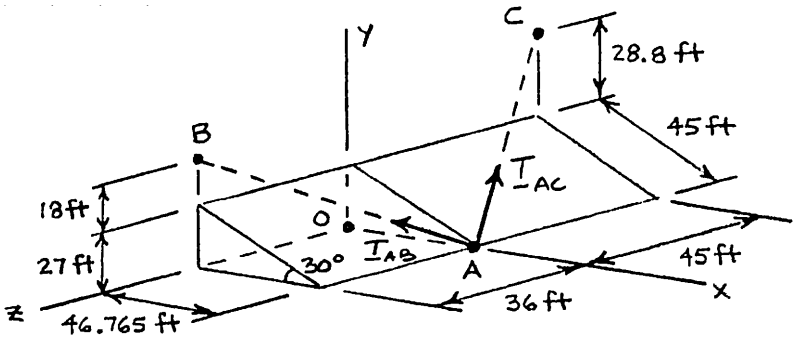
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PROBLEM 2.88

In order to move a wrecked truck, two cables are attached at A and pulled by winches B and C as shown. Knowing that the tension in cable AC is 1.5 kips, determine the components of the force exerted at A by the cable.

SOLUTION



$\underline{AB} = 74.216$ ft $\underline{AC} = 85.590$ ft

Cable AB:

$$\boldsymbol{\lambda}_{AC} = \frac{\overrightarrow{AC}}{AC} = \frac{(-46.765\text{ ft})\mathbf{i} + (55.8\text{ ft})\mathbf{j} + (-45\text{ ft})\mathbf{k}}{85.590\text{ ft}}$$

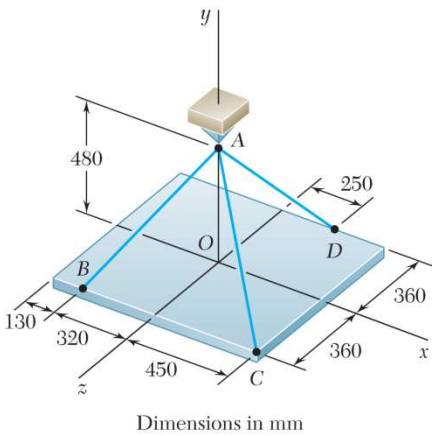
$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = (1.5\text{ kips})\frac{-46.765\mathbf{i} + 55.8\mathbf{j} - 45\mathbf{k}}{85.590}$$

$$(T_{AC})_x = -0.820\text{ kips} \blacktriangleleft$$

$$(T_{AC})_y = +0.978\text{ kips} \blacktriangleleft$$

$$(T_{AC})_z = -0.789\text{ kips} \blacktriangleleft$$

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Dimensions in mm

PROBLEM 2.89

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable AB is 408 N, determine the components of the force exerted on the plate at B.

SOLUTION

We have:

$$\overrightarrow{BA} = +(320 \text{ mm})\mathbf{i} + (480 \text{ mm})\mathbf{j} - (360 \text{ mm})\mathbf{k} \qquad BA = 680 \text{ mm}$$

Thus:

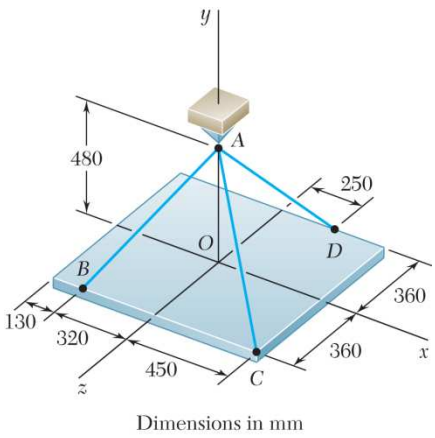
$$\mathrm{F}_B = T_{BA}\boldsymbol{\lambda}_{BA} = T_{BA}\frac{\overrightarrow{BA}}{BA} = T_{BA}\left(\frac{8}{17}\mathbf{i} + \frac{12}{17}\mathbf{j} - \frac{9}{17}\mathbf{k}\right)$$

$$\left(\frac{8}{17}T_{BA}\right)\mathbf{i} + \left(\frac{12}{17}T_{BA}\right)\mathbf{j} - \left(\frac{9}{17}T_{BA}\right)\mathbf{k} = 0$$

Setting $T_{BA} = 408$ N yields,

$$F_x = +192.0 \text{ N}, \quad F_y = +288 \text{ N}, \quad F_z = -216 \text{ N} \blacktriangleleft$$

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Dimensions in mm

PROBLEM 2.90

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable *AD* is 429 N, determine the components of the force exerted on the plate at *D*.

SOLUTION

We have:

$$\overrightarrow{DA} = -(250\text{ mm})\mathbf{i} + (480\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad DA = 650\text{ mm}$$

Thus:

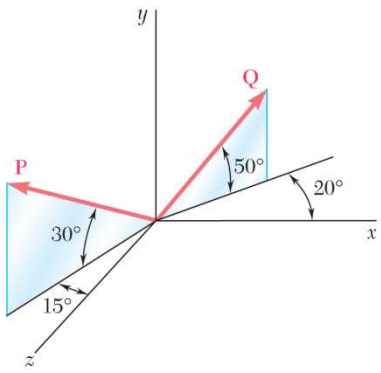
$$\mathrm{F}_D = T_{DA}\boldsymbol{\lambda}_{DA} = T_{DA}\frac{\overrightarrow{DA}}{DA} = T_{DA}\left(-\frac{5}{13}\mathbf{i} + \frac{48}{65}\mathbf{j} + \frac{36}{65}\mathbf{k}\right)$$

$$-\left(\frac{5}{13}T_{DA}\right)\mathbf{i} + \left(\frac{48}{65}T_{DA}\right)\mathbf{j} + \left(\frac{36}{65}T_{DA}\right)\mathbf{k} = 0$$

Setting $T_{DA} = 429\text{ N}$ yields,

$$F_x = -165.0\text{ N}, \quad F_y = +317\text{ N}, \quad F_z = +238\text{ N} \blacktriangleleft$$

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PROBLEM 2.91

Find the magnitude and direction of the resultant of the two forces shown knowing that $P = 300$ N and $Q = 400$ N.

SOLUTION

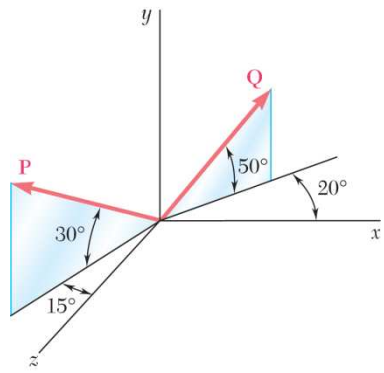
$$\mathbf{P} = (300\text{ N})[-\cos 30^\circ \sin 15^\circ \mathbf{i} + \sin 30^\circ \mathbf{j} + \cos 30^\circ \cos 15^\circ \mathbf{k}]$$
$$= -(67.243\text{ N})\mathbf{i} + (150\text{ N})\mathbf{j} + (250.95\text{ N})\mathbf{k}$$
$$\mathbf{Q} = (400\text{ N})[\cos 50^\circ \cos 20^\circ \mathbf{i} + \sin 50^\circ \mathbf{j} - \cos 50^\circ \sin 20^\circ \mathbf{k}]$$
$$= (400\text{ N})[0.60402\mathbf{i} + 0.76604\mathbf{j} - 0.21985]$$
$$= (241.61\text{ N})\mathbf{i} + (306.42\text{ N})\mathbf{j} - (87.939\text{ N})\mathbf{k}$$
$$\mathbf{R} = \mathbf{P} + \mathbf{Q}$$
$$= (174.367\text{ N})\mathbf{i} + (456.42\text{ N})\mathbf{j} + (163.011\text{ N})\mathbf{k}$$
$$R = \sqrt{(174.367\text{ N})^2 + (456.42\text{ N})^2 + (163.011\text{ N})^2}$$
$$= 515.07\text{ N} \qquad R = 515\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{R_x}{R} = \frac{174.367\text{ N}}{515.07\text{ N}} = 0.33853 \qquad \theta_x = 70.2^\circ \blacktriangleleft$$

$$\cos\theta_y = \frac{R_y}{R} = \frac{456.42\text{ N}}{515.07\text{ N}} = 0.88613 \qquad \theta_y = 27.6^\circ \blacktriangleleft$$

$$\cos\theta_z = \frac{R_z}{R} = \frac{163.011\text{ N}}{515.07\text{ N}} = 0.31648 \qquad \theta_z = 71.5^\circ \blacktriangleleft$$

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PROBLEM 2.92

Find the magnitude and direction of the resultant of the two forces shown knowing that $P = 400$ N and $Q = 300$ N.

SOLUTION

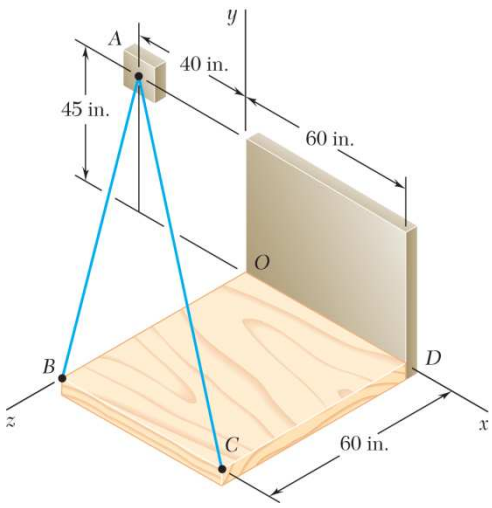
$$\mathbf{P} = (400\text{ N})[-\cos 30^\circ \sin 15^\circ \mathbf{i} + \sin 30^\circ \mathbf{j} + \cos 30^\circ \cos 15^\circ \mathbf{k}]$$
$$= -(89.678\text{ N})\mathbf{i} + (200\text{ N})\mathbf{j} + (334.61\text{ N})\mathbf{k}$$
$$\mathbf{Q} = (300\text{ N})[\cos 50^\circ \cos 20^\circ \mathbf{i} + \sin 50^\circ \mathbf{j} - \cos 50^\circ \sin 20^\circ \mathbf{k}]$$
$$= (181.21\text{ N})\mathbf{i} + (229.81\text{ N})\mathbf{j} - (65.954\text{ N})\mathbf{k}$$
$$\mathbf{R} = \mathbf{P} + \mathbf{Q}$$
$$= (91.532\text{ N})\mathbf{i} + (429.81\text{ N})\mathbf{j} + (268.66\text{ N})\mathbf{k}$$
$$R = \sqrt{(91.532\text{ N})^2 + (429.81\text{ N})^2 + (268.66\text{ N})^2}$$
$$= 515.07\text{ N} \qquad R = 515\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{R_x}{R} = \frac{91.532\text{ N}}{515.07\text{ N}} = 0.177708 \qquad \theta_x = 79.8^\circ \blacktriangleleft$$

$$\cos\theta_y = \frac{R_y}{R} = \frac{429.81\text{ N}}{515.07\text{ N}} = 0.83447 \qquad \theta_y = 33.4^\circ \blacktriangleleft$$

$$\cos\theta_z = \frac{R_z}{R} = \frac{268.66\text{ N}}{515.07\text{ N}} = 0.52160 \qquad \theta_z = 58.6^\circ \blacktriangleleft$$

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PROBLEM 2.93

Knowing that the tension is 425 lb in cable AB and 510 lb in cable AC, determine the magnitude and direction of the resultant of the forces exerted at A by the two cables.

SOLUTION

$$\overrightarrow{AB} = (40 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}$$

$$AB = \sqrt{(40 \text{ in.})^2 + (45 \text{ in.})^2 + (60 \text{ in.})^2} = 85 \text{ in.}$$

$$\overrightarrow{AC} = (100 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}$$

$$AC = \sqrt{(100 \text{ in.})^2 + (45 \text{ in.})^2 + (60 \text{ in.})^2} = 125 \text{ in.}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (425 \text{ lb})\left[\frac{(40 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}}{85 \text{ in.}}\right]$$

$$\mathbf{T}_{AB} = (200 \text{ lb})\mathbf{i} - (225 \text{ lb})\mathbf{j} + (300 \text{ lb})\mathbf{k}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = (510 \text{ lb})\left[\frac{(100 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}}{125 \text{ in.}}\right]$$

$$\mathbf{T}_{AC} = (408 \text{ lb})\mathbf{i} - (183.6 \text{ lb})\mathbf{j} + (244.8 \text{ lb})\mathbf{k}$$

$$\mathbf{R} = \mathbf{T}_{AB} + \mathbf{T}_{AC} = (608)\mathbf{i} - (408.6 \text{ lb})\mathbf{j} + (544.8 \text{ lb})\mathbf{k}$$

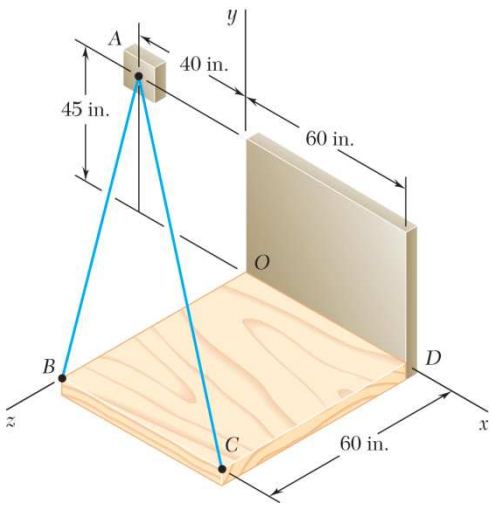
Then: $R = 912.92 \text{ lb}$ $\qquad R = 913 \text{ lb}$ ◀

and $\cos\theta_x = \dfrac{608 \text{ lb}}{912.92 \text{ lb}} = 0.66599$ $\qquad \theta_x = 48.2°$ ◀

$\cos\theta_y = \dfrac{408.6 \text{ lb}}{912.92 \text{ lb}} = -0.44757$ $\qquad \theta_y = 116.6°$ ◀

$\cos\theta_z = \dfrac{544.8 \text{ lb}}{912.92 \text{ lb}} = 0.59677$ $\qquad \theta_z = 53.4°$ ◀

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PROBLEM 2.94

Knowing that the tension is 510 lb in cable AB and 425 lb in cable AC, determine the magnitude and direction of the resultant of the forces exerted at A by the two cables.

SOLUTION

$$\overrightarrow{AB} = (40 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}$$

$$AB = \sqrt{(40 \text{ in.})^2 + (45 \text{ in.})^2 + (60 \text{ in.})^2} = 85 \text{ in.}$$

$$\overrightarrow{AC} = (100 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}$$

$$AC = \sqrt{(100 \text{ in.})^2 + (45 \text{ in.})^2 + (60 \text{ in.})^2} = 125 \text{ in.}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (510 \text{ lb})\left[\frac{(40 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}}{85 \text{ in.}}\right]$$

$$\mathbf{T}_{AB} = (240 \text{ lb})\mathbf{i} - (270 \text{ lb})\mathbf{j} + (360 \text{ lb})\mathbf{k}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = (425 \text{ lb})\left[\frac{(100 \text{ in.})\mathbf{i} - (45 \text{ in.})\mathbf{j} + (60 \text{ in.})\mathbf{k}}{125 \text{ in.}}\right]$$

$$\mathbf{T}_{AC} = (340 \text{ lb})\mathbf{i} - (153 \text{ lb})\mathbf{j} + (204 \text{ lb})\mathbf{k}$$

$$\mathbf{R} = \mathbf{T}_{AB} + \mathbf{T}_{AC} = (580 \text{ lb})\mathbf{i} - (423 \text{ lb})\mathbf{j} + (564 \text{ lb})\mathbf{k}$$

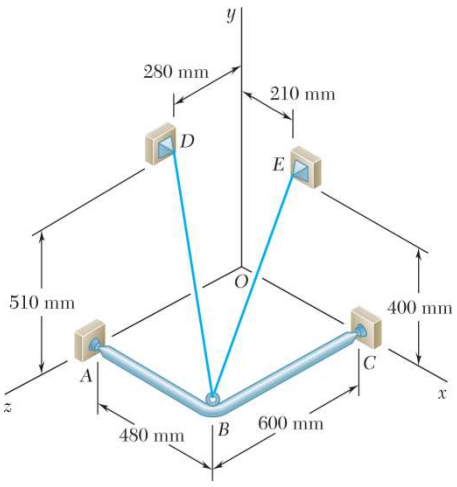
Then: $R = 912.92 \text{ lb}$ $\qquad R = 913 \text{ lb}$ ◀

and $\cos\theta_x = \dfrac{580 \text{ lb}}{912.92 \text{ lb}} = 0.63532$ $\qquad \theta_x = 50.6°$ ◀

$\cos\theta_y = \dfrac{-423 \text{ lb}}{912.92 \text{ lb}} = -0.46335$ $\qquad \theta_y = 117.6°$ ◀

$\cos\theta_z = \dfrac{564 \text{ lb}}{912.92 \text{ lb}} = 0.61780$ $\qquad \theta_z = 51.8°$ ◀

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PROBLEM 2.95

For the frame of Problem 2.85, determine the magnitude and direction of the resultant of the forces exerted by the cable at *B* knowing that the tension in the cable is 385 N.

PROBLEM 2.85 A frame *ABC* is supported in part by cable *DBE* that passes through a frictionless ring at *B*. Knowing that the tension in the cable is 385 N, determine the components of the force exerted by the cable on the support at *D*.

SOLUTION

$$\overrightarrow{BD} = -(480\text{ mm})\mathbf{i} + (510\text{ mm})\mathbf{j} - (320\text{ mm})\mathbf{k}$$

$$BD = \sqrt{(480\text{ mm})^2 + (510\text{ mm})^2 + (320\text{ mm})^2} = 770\text{ mm}$$

$$\mathbf{F}_{BD} = T_{BD}\boldsymbol{\lambda}_{BD} = T_{BD}\frac{\overrightarrow{BD}}{BD}$$

$$= \frac{(385\text{ N})}{(770\text{ mm})}[-(480\text{ mm})\mathbf{i} + (510\text{ mm})\mathbf{j} - (320\text{ mm})\mathbf{k}]$$

$$= -(240\text{ N})\mathbf{i} + (255\text{ N})\mathbf{j} - (160\text{ N})\mathbf{k}$$

$$\overrightarrow{BE} = -(270\text{ mm})\mathbf{i} + (400\text{ mm})\mathbf{j} - (600\text{ mm})\mathbf{k}$$

$$BE = \sqrt{(270\text{ mm})^2 + (400\text{ mm})^2 + (600\text{ mm})^2} = 770\text{ mm}$$

$$\mathbf{F}_{BE} = T_{BE}\boldsymbol{\lambda}_{BE} = T_{BE}\frac{\overrightarrow{BE}}{BE}$$

$$= \frac{(385\text{ N})}{(770\text{ mm})}[-(270\text{ mm})\mathbf{i} + (400\text{ mm})\mathbf{j} - (600\text{ mm})\mathbf{k}]$$

$$= -(135\text{ N})\mathbf{i} + (200\text{ N})\mathbf{j} - (300\text{ N})\mathbf{k}$$

$$\mathbf{R} = \mathbf{F}_{BD} + \mathbf{F}_{BE} = -(375\text{ N})\mathbf{i} + (455\text{ N})\mathbf{j} - (460\text{ N})\mathbf{k}$$

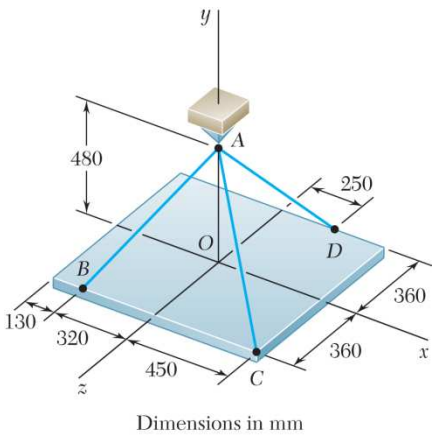
$$R = \sqrt{(375\text{ N})^2 + (455\text{ N})^2 + (460\text{ N})^2} = 747.83\text{ N} \qquad R = 748\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{-375\text{ N}}{747.83\text{ N}} \qquad \theta_x = 120.1° \blacktriangleleft$$

$$\cos\theta_y = \frac{455\text{ N}}{747.83\text{ N}} \qquad \theta_y = 52.5° \blacktriangleleft$$

$$\cos\theta_z = \frac{-460\text{ N}}{747.83\text{ N}} \qquad \theta_z = 128.0° \blacktriangleleft$$

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Dimensions in mm

PROBLEM 2.96

For the plate of Prob. 2.89, determine the tensions in cables *AB* and *AD* knowing that the tension in cable *AC* is 54 N and that the resultant of the forces exerted by the three cables at *A* must be vertical.

SOLUTION

We have:

$$\overrightarrow{AB} = -(320\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad AB = 680\text{ mm}$$
$$\overrightarrow{AC} = (450\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad AC = 750\text{ mm}$$
$$\overrightarrow{AD} = (250\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} - (360\text{ mm})\mathbf{k} \qquad AD = 650\text{ mm}$$

Thus:

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = \frac{T_{AB}}{680}(-320\mathbf{i} - 480\mathbf{j} + 360\mathbf{k})$$
$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = \frac{54}{750}(450\mathbf{i} - 480\mathbf{j} + 360\mathbf{k})$$
$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = \frac{T_{AD}}{650}(250\mathbf{i} - 480\mathbf{j} - 360\mathbf{k})$$

Substituting into the Eq. $\mathbf{R} = \Sigma\mathbf{F}$ and factoring **i**, **j**, **k**:

$$\mathbf{R} = \left(-\frac{320}{680}T_{AB} + 32.40 + \frac{250}{650}T_{AD}\right)\mathbf{i}$$
$$+\left(-\frac{480}{680}T_{AB} - 34.560 - \frac{480}{650}T_{AD}\right)\mathbf{j}$$
$$+\left(\frac{360}{680}T_{AB} + 25.920 - \frac{360}{650}T_{AD}\right)\mathbf{k}$$

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PROBLEM 2.96 (Continued)

Since **R** is vertical, the coefficients of **i** and **k** are zero:

$$\mathbf{i}: \qquad -\frac{320}{680}T_{AB} + 32.40 + \frac{250}{650}T_{AD} = 0 \tag{1}$$

$$\mathbf{k}: \qquad \frac{360}{680}T_{AB} + 25.920 - \frac{360}{650}T_{AD} = 0 \tag{2}$$

Multiply (1) by 3.6 and (2) by 2.5 then add:

$$-\frac{252}{680}T_{AB} + 181.440 = 0$$

$$T_{AB} = 489.60 \text{ N}$$

$$T_{AB} = 490 \text{ N} \blacktriangleleft$$

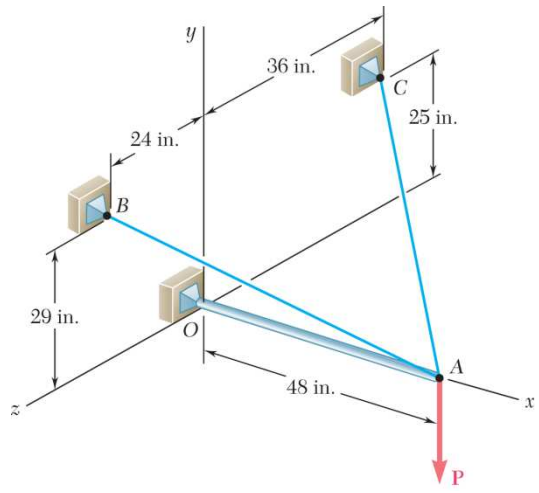
Substitute into (2) and solve for T_{AD}:

$$\frac{360}{680}(489.60 \text{ N}) + 25.920 - \frac{360}{650}T_{AD} = 0$$

$$T_{AD} = 514.80 \text{ N}$$

$$T_{AD} = 515 \text{ N} \blacktriangleleft$$

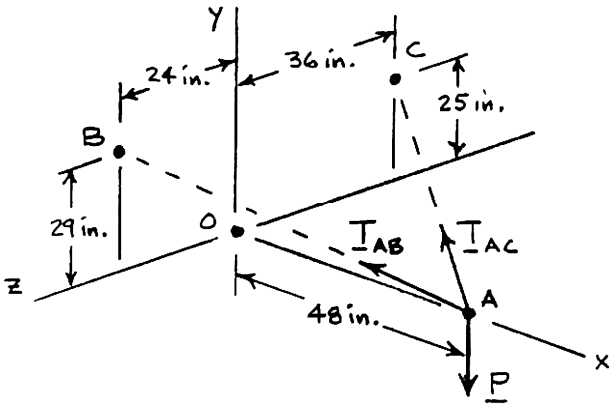
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PROBLEM 2.97

The boom OA carries a load **P** and is supported by two cables as shown. Knowing that the tension in cable AB is 183 lb and that the resultant of the load **P** and of the forces exerted at A by the two cables must be directed along OA, determine the tension in cable AC.

SOLUTION



Cable AB:

$$T_{AB} = 183 \text{ lb}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (183 \text{ lb})\frac{(-48 \text{ in.})\mathbf{i} + (29 \text{ in.})\mathbf{j} + (24 \text{ in.})\mathbf{k}}{61 \text{ in.}}$$

$$\mathbf{T}_{AB} = -(144 \text{ lb})\mathbf{i} + (87 \text{ lb})\mathbf{j} + (72 \text{ lb})\mathbf{k}$$

Cable AC:

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\frac{(-48 \text{ in.})\mathbf{i} + (25 \text{ in.})\mathbf{j} + (-36 \text{ in.})\mathbf{k}}{65 \text{ in.}}$$

$$\mathbf{T}_{AC} = -\frac{48}{65}T_{AC}\mathbf{i} + \frac{25}{65}T_{AC}\mathbf{j} - \frac{36}{65}T_{AC}\mathbf{k}$$

Load P:

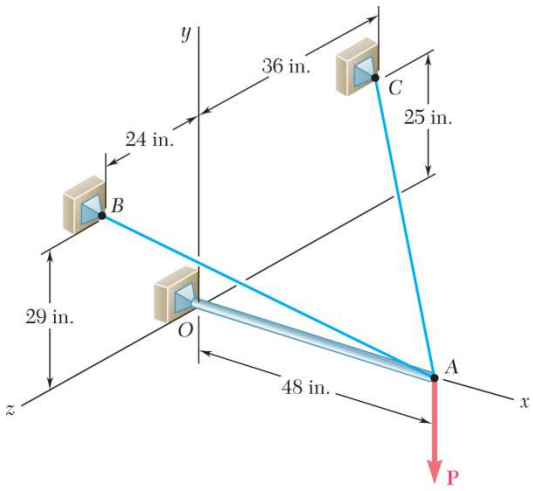
$$\mathbf{P} = P\,\mathbf{j}$$

For resultant to be directed along OA, i.e., x-axis

$$R_z = 0: \quad \Sigma F_z = (72 \text{ lb}) - \frac{36}{65}T'_{AC} = 0$$

$$T_{AC} = 130.0 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.98

For the boom and loading of Problem. 2.97, determine the magnitude of the load **P**.

PROBLEM 2.97 The boom *OA* carries a load **P** and is supported by two cables as shown. Knowing that the tension in cable *AB* is 183 lb and that the resultant of the load **P** and of the forces exerted at *A* by the two cables must be directed along *OA*, determine the tension in cable *AC*.

SOLUTION

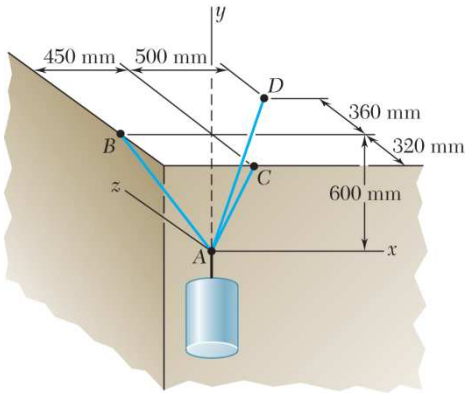
See Problem 2.97. Since resultant must be directed along *OA*, i.e., the *x*-axis, we write

$$R_y = 0: \quad \Sigma F_y = (87 \text{ lb}) + \frac{25}{65} T_{AC} - P = 0$$

$T_{AC} = 130.0 \text{ lb}$ from Problem 2.97.

Then $$(87 \text{ lb}) + \frac{25}{65}(130.0 \text{ lb}) - P = 0$$ $$P = 137.0 \text{ lb} \blacktriangleleft$$

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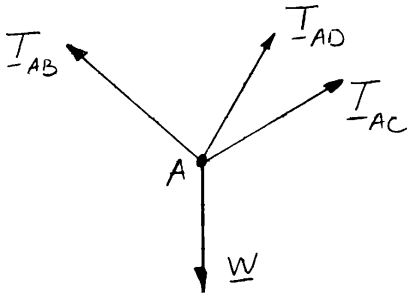


PROBLEM 2.99

A container is supported by three cables that are attached to a ceiling as shown. Determine the weight W of the container, knowing that the tension in cable AB is 6 kN.

SOLUTION

Free-Body Diagram at A:



The forces applied at A are: $\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD}$, and $\mathbf{W}$

where $\mathbf{W} = W\mathbf{j}$. To express the other forces in terms of the unit vectors $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$, we write

$$\overrightarrow{AB} = -(450 \text{ mm})\mathbf{i} + (600 \text{ mm})\mathbf{j} \qquad AB = 750 \text{ mm}$$

$$\overrightarrow{AC} = +(600 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k} \qquad AC = 680 \text{ mm}$$

$$\overrightarrow{AD} = +(500 \text{ mm})\mathbf{i} + (600 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k} \qquad AD = 860 \text{ mm}$$

and

$$\mathbf{T}_{AB} = \boldsymbol{\lambda}_{AB} T_{AB} = T_{AB} \frac{\overrightarrow{AB}}{AB} = T_{AB} \frac{(-450 \text{ mm})\mathbf{i} + (600 \text{ mm})\mathbf{j}}{750 \text{ mm}}$$

$$= \left(-\frac{45}{75}\mathbf{i} + \frac{60}{75}\mathbf{j} \right) T_{AB}$$

$$\mathbf{T}_{AC} = \boldsymbol{\lambda}_{AC} T_{AC} = T_{AC} \frac{\overrightarrow{AC}}{AC} = T_{AC} \frac{(600 \text{ mm})\mathbf{i} - (320 \text{ mm})\mathbf{j}}{680 \text{ mm}}$$

$$= \left(\frac{60}{68}\mathbf{j} - \frac{32}{68}\mathbf{k} \right) T_{AC}$$

$$\mathbf{T}_{AD} = \boldsymbol{\lambda}_{AD} T_{AD} = T_{AD} \frac{\overrightarrow{AD}}{AD} = T_{AD} \frac{(500 \text{ mm})\mathbf{i} + (600 \text{ mm})\mathbf{j} + (360 \text{ mm})\mathbf{k}}{860 \text{ mm}}$$

$$= \left(\frac{50}{86}\mathbf{i} + \frac{60}{86}\mathbf{j} + \frac{36}{86}\mathbf{k} \right) T_{AD}$$

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PROBLEM 2.99 (Continued)

Equilibrium condition: $\Sigma F = 0: \quad \therefore \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{W} = 0$

Substituting the expressions obtained for $\mathbf{T}_{AB}$, $\mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$; factoring **i**, **j**, and **k**; and equating each of the coefficients to zero gives the following equations:

From **i**: $$-\frac{45}{75}T_{AB} + \frac{50}{86}T_{AD} = 0 \qquad (1)$$

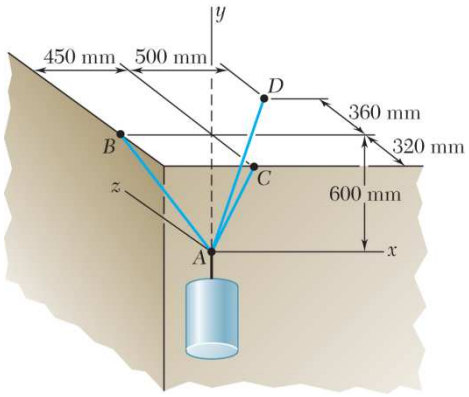
From **j**: $$\frac{60}{75}T_{AB} + \frac{60}{68}T_{AC} + \frac{60}{86}T_{AD} - W = 0 \qquad (2)$$

From **k**: $$-\frac{32}{68}T_{AC} + \frac{36}{86}T_{AD} = 0 \qquad (3)$$

Setting $T_{AB} = 6$ kN in (1) and (2), and solving the resulting set of equations gives

$$T_{AC} = 6.1920 \text{ kN}$$
$$T_{AC} = 5.5080 \text{ kN} \qquad W = 13.98 \text{ kN} \blacktriangleleft$$

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PROBLEM 2.100

A container is supported by three cables that are attached to a ceiling as shown. Determine the weight W of the container, knowing that the tension in cable AD is 4.3 kN.

SOLUTION

See Problem 2.99 for the figure and analysis leading to the following set of linear algebraic equations:

$$-\frac{45}{75}T_{AB}+\frac{50}{86}T_{AD}=0 \tag{1}$$

$$\frac{60}{75}T_{AB}+\frac{60}{68}T_{AC}+\frac{60}{86}T_{AD}-W=0 \tag{2}$$

$$-\frac{32}{68}T_{AC}+\frac{36}{86}T_{AD}=0 \tag{3}$$

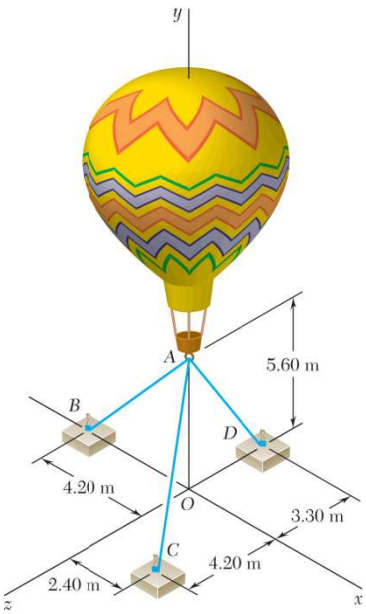
Setting $T_{AD}=4.3\text{ kN}$ into the above equations gives

$$T_{AB}=4.1667\text{ kN}$$

$$T_{AC}=3.8250\text{ kN}$$

$$W=9.71\text{ kN} \blacktriangleleft$$

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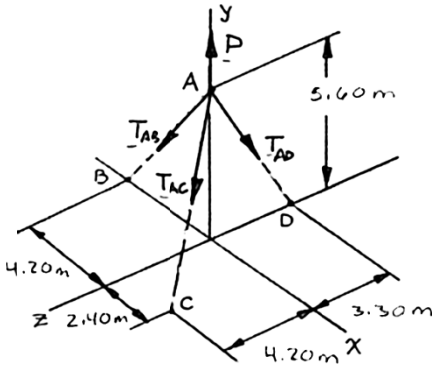


PROBLEM 2.101

Three cables are used to tether a balloon as shown. Determine the vertical force **P** exerted by the balloon at *A* knowing that the tension in cable *AD* is 481 N.

SOLUTION

FREE-BODY DIAGRAM AT *A*



The forces applied at *A* are: $\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD}$, and **P**

where $\mathbf{P} = P\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{AB} = -(4.20\text{ m})\mathbf{i} - (5.60\text{ m})\mathbf{j} \qquad AB = 7.00\text{ m}$$

$$\overrightarrow{AC} = (2.40\text{ m})\mathbf{i} - (5.60\text{ m})\mathbf{j} + (4.20\text{ m})\mathbf{k} \qquad AC = 7.40\text{ m}$$

$$\overrightarrow{AD} = -(5.60\text{ m})\mathbf{j} - (3.30\text{ m})\mathbf{k} \qquad AD = 6.50\text{ m}$$

and

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = (-0.6\mathbf{i} - 0.8\mathbf{j})T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = (0.32432\mathbf{i} - 0.75676\mathbf{j} + 0.56757\mathbf{k})T_{AC}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = (-0.86154\mathbf{j} - 0.50769\mathbf{k})T_{AD}$$

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PROBLEM 2.101 (Continued)

Equilibrium condition: $\Sigma F = 0$: $\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$

Substituting the expressions obtained for $\mathbf{T}_{AB}$, $\mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$ and factoring **i**, **j**, and **k**:

$$(-0.6T_{AB} + 0.32432T_{AC})\mathbf{i} + (-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P)\mathbf{j} + (0.56757T_{AC} - 0.50769T_{AD})\mathbf{k} = 0$$

Equating to zero the coefficients of **i**, **j**, **k**:

$$-0.6T_{AB} + 0.32432T_{AC} = 0 \tag{1}$$

$$-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P = 0 \tag{2}$$

$$0.56757T_{AC} - 0.50769T_{AD} = 0 \tag{3}$$

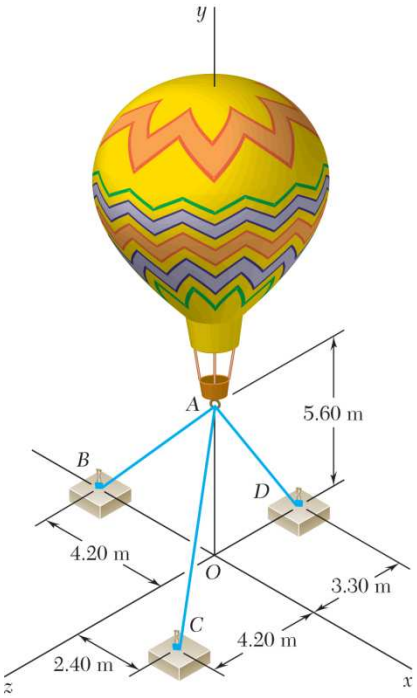
Setting $T_{AD} = 481$ N in (2) and (3), and solving the resulting set of equations gives

$$T_{AC} = 430.26 \text{ N}$$

$$T_{AD} = 232.57 \text{ N}$$

$$\mathbf{P} = 926 \text{ N} \uparrow \blacktriangleleft$$

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PROBLEM 2.102

Three cables are used to tether a balloon as shown. Knowing that the balloon exerts an 800-N vertical force at A, determine the tension in each cable.

SOLUTION

See Problem 2.101 for the figure and analysis leading to the linear algebraic Equations (1), (2), and (3).

$$-0.6T_{AB} + 0.32432T_{AC} = 0 \tag{1}$$

$$-0.8T_{AB} - 0.75676T_{AC} - 0.86154T_{AD} + P = 0 \tag{2}$$

$$0.56757T_{AC} - 0.50769T_{AD} = 0 \tag{3}$$

From Eq. (1): $T_{AB} = 0.54053T_{AC}$

From Eq. (3): $T_{AD} = 1.11795T_{AC}$

Substituting for T_{AB} and T_{AD} in terms of T_{AC} into Eq. (2) gives

$$-0.8(0.54053T_{AC}) - 0.75676T_{AC} - 0.86154(1.11795T_{AC}) + P = 0$$

$$2.1523T_{AC} = P; \quad P = 800 \text{ N}$$

$$T_{AC} = \frac{800 \text{ N}}{2.1523}$$

$$= 371.69 \text{ N}$$

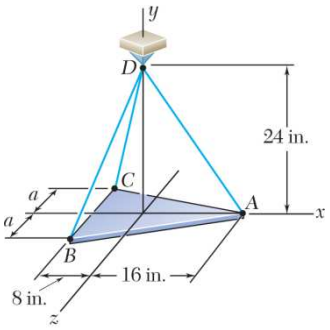
Substituting into expressions for T_{AB} and T_{AD} gives

$$T_{AB} = 0.54053(371.69 \text{ N})$$

$$T_{AD} = 1.11795(371.69 \text{ N})$$

$$T_{AB} = 201 \text{ N}, \quad T_{AC} = 372 \text{ N}, \quad T_{AD} = 416 \text{ N} \blacktriangleleft$$

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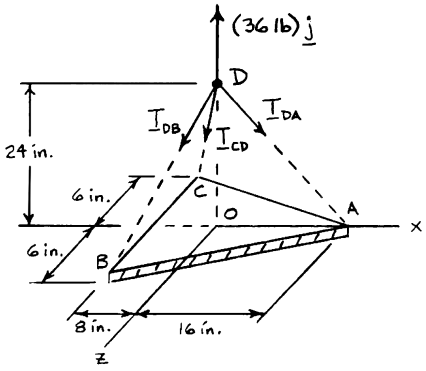
PROBLEM 2.103

A 36-lb triangular plate is supported by three wires as shown. Determine the tension in each wire, knowing that $a = 6$ in.

SOLUTION

By Symmetry $T_{DB} = T_{DC}$

Free-Body Diagram of Point *D*:



The forces applied at *D* are: $\mathbf{T}_{DB}, \mathbf{T}_{DC}, \mathbf{T}_{DA},$ and $\mathbf{P}$

where $\mathbf{P} = P\mathbf{j} = (36 \text{ lb})\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{DA} = (16 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} \qquad DA = 28.844 \text{ in.}$$

$$\overrightarrow{DB} = -(8 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} + (6 \text{ in.})\mathbf{k} \qquad DB = 26.0 \text{ in.}$$

$$\overrightarrow{DC} = -(8 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} - (6 \text{ in.})\mathbf{k} \qquad DC = 26.0 \text{ in.}$$

and

$$\mathbf{T}_{DA} = T_{DA}\boldsymbol{\lambda}_{DA} = T_{DA}\frac{\overrightarrow{DA}}{DA} = (0.55471\mathbf{i} - 0.83206\mathbf{j})T_{DA}$$

$$\mathbf{T}_{DB} = T_{DB}\boldsymbol{\lambda}_{DB} = T_{DB}\frac{\overrightarrow{DB}}{DB} = (-0.30769\mathbf{i} - 0.92308\mathbf{j} + 0.23077\mathbf{k})T_{DB}$$

$$\mathbf{T}_{DC} = T_{DC}\boldsymbol{\lambda}_{DC} = T_{DC}\frac{\overrightarrow{DC}}{DC} = (-0.30769\mathbf{i} - 0.92308\mathbf{j} - 0.23077\mathbf{k})T_{DC}$$

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PROBLEM 2.103 (Continued)

Equilibrium condition: $\Sigma F = 0$: $\mathbf{T}_{DA} + \mathbf{T}_{DB} + \mathbf{T}_{DC} + (36 \text{ lb})\mathbf{j} = 0$

Substituting the expressions obtained for $\mathbf{T}_{DA}$, $\mathbf{T}_{DB}$, and $\mathbf{T}_{DC}$ and factoring **i**, **j**, and **k**:

$$(0.55471T_{DA} - 0.30769T_{DB} - 0.30769T_{DC})\mathbf{i} + (-0.83206T_{DA} - 0.92308T_{DB} - 0.92308T_{DC} + 36 \text{ lb})\mathbf{j} + (0.23077T_{DB} - 0.23077T_{DC})\mathbf{k} = 0$$

Equating to zero the coefficients of **i**, **j**, **k**:

$$0.55471T_{DA} - 0.30769T_{DB} - 0.30769T_{DC} = 0 \quad (1)$$

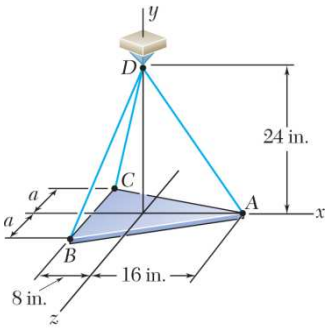
$$-0.83206T_{DA} - 0.92308T_{DB} - 0.92308T_{DC} + 36 \text{ lb} = 0 \quad (2)$$

$$0.23077T_{DB} - 0.23077T_{DC} = 0 \quad (3)$$

Equation (3) confirms that $T_{DB} = T_{DC}$. Solving simultaneously gives,

$$T_{DA} = 14.42 \text{ lb}; \quad T_{DB} = T_{DC} = 13.00 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.104

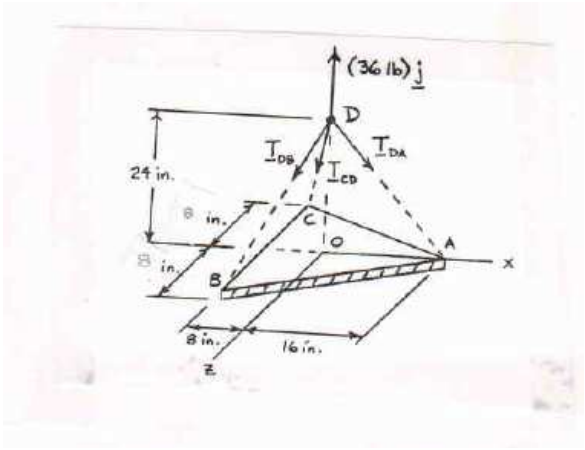
Solve Prob. 2.103, assuming that $a = 8$ in.

PROBLEM 2.103 A 36-lb triangular plate is supported by three wires as shown. Determine the tension in each wire, knowing that $a = 6$ in.

SOLUTION

By Symmetry $T_{DB} = T_{DC}$

Free-Body Diagram of Point *D*:



The forces applied at D are: $\mathbf{T}_{DB}, \mathbf{T}_{DC}, \mathbf{T}_{DA}$, and $\mathbf{P}$

where $\mathbf{P} = P\mathbf{j} = (36 \text{ lb})\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{DA} = (16 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} \qquad DA = 28.844 \text{ in.}$$

$$\overrightarrow{DB} = -(8 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} + (8 \text{ in.})\mathbf{k} \qquad DB = 26.533 \text{ in.}$$

$$\overrightarrow{DC} = -(8 \text{ in.})\mathbf{i} - (24 \text{ in.})\mathbf{j} - (8 \text{ in.})\mathbf{k} \qquad DC = 26.533 \text{ in.}$$

and

$$\mathbf{T}_{DA} = T_{DA}\boldsymbol{\lambda}_{DA} = T_{DA}\frac{\overrightarrow{DA}}{DA} = (0.55471\mathbf{i} - 0.83206\mathbf{j})T_{DA}$$

$$\mathbf{T}_{DB} = T_{DB}\boldsymbol{\lambda}_{DB} = T_{DB}\frac{\overrightarrow{DB}}{DB} = (-0.30151\mathbf{i} - 0.90453\mathbf{j} + 0.30151\mathbf{k})T_{DB}$$

$$\mathbf{T}_{DC} = T_{DC}\boldsymbol{\lambda}_{DC} = T_{DC}\frac{\overrightarrow{DC}}{DC} = (-0.30151\mathbf{i} - 0.90453\mathbf{j} - 0.30151\mathbf{k})T_{DC}$$

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PROBLEM 2.104 (Continued)

Equilibrium condition: $\Sigma F = 0$: $\mathbf{T}_{DA} + \mathbf{T}_{DB} + \mathbf{T}_{DC} + (36 \text{ lb})\mathbf{j} = 0$

Substituting the expressions obtained for $\mathbf{T}_{DA}$, $\mathbf{T}_{DB}$, and $\mathbf{T}_{DC}$ and factoring **i**, **j**, and **k**:

$$(0.55471T_{DA} - 0.30151T_{DB} - 0.30151T_{DC})\mathbf{i} + (-0.83206T_{DA} - 0.90453T_{DB} - 0.90453T_{DC} + 36 \text{ lb})\mathbf{j} + (0.30151T_{DB} - 0.30151T_{DC})\mathbf{k} = 0$$

Equating to zero the coefficients of **i**, **j**, **k**:

$$0.55471T_{DA} - 0.30151T_{DB} - 0.30151T_{DC} = 0 \quad (1)$$

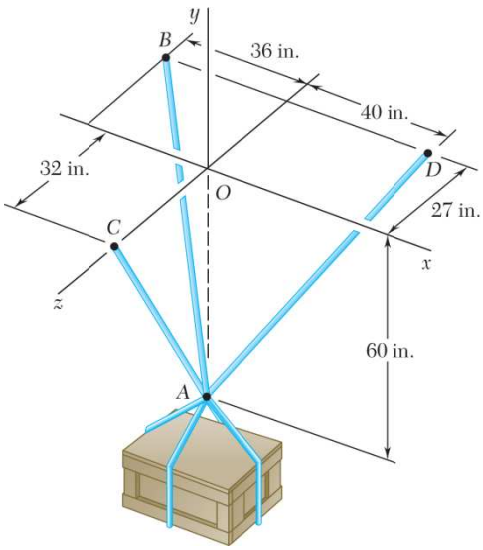
$$-0.83206T_{DA} - 0.90453T_{DB} - 0.90453T_{DC} + 36 \text{ lb} = 0 \quad (2)$$

$$0.30151T_{DB} - 0.30151T_{DC} = 0 \quad (3)$$

Equation (3) confirms that $T_{DB} = T_{DC}$. Solving simultaneously gives,

$$T_{DA} = 14.42 \text{ lb}; \quad T_{DB} = T_{DC} = 13.27 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.105

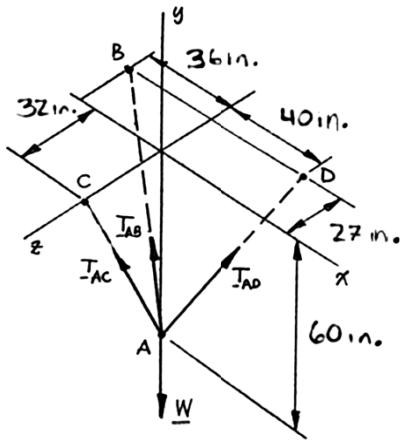
A crate is supported by three cables as shown. Determine the weight of the crate knowing that the tension in cable AC is 544 lb.

Solution The forces applied at A are:

$$\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD} \text{ and } \mathbf{W}$$

where $\mathbf{P} = P\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{AB} = -(36 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (27 \text{ in.})\mathbf{k}$$
$$AB = 75 \text{ in.}$$
$$\overrightarrow{AC} = (60 \text{ in.})\mathbf{j} + (32 \text{ in.})\mathbf{k}$$
$$AC = 68 \text{ in.}$$
$$\overrightarrow{AD} = (40 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (27 \text{ in.})\mathbf{k}$$
$$AD = 77 \text{ in.}$$



and

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$
$$= (-0.48\mathbf{i} + 0.8\mathbf{j} - 0.36\mathbf{k})T_{AB}$$
$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC}$$
$$= (0.88235\mathbf{j} + 0.47059\mathbf{k})T_{AC}$$
$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD}$$
$$= (0.51948\mathbf{i} + 0.77922\mathbf{j} - 0.35065\mathbf{k})T_{AD}$$

Equilibrium Condition with $\mathbf{W} = -W\mathbf{j}$

$$\Sigma F = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} - W\mathbf{j} = 0$$

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PROBLEM 2.105 (Continued)

Substituting the expressions obtained for $\mathbf{T}_{AB}$, $\mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$ and factoring **i**, **j**, and **k**:

$$(-0.48T_{AB} + 0.51948T_{AD})\mathbf{i} + (0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W)\mathbf{j}$$
$$+ (-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD})\mathbf{k} = 0$$

Equating to zero the coefficients of **i**, **j**, **k**:

$$-0.48T_{AB} + 0.51948T_{AD} = 0 \tag{1}$$

$$0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W = 0 \tag{2}$$

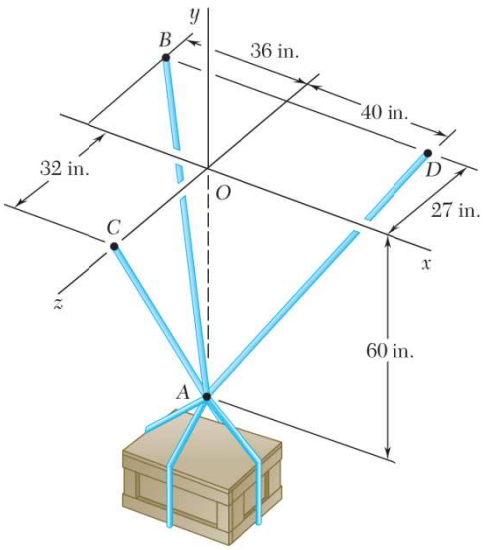
$$-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD} = 0 \tag{3}$$

Substituting $T_{AC} = 544$ lb in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms, gives:

$$T_{AB} = 374.27 \text{ lb}$$
$$T_{AD} = 345.82 \text{ lb} \qquad W = 1049 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.106

A 1600-lb crate is supported by three cables as shown. Determine the tension in each cable.

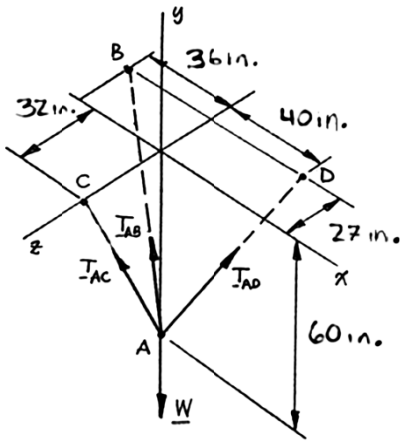
SOLUTION

The forces applied at A are:

$$\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{T}_{AD} \text{ and } \mathbf{W}$$

where $\mathbf{P} = P\mathbf{j}$. To express the other forces in terms of the unit vectors $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$, we write

$$\overrightarrow{AB} = -(36 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (27 \text{ in.})\mathbf{k}$$
$$AB = 75 \text{ in.}$$
$$\overrightarrow{AC} = (60 \text{ in.})\mathbf{j} + (32 \text{ in.})\mathbf{k}$$
$$AC = 68 \text{ in.}$$
$$\overrightarrow{AD} = (40 \text{ in.})\mathbf{i} + (60 \text{ in.})\mathbf{j} - (27 \text{ in.})\mathbf{k}$$
$$AD = 77 \text{ in.}$$



and

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$
$$= (-0.48\mathbf{i} + 0.8\mathbf{j} - 0.36\mathbf{k})T_{AB}$$
$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC}$$
$$= (0.88235\mathbf{j} + 0.47059\mathbf{k})T_{AC}$$
$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD}$$
$$= (0.51948\mathbf{i} + 0.77922\mathbf{j} - 0.35065\mathbf{k})T_{AD}$$

Equilibrium Condition with $\mathbf{W} = -W\mathbf{j}$

$$\Sigma F = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} - W\mathbf{j} = 0$$

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PROBLEM 2.106 (Continued)

Substituting the expressions obtained for $\mathbf{T}_{AB}$, $\mathbf{T}_{AC}$, and $\mathbf{T}_{AD}$ and factoring **i**, **j**, and **k**:

$$(-0.48T_{AB} + 0.51948T_{AD})\mathbf{i} + (0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W)\mathbf{j}$$
$$+ (-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD})\mathbf{k} = 0$$

Equating to zero the coefficients of **i**, **j**, **k**:

$$-0.48T_{AB} + 0.51948T_{AD} = 0 \quad (1)$$

$$0.8T_{AB} + 0.88235T_{AC} + 0.77922T_{AD} - W = 0 \quad (2)$$

$$-0.36T_{AB} + 0.47059T_{AC} - 0.35065T_{AD} = 0 \quad (3)$$

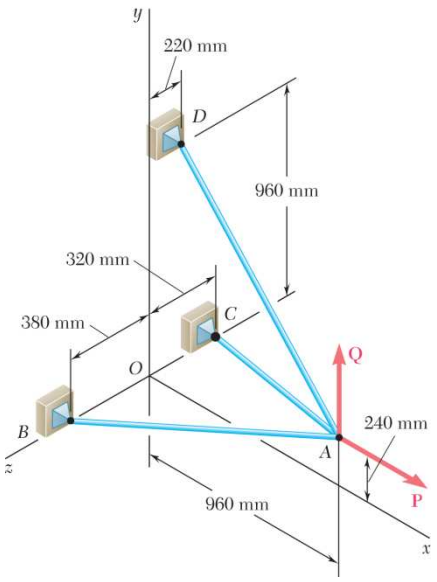
Substituting $W = 1600$ lb in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms gives,

$T_{AB} = 571$ lb ◀

$T_{AC} = 830$ lb ◀

$T_{AD} = 528$ lb ◀

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PROBLEM 2.107

Three cables are connected at A, where the forces **P** and **Q** are applied as shown. Knowing that $Q = 0$, find the value of P for which the tension in cable AD is 305 N.

SOLUTION

$$\Sigma \mathbf{F}_A = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{P} = 0 \quad \text{where} \quad \mathbf{P} = P\mathbf{i}$$

$$\overrightarrow{AB} = -(960\text{ mm})\mathbf{i} - (240\text{ mm})\mathbf{j} + (380\text{ mm})\mathbf{k} \qquad AB = 1060\text{ mm}$$

$$\overrightarrow{AC} = -(960\text{ mm})\mathbf{i} - (240\text{ mm})\mathbf{j} - (320\text{ mm})\mathbf{k} \qquad AC = 1040\text{ mm}$$

$$\overrightarrow{AD} = -(960\text{ mm})\mathbf{i} + (720\text{ mm})\mathbf{j} - (220\text{ mm})\mathbf{k} \qquad AD = 1220\text{ mm}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = T_{AB}\left(-\frac{48}{53}\mathbf{i} - \frac{12}{53}\mathbf{j} + \frac{19}{53}\mathbf{k}\right)$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\left(-\frac{12}{13}\mathbf{i} - \frac{3}{13}\mathbf{j} - \frac{4}{13}\mathbf{k}\right)$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = \frac{305\text{ N}}{1220\text{ mm}}[(-960\text{ mm})\mathbf{i} + (720\text{ mm})\mathbf{j} - (220\text{ mm})\mathbf{k}]$$
$$= -(240\text{ N})\mathbf{i} + (180\text{ N})\mathbf{j} - (55\text{ N})\mathbf{k}$$

Substituting into $\Sigma \mathbf{F}_A = 0$, factoring **i**, **j**, **k**, and setting each coefficient equal to ϕ gives:

$$\mathbf{i}: \quad P = \frac{48}{53}T_{AB} + \frac{12}{13}T_{AC} + 240\text{ N} \tag{1}$$

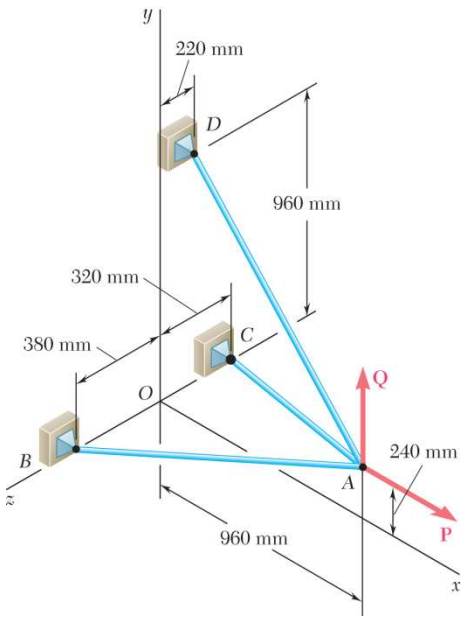
$$\mathbf{j}: \quad \frac{12}{53}T_{AB} + \frac{3}{13}T_{AC} = 180\text{ N} \tag{2}$$

$$\mathbf{k}: \quad \frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} = 55\text{ N} \tag{3}$$

Solving the system of linear equations using conventional algorithms gives:

$$T_{AB} = 446.71\text{ N}$$
$$T_{AC} = 341.71\text{ N}$$
$$P = 960\text{ N} \blacktriangleleft$$

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PROBLEM 2.108

Three cables are connected at A, where the forces **P** and **Q** are applied as shown. Knowing that $P = 1200$ N, determine the values of Q for which cable AD is taut.

SOLUTION

We assume that $T_{AD} = 0$ and write $\quad \Sigma \mathbf{F}_A = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + Q\mathbf{j} + (1200 \text{ N})\mathbf{i} = 0$

$$\overrightarrow{AB} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} + (380 \text{ mm})\mathbf{k} \quad AB = 1060 \text{ mm}$$

$$\overrightarrow{AC} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k} \quad AC = 1040 \text{ mm}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = \left(-\frac{48}{53}\mathbf{i} - \frac{12}{53}\mathbf{j} + \frac{19}{53}\mathbf{k}\right)T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = \left(-\frac{12}{13}\mathbf{i} - \frac{3}{13}\mathbf{j} - \frac{4}{13}\mathbf{k}\right)T_{AC}$$

Substituting into $\Sigma \mathbf{F}_A = 0$, factoring **i**, **j**, **k**, and setting each coefficient equal to ϕ gives:

$$\mathbf{i}: \quad -\frac{48}{53}T_{AB} - \frac{12}{13}T_{AC} + 1200 \text{ N} = 0 \tag{1}$$

$$\mathbf{j}: \quad -\frac{12}{53}T_{AB} - \frac{3}{13}T_{AC} + Q = 0 \tag{2}$$

$$\mathbf{k}: \quad \frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} = 0 \tag{3}$$

Solving the resulting system of linear equations using conventional algorithms gives:

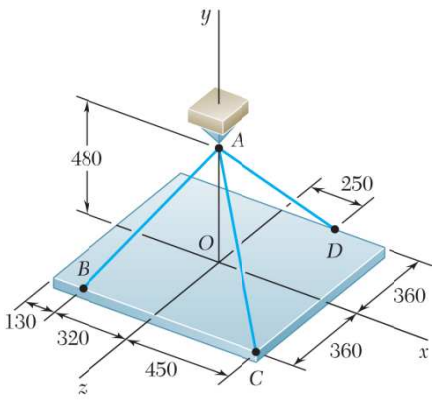
$$T_{AB} = 605.71 \text{ N}$$

$$T_{AC} = 705.71 \text{ N}$$

$$Q = 300.00 \text{ N} \qquad 0 \le Q < 300 \text{ N} \blacktriangleleft$$

Note: This solution assumes that Q is directed upward as shown $(Q \ge 0)$, if negative values of Q are considered, cable AD remains taut, but AC becomes slack for $Q = -460$ N.

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Dimensions in mm

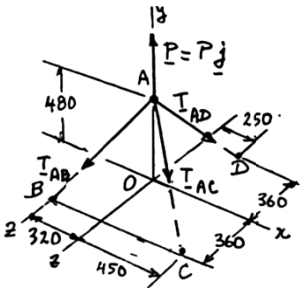
PROBLEM 2.109

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable AC is 60 N, determine the weight of the plate.

SOLUTION

We note that the weight of the plate is equal in magnitude to the force **P** exerted by the support on Point A.

Free Body A:



Dimensions in mm

$$\Sigma F = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$$

We have:

$$\overrightarrow{AB} = -(320\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad AB = 680\text{ mm}$$

$$\overrightarrow{AC} = (450\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} + (360\text{ mm})\mathbf{k} \qquad AC = 750\text{ mm}$$

$$\overrightarrow{AD} = (250\text{ mm})\mathbf{i} - (480\text{ mm})\mathbf{j} - (360\text{ mm})\mathbf{k} \qquad AD = 650\text{ mm}$$

Thus:

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = \left(-\frac{8}{17}\mathbf{i} - \frac{12}{17}\mathbf{j} + \frac{9}{17}\mathbf{k}\right)T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = \left(0.6\mathbf{i} - 0.64\mathbf{j} + 0.48\mathbf{k}\right)T_{AC}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = \left(\frac{5}{13}\mathbf{i} - \frac{9.6}{13}\mathbf{j} - \frac{7.2}{13}\mathbf{k}\right)T_{AD}$$

Substituting into the Eq. $\Sigma F = 0$ and factoring $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$:

$$\left(-\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD}\right)\mathbf{i}$$

$$+\left(-\frac{12}{17}T_{AB} - 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P\right)\mathbf{j}$$

$$+\left(\frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD}\right)\mathbf{k} = 0$$

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PROBLEM 2.109 (Continued)

Setting the coefficient of **i**, **j**, **k** equal to zero:

$$\mathbf{i}: \quad -\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD} = 0 \tag{1}$$

$$\mathbf{j}: \quad -\frac{12}{7}T_{AB} - 0.64T_{AC} - \frac{9.6}{13}T_{AD} + P = 0 \tag{2}$$

$$\mathbf{k}: \quad \frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD} = 0 \tag{3}$$

Making $T_{AC} = 60$ N in (1) and (3):

$$-\frac{8}{17}T_{AB} + 36\text{ N} + \frac{5}{13}T_{AD} = 0 \tag{1′}$$

$$\frac{9}{17}T_{AB} + 28.8\text{ N} - \frac{7.2}{13}T_{AD} = 0 \tag{3′}$$

Multiply (1′) by 9, (3′) by 8, and add:

$$554.4\text{ N} - \frac{12.6}{13}T_{AD} = 0 \quad T_{AD} = 572.0\text{ N}$$

Substitute into (1′) and solve for T_{AB}:

$$T_{AB} = \frac{17}{8}\left(36 + \frac{5}{13} \times 572\right) \qquad T_{AB} = 544.0\text{ N}$$

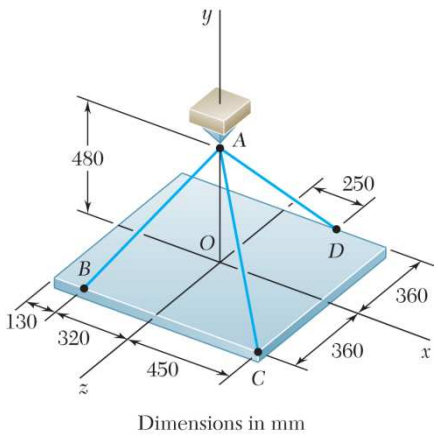
Substitute for the tensions in Eq. (2) and solve for P:

$$P = \frac{12}{17}(544\text{ N}) + 0.64(60\text{ N}) + \frac{9.6}{13}(572\text{ N})$$

$$= 844.8\text{ N}$$

Weight of plate $= P = 845$ N ◀

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Dimensions in mm

PROBLEM 2.110

A rectangular plate is supported by three cables as shown. Knowing that the tension in cable *AD* is 520 N, determine the weight of the plate.

SOLUTION

See Problem 2.109 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-\frac{8}{17}T_{AB}+0.6T_{AC}+\frac{5}{13}T_{AD}=0 \tag{1}$$

$$-\frac{12}{17}T_{AB}+0.64T_{AC}-\frac{9.6}{13}T_{AD}+P=0 \tag{2}$$

$$\frac{9}{17}T_{AB}+0.48T_{AC}-\frac{7.2}{13}T_{AD}=0 \tag{3}$$

Making $T_{AD}=520$ N in Eqs. (1) and (3):

$$-\frac{8}{17}T_{AB}+0.6T_{AC}+200\text{ N}=0 \tag{1′}$$

$$\frac{9}{17}T_{AB}+0.48T_{AC}-288\text{ N}=0 \tag{3′}$$

Multiply (1′) by 9, (3′) by 8, and add:

$$9.24T_{AC}-504\text{ N}=0 \quad T_{AC}=54.5455\text{ N}$$

Substitute into (1′) and solve for T_{AB}:

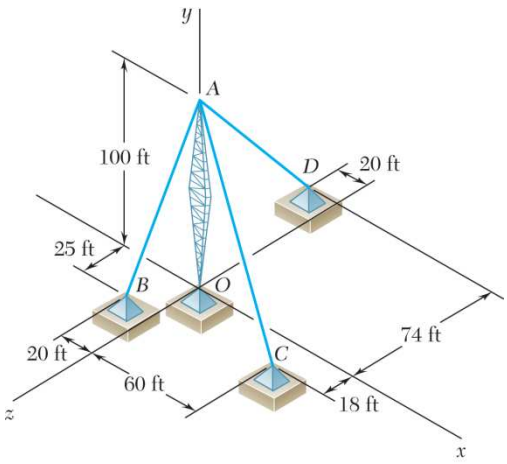
$$T_{AB}=\frac{17}{8}(0.6\times 54.5455+200) \quad T_{AB}=494.545\text{ N}$$

Substitute for the tensions in Eq. (2) and solve for *P*:

$$P=\frac{12}{17}(494.545\text{ N})+0.64(54.5455\text{ N})+\frac{9.6}{13}(520\text{ N})$$
$$=768.00\text{ N}$$

Weight of plate $=P=768$ N ◀

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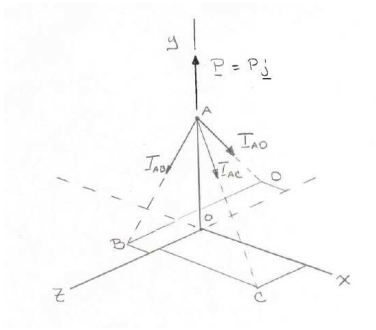
PROBLEM 2.111

A transmission tower is held by three guy wires attached to a pin at *A* and anchored by bolts at *B*, *C*, and *D*. If the tension in wire *AB* is 840 lb, determine the vertical force **P** exerted by the tower on the pin at *A*.

SOLUTION

$$\Sigma \mathbf{F} = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$$

Free-Body Diagram at *A*:



$$\overrightarrow{AB} = -20\mathbf{i} - 100\mathbf{j} + 25\mathbf{k} \quad AB = 105 \text{ ft}$$
$$\overrightarrow{AC} = 60\mathbf{i} - 100\mathbf{j} + 18\mathbf{k} \quad AC = 118 \text{ ft}$$
$$\overrightarrow{AD} = -20\mathbf{i} - 100\mathbf{j} - 74\mathbf{k} \quad AD = 126 \text{ ft}$$

We write

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$
$$= \left(-\frac{4}{21}\mathbf{i} - \frac{20}{21}\mathbf{j} + \frac{5}{21}\mathbf{k}\right)T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC}$$
$$= \left(\frac{30}{59}\mathbf{i} - \frac{50}{59}\mathbf{j} + \frac{9}{59}\mathbf{k}\right)T_{AC}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD}$$
$$= \left(-\frac{10}{63}\mathbf{i} - \frac{50}{63}\mathbf{j} - \frac{37}{63}\mathbf{k}\right)T_{AD}$$

Substituting into the Eq. $\Sigma\mathbf{F} = 0$ and factoring $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$:

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PROBLEM 2.111 (Continued)

$$\left(-\frac{4}{21}T_{AB}+\frac{30}{59}T_{AC}-\frac{10}{63}T_{AD}\right)\mathbf{i}$$
$$+\left(-\frac{20}{21}T_{AB}-\frac{50}{59}T_{AC}-\frac{50}{63}T_{AD}+P\right)\mathbf{j}$$
$$+\left(\frac{5}{21}T_{AB}+\frac{9}{59}T_{AC}-\frac{37}{63}T_{AD}\right)\mathbf{k}=0$$

Setting the coefficients of **i**, **j**, **k**, equal to zero:

$$\mathbf{i}: \quad -\frac{4}{21}T_{AB}+\frac{30}{59}T_{AC}-\frac{10}{63}T_{AD}=0 \tag{1}$$

$$\mathbf{j}: \quad -\frac{20}{21}T_{AB}-\frac{50}{59}T_{AC}-\frac{50}{63}T_{AD}+P=0 \tag{2}$$

$$\mathbf{k}: \quad \frac{5}{21}T_{AB}+\frac{9}{59}T_{AC}-\frac{37}{63}T_{AD}=0 \tag{3}$$

Set $T_{AB}=840$ lb in Eqs. (1) – (3):

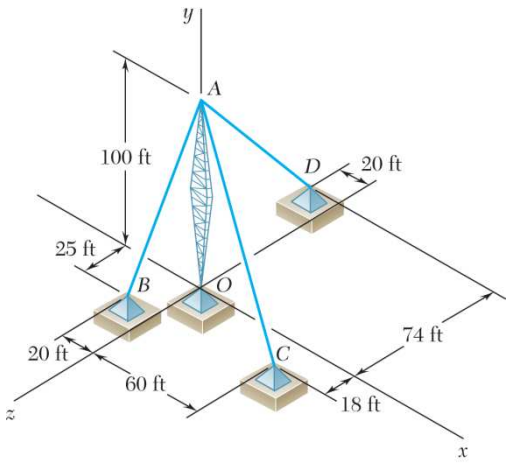
$$-160 \text{ lb}+\frac{30}{59}T_{AC}-\frac{10}{63}T_{AD}=0 \tag{1′}$$

$$-800 \text{ lb}-\frac{50}{59}T_{AC}-\frac{50}{63}T_{AD}+P=0 \tag{2′}$$

$$200 \text{ lb}+\frac{9}{59}T_{AC}-\frac{37}{63}T_{AD}=0 \tag{3′}$$

Solving, $T_{AC}=458.12$ lb $T_{AD}=459.53$ lb $P=1552.94$ lb $P=1553$ lb ◀

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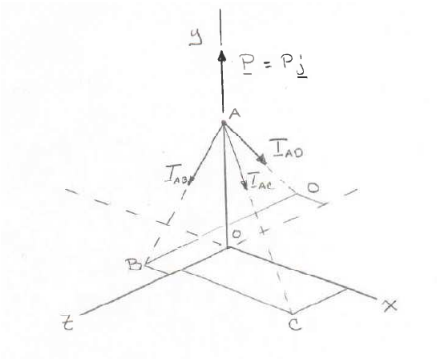
PROBLEM 2.112

A transmission tower is held by three guy wires attached to a pin at *A* and anchored by bolts at *B*, *C*, and *D*. If the tension in wire *AC* is 590 lb, determine the vertical force **P** exerted by the tower on the pin at *A*.

SOLUTION

$$\Sigma \mathbf{F} = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + P\mathbf{j} = 0$$

Free-Body Diagram at *A*:



$$\overrightarrow{AB} = -20\mathbf{i} - 100\mathbf{j} + 25\mathbf{k} \quad AB = 105 \text{ ft}$$
$$\overrightarrow{AC} = 60\mathbf{i} - 100\mathbf{j} + 18\mathbf{k} \quad AC = 118 \text{ ft}$$
$$\overrightarrow{AD} = -20\mathbf{i} - 100\mathbf{j} - 74\mathbf{k} \quad AD = 126 \text{ ft}$$

We write

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$
$$= \left(-\frac{4}{21}\mathbf{i} - \frac{20}{21}\mathbf{j} + \frac{5}{21}\mathbf{k}\right)T_{AB}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC}$$
$$= \left(\frac{30}{59}\mathbf{i} - \frac{50}{59}\mathbf{j} + \frac{9}{59}\mathbf{k}\right)T_{AC}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD}$$
$$= \left(-\frac{10}{63}\mathbf{i} - \frac{50}{63}\mathbf{j} - \frac{37}{63}\mathbf{k}\right)T_{AD}$$

Substituting into the Eq. $\Sigma \mathbf{F} = 0$ and factoring $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$:

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PROBLEM 2.112 (Continued)

$$\left(-\frac{4}{21}T_{AB}+\frac{30}{59}T_{AC}-\frac{10}{63}T_{AD}\right)\mathbf{i}$$
$$+\left(-\frac{20}{21}T_{AB}-\frac{50}{59}T_{AC}-\frac{50}{63}T_{AD}+P\right)\mathbf{j}$$
$$+\left(\frac{5}{21}T_{AB}+\frac{9}{59}T_{AC}-\frac{37}{63}T_{AD}\right)\mathbf{k}=0$$

Setting the coefficients of $\mathbf{i}$, $\mathbf{j}$, $\mathbf{k}$, equal to zero:

$$\mathbf{i}: \quad -\frac{4}{21}T_{AB}+\frac{30}{59}T_{AC}-\frac{10}{63}T_{AD}=0 \tag{1}$$

$$\mathbf{j}: \quad -\frac{20}{21}T_{AB}-\frac{50}{59}T_{AC}-\frac{50}{63}T_{AD}+P=0 \tag{2}$$

$$\mathbf{k}: \quad \frac{5}{21}T_{AB}+\frac{9}{59}T_{AC}-\frac{37}{63}T_{AD}=0 \tag{3}$$

Set $T_{AC}=590$ lb in Eqs. (1) – (3):

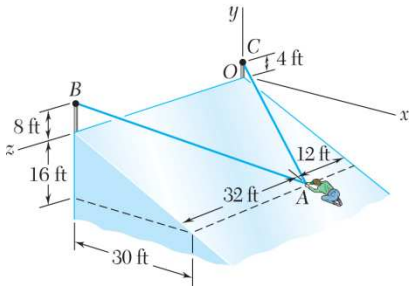
$$-\frac{4}{21}T_{AB}+300\text{ lb}-\frac{10}{63}T_{AD}=0 \tag{1′}$$

$$-\frac{20}{21}T_{AB}-500\text{ lb}-\frac{50}{63}T_{AD}+P=0 \tag{2′}$$

$$\frac{5}{21}T_{AB}+90\text{ lb}-\frac{37}{63}T_{AD}=0 \tag{3′}$$

Solving, $T_{AB}=1081.82$ lb $T_{AD}=591.82$ lb $P=2000$ lb ◀

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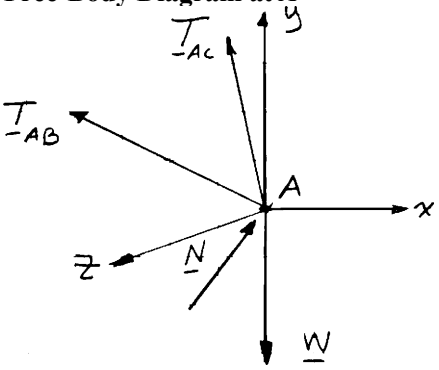


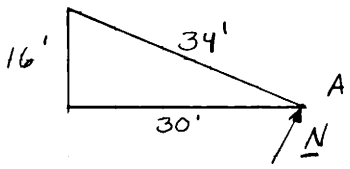
PROBLEM 2.113

In trying to move across a slippery icy surface, a 175-lb man uses two ropes AB and AC. Knowing that the force exerted on the man by the icy surface is perpendicular to that surface, determine the tension in each rope.

SOLUTION

Free-Body Diagram at A





$$\mathbf{N} = N\left(\frac{16}{34}\mathbf{i} + \frac{30}{34}\mathbf{j}\right)$$

and $\mathbf{W} = W\,\mathbf{j} = -(175\text{ lb})\mathbf{j}$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\frac{(-30\text{ ft})\mathbf{i} + (20\text{ ft})\mathbf{j} - (12\text{ ft})\mathbf{k}}{38\text{ ft}}$$

$$= T_{AC}\left(-\frac{15}{19}\mathbf{i} + \frac{10}{19}\mathbf{j} - \frac{6}{19}\mathbf{k}\right)$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = T_{AB}\frac{(-30\text{ ft})\mathbf{i} + (24\text{ ft})\mathbf{j} + (32\text{ ft})\mathbf{k}}{50\text{ ft}}$$

$$= T_{AB}\left(-\frac{15}{25}\mathbf{i} + \frac{12}{25}\mathbf{j} + \frac{16}{25}\mathbf{k}\right)$$

Equilibrium condition: $\Sigma\mathbf{F} = 0$

$$\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{N} + \mathbf{W} = 0$$

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PROBLEM 2.113 (Continued)

Substituting the expressions obtained for $\mathbf{T}_{AB}, \mathbf{T}_{AC}, \mathbf{N}$, and $\mathbf{W}$; factoring **i**, **j**, and **k**; and equating each of the coefficients to zero gives the following equations:

From **i**:
$$-\frac{15}{25}T_{AB} - \frac{15}{19}T_{AC} + \frac{16}{34}N = 0 \tag{1}$$

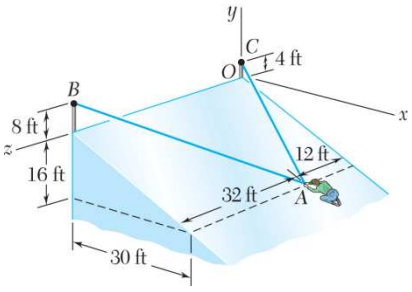
From **j**:
$$\frac{12}{25}T_{AB} + \frac{10}{19}T_{AC} + \frac{30}{34}N - (175 \text{ lb}) = 0 \tag{2}$$

From **k**:
$$\frac{16}{25}T_{AB} - \frac{6}{19}T_{AC} = 0 \tag{3}$$

Solving the resulting set of equations gives:

$$T_{AB} = 30.8 \text{ lb}; \quad T_{AC} = 62.5 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.114

Solve Problem 2.113, assuming that a friend is helping the man at A by pulling on him with a force $\mathbf{P} = -(45 \text{ lb})\mathbf{k}$.

PROBLEM 2.113 In trying to move across a slippery icy surface, a 175-lb man uses two ropes AB and AC. Knowing that the force exerted on the man by the icy surface is perpendicular to that surface, determine the tension in each rope.

SOLUTION

Refer to Problem 2.113 for the figure and analysis leading to the following set of equations, Equation (3) being modified to include the additional force $\mathbf{P} = (-45 \text{ lb})\mathbf{k}$.

$$-\frac{15}{25}T_{AB} - \frac{15}{19}T_{AC} + \frac{16}{34}N = 0 \tag{1}$$

$$\frac{12}{25}T_{AB} + \frac{10}{19}T_{AC} + \frac{30}{34}N - (175 \text{ lb}) = 0 \tag{2}$$

$$\frac{16}{25}T_{AB} - \frac{6}{19}T_{AC} - (45 \text{ lb}) = 0 \tag{3}$$

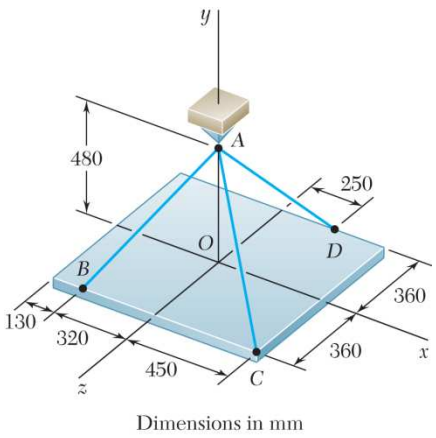
Solving the resulting set of equations simultaneously gives:

$$T_{AB} = 81.3 \text{ lb} \blacktriangleleft$$

$$T_{AC} = 22.2 \text{ lb} \blacktriangleleft$$

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Vector Mechanics for Engineers Statics and Dynamics 11th edition Beer Solutions Manual



Dimensions in mm

PROBLEM 2.115

For the rectangular plate of Problems 2.109 and 2.110, determine the tension in each of the three cables knowing that the weight of the plate is 792 N.

SOLUTION

See Problem 2.109 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below. Setting $P = 792$ N gives:

$$-\frac{8}{17}T_{AB} + 0.6T_{AC} + \frac{5}{13}T_{AD} = 0 \tag{1}$$

$$-\frac{12}{17}T_{AB} - 0.64T_{AC} - \frac{9.6}{13}T_{AD} + 792\text{ N} = 0 \tag{2}$$

$$\frac{9}{17}T_{AB} + 0.48T_{AC} - \frac{7.2}{13}T_{AD} = 0 \tag{3}$$

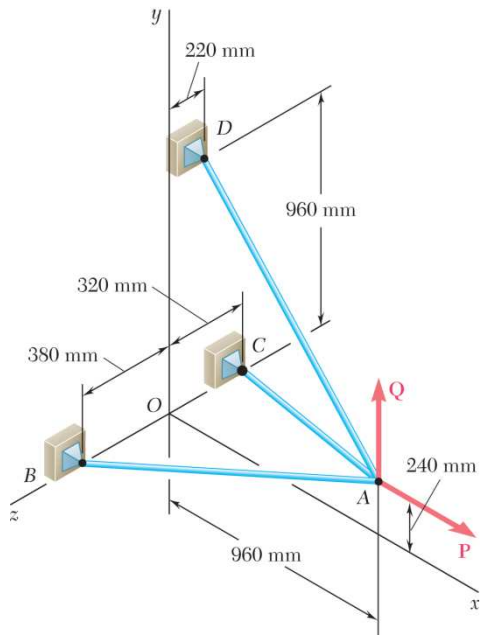
Solving Equations (1), (2), and (3) by conventional algorithms gives

$$T_{AB} = 510.00\text{ N} \qquad T_{AB} = 510\text{ N} \blacktriangleleft$$

$$T_{AC} = 56.250\text{ N} \qquad T_{AC} = 56.2\text{ N} \blacktriangleleft$$

$$T_{AD} = 536.25\text{ N} \qquad T_{AD} = 536\text{ N} \blacktriangleleft$$

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PROBLEM 2.116

For the cable system of Problems 2.107 and 2.108, determine the tension in each cable knowing that $P = 2880$ N and $Q = 0$.

SOLUTION

$$\Sigma \mathbf{F}_A = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{P} + \mathbf{Q} = 0$$

Where $\mathbf{P} = P\mathbf{i}$ and $\mathbf{Q} = Q\mathbf{j}$

$$\overrightarrow{AB} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} + (380 \text{ mm})\mathbf{k} \qquad AB = 1060 \text{ mm}$$

$$\overrightarrow{AC} = -(960 \text{ mm})\mathbf{i} - (240 \text{ mm})\mathbf{j} - (320 \text{ mm})\mathbf{k} \qquad AC = 1040 \text{ mm}$$

$$\overrightarrow{AD} = -(960 \text{ mm})\mathbf{i} + (720 \text{ mm})\mathbf{j} - (220 \text{ mm})\mathbf{k} \qquad AD = 1220 \text{ mm}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB} = T_{AB}\left(-\frac{48}{53}\mathbf{i} - \frac{12}{53}\mathbf{j} + \frac{19}{53}\mathbf{k}\right)$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = T_{AC}\left(-\frac{12}{13}\mathbf{i} - \frac{3}{13}\mathbf{j} - \frac{4}{13}\mathbf{k}\right)$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = T_{AD}\left(-\frac{48}{61}\mathbf{i} + \frac{36}{61}\mathbf{j} - \frac{11}{61}\mathbf{k}\right)$$

Substituting into $\Sigma \mathbf{F}_A = 0$, setting $P = (2880 \text{ N})\mathbf{i}$ and $Q = 0$, and setting the coefficients of **i**, **j**, **k** equal to 0, we obtain the following three equilibrium equations:

$$\mathbf{i}: \quad -\frac{48}{53}T_{AB} - \frac{12}{13}T_{AC} - \frac{48}{61}T_{AD} + 2880 \text{ N} = 0 \tag{1}$$

$$\mathbf{j}: \quad -\frac{12}{53}T_{AB} - \frac{3}{13}T_{AC} + \frac{36}{61}T_{AD} = 0 \tag{2}$$

$$\mathbf{k}: \quad \frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} - \frac{11}{61}T_{AD} = 0 \tag{3}$$

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PROBLEM 2.116 (Continued)

Solving the system of linear equations using conventional algorithms gives:

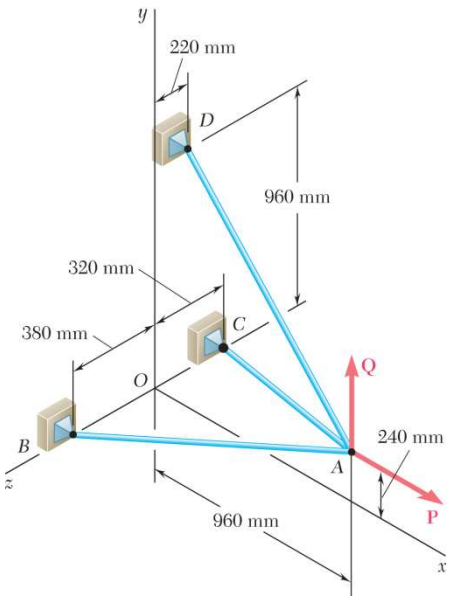
$$T_{AB} = 1340.14 \text{ N}$$
$$T_{AC} = 1025.12 \text{ N}$$
$$T_{AD} = 915.03 \text{ N}$$

$$T_{AB} = 1340 \text{ N} \blacktriangleleft$$

$$T_{AC} = 1025 \text{ N} \blacktriangleleft$$

$$T_{AD} = 915 \text{ N} \blacktriangleleft$$

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PROBLEM 2.117

For the cable system of Problems 2.107 and 2.108, determine the tension in each cable knowing that $P = 2880$ N and $Q = 576$ N.

SOLUTION

See Problem 2.116 for the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-\frac{48}{53}T_{AB} - \frac{12}{13}T_{AC} - \frac{48}{61}T_{AD} + P = 0 \tag{1}$$

$$-\frac{12}{53}T_{AB} - \frac{3}{13}T_{AC} + \frac{36}{61}T_{AD} + Q = 0 \tag{2}$$

$$\frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} - \frac{11}{61}T_{AD} = 0 \tag{3}$$

Setting $P = 2880$ N and $Q = 576$ N gives:

$$-\frac{48}{53}T_{AB} - \frac{12}{13}T_{AC} - \frac{48}{61}T_{AD} + 2880\text{ N} = 0 \tag{1'}$$

$$-\frac{12}{53}T_{AB} - \frac{3}{13}T_{AC} + \frac{36}{61}T_{AD} + 576\text{ N} = 0 \tag{2'}$$

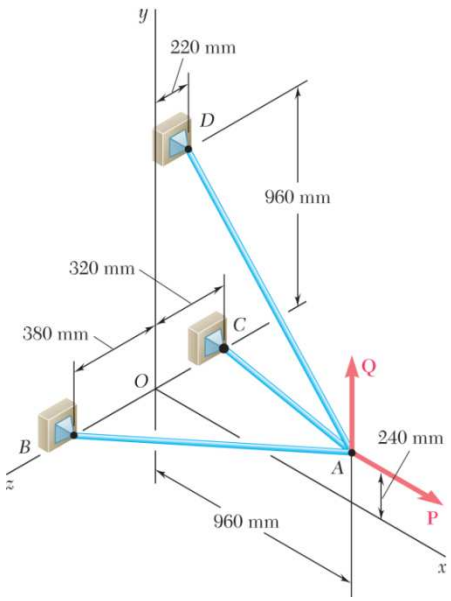
$$\frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} - \frac{11}{61}T_{AD} = 0 \tag{3'}$$

Solving the resulting set of equations using conventional algorithms gives:

$$T_{AB} = 1431.00\text{ N}$$
$$T_{AC} = 1560.00\text{ N}$$
$$T_{AD} = 183.010\text{ N}$$

$$T_{AB} = 1431\text{ N} \blacktriangleleft$$
$$T_{AC} = 1560\text{ N} \blacktriangleleft$$
$$T_{AD} = 183.0\text{ N} \blacktriangleleft$$

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PROBLEM 2.118

For the cable system of Problems 2.107 and 2.108, determine the tension in each cable knowing that $P = 2880$ N and $Q = -576$ N. (**Q** is directed downward).

SOLUTION

See Problem 2.116 for the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$-\frac{48}{53}T_{AB} - \frac{12}{13}T_{AC} - \frac{48}{61}T_{AD} + P = 0 \tag{1}$$

$$-\frac{12}{53}T_{AB} - \frac{3}{13}T_{AC} + \frac{36}{61}T_{AD} + Q = 0 \tag{2}$$

$$\frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} - \frac{11}{61}T_{AD} = 0 \tag{3}$$

Setting $P = 2880$ N and $Q = -576$ N gives:

$$-\frac{48}{53}T_{AB} - \frac{12}{13}T_{AC} - \frac{48}{61}T_{AD} + 2880\text{ N} = 0 \tag{1'}$$

$$-\frac{12}{53}T_{AB} - \frac{3}{13}T_{AC} + \frac{36}{61}T_{AD} - 576\text{ N} = 0 \tag{2'}$$

$$\frac{19}{53}T_{AB} - \frac{4}{13}T_{AC} - \frac{11}{61}T_{AD} = 0 \tag{3'}$$

Solving the resulting set of equations using conventional algorithms gives:

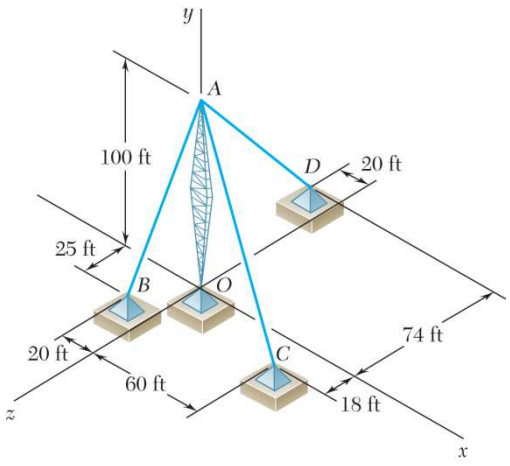
$$T_{AB} = 1249.29\text{ N}$$
$$T_{AC} = 490.31\text{ N}$$
$$T_{AD} = 1646.97\text{ N}$$

$$T_{AB} = 1249\text{ N} \blacktriangleleft$$

$$T_{AC} = 490\text{ N} \blacktriangleleft$$

$$T_{AD} = 1647\text{ N} \blacktriangleleft$$

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PROBLEM 2.119

For the transmission tower of Probs. 2.111 and 2.112, determine the tension in each guy wire knowing that the tower exerts on the pin at A an upward vertical force of 1800 lb.

PROBLEM 2.111 A transmission tower is held by three guy wires attached to a pin at A and anchored by bolts at B, C, and D. If the tension in wire AB is 840 lb, determine the vertical force **P** exerted by the tower on the pin at A.

SOLUTION

See Problem 2.111 for the figure and the analysis leading to the linear algebraic Equations (1), (2), and (3) below:

$$\mathbf{i}: \quad -\frac{4}{21}T_{AB}+\frac{30}{59}T_{AC}-\frac{10}{63}T_{AD}=0 \tag{1}$$

$$\mathbf{j}: \quad -\frac{20}{21}T_{AB}-\frac{50}{59}T_{AC}-\frac{50}{63}T_{AD}+P=0 \tag{2}$$

$$\mathbf{k}: \quad \frac{5}{21}T_{AB}+\frac{9}{59}T_{AC}-\frac{37}{63}T_{AD}=0 \tag{3}$$

Substituting for $P=1800$ lb in Equations (1), (2), and (3) above and solving the resulting set of equations using conventional algorithms gives:

$$-\frac{4}{21}T_{AB}+\frac{30}{59}T_{AC}-\frac{10}{63}T_{AD}=0 \tag{1′}$$

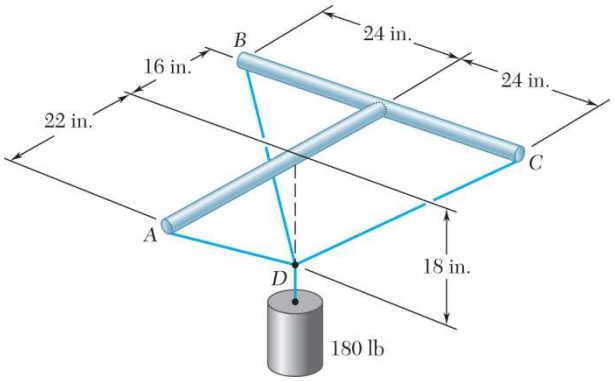
$$-\frac{20}{21}T_{AB}-\frac{50}{59}T_{AC}-\frac{50}{63}T_{AD}+1800\text{ lb}=0 \tag{2′}$$

$$\frac{5}{21}T_{AB}+\frac{9}{59}T_{AC}-\frac{37}{63}T_{AD}=0 \tag{3′}$$

$$T_{AB}=973.64\text{ lb}$$
$$T_{AC}=531.00\text{ lb}$$
$$T_{AD}=532.64\text{ lb}$$

$$T_{AB}=974\text{ lb} \blacktriangleleft$$
$$T_{AC}=531\text{ lb} \blacktriangleleft$$
$$T_{AD}=533\text{ lb} \blacktriangleleft$$

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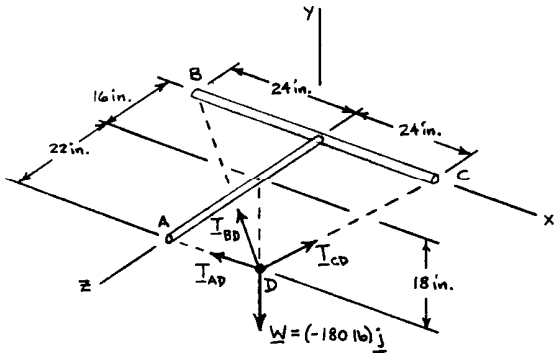


PROBLEM 2.120

Three wires are connected at point *D*, which is located 18 in. below the T-shaped pipe support *ABC*. Determine the tension in each wire when a 180-lb cylinder is suspended from point *D* as shown.

SOLUTION

Free-Body Diagram of Point *D*:



The forces applied at *D* are:

$$\mathbf{T}_{DA}, \mathbf{T}_{DB}, \mathbf{T}_{DC} \text{ and } \mathbf{W}$$

where $\mathbf{W} = -180.0\ \text{lb}\mathbf{j}$. To express the other forces in terms of the unit vectors **i**, **j**, **k**, we write

$$\overrightarrow{DA} = (18\ \text{in.})\mathbf{j} + (22\ \text{in.})\mathbf{k}$$
$$DA = 28.425\ \text{in.}$$
$$\overrightarrow{DB} = -(24\ \text{in.})\mathbf{i} + (18\ \text{in.})\mathbf{j} - (16\ \text{in.})\mathbf{k}$$
$$DB = 34.0\ \text{in.}$$
$$\overrightarrow{DC} = (24\ \text{in.})\mathbf{i} + (18\ \text{in.})\mathbf{j} - (16\ \text{in.})\mathbf{k}$$
$$DC = 34.0\ \text{in.}$$

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PROBLEM 2.120 (Continued)

and

$$\mathbf{T}_{DA} = T_{Da}\boldsymbol{\lambda}_{DA} = T_{Da}\frac{\overrightarrow{DA}}{DA}$$
$$= (0.63324\mathbf{j} + 0.77397\mathbf{k})T_{DA}$$
$$\mathbf{T}_{DB} = T_{DB}\boldsymbol{\lambda}_{DB} = T_{DB}\frac{\overrightarrow{DB}}{DB}$$
$$= (-0.70588\mathbf{i} + 0.52941\mathbf{j} - 0.47059\mathbf{k})T_{DB}$$
$$\mathbf{T}_{DC} = T_{DC}\boldsymbol{\lambda}_{DC} = T_{DC}\frac{\overrightarrow{DC}}{DC}$$
$$= (0.70588\mathbf{i} + 0.52941\mathbf{j} - 0.47059\mathbf{k})T_{DC}$$

Equilibrium Condition with $\mathbf{W} = -W\mathbf{j}$

$$\Sigma F = 0: \quad \mathbf{T}_{DA} + \mathbf{T}_{DB} + \mathbf{T}_{DC} - W\mathbf{j} = 0$$

Substituting the expressions obtained for $\mathbf{T}_{DA}$, $\mathbf{T}_{DB}$, and $\mathbf{T}_{DC}$ and factoring **i**, **j**, and **k**:

$$(-0.70588T_{DB} + 0.70588T_{DC})\mathbf{i}$$
$$(0.63324T_{DA} + 0.52941T_{DB} + 0.52941T_{DC} - W)\mathbf{j}$$
$$(0.77397T_{DA} - 0.47059T_{DB} - 0.47059T_{DC})\mathbf{k}$$

Equating to zero the coefficients of **i**, **j**, **k**:

$$-0.70588T_{DB} + 0.70588T_{DC} = 0 \tag{1}$$

$$0.63324T_{DA} + 0.52941T_{DB} + 0.52941T_{DC} - W = 0 \tag{2}$$

$$0.77397T_{DA} - 0.47059T_{DB} - 0.47059T_{DC} = 0 \tag{3}$$

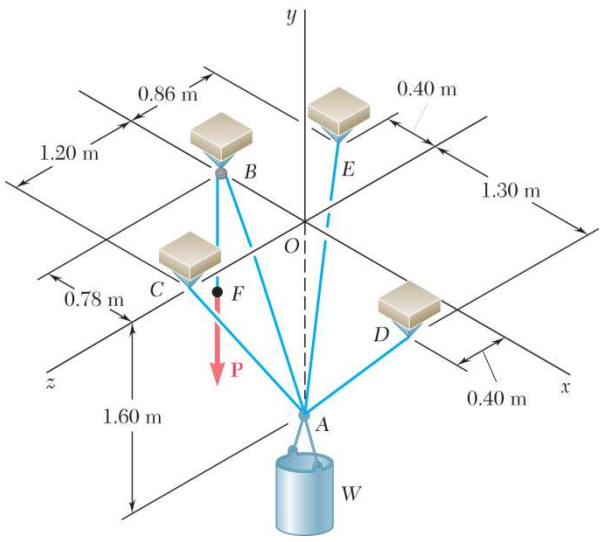
Substituting $W = 180$ lb in Equations (1), (2), and (3) above, and solving the resulting set of equations using conventional algorithms gives,

$T_{DA} = 119.7$ lb ◀

$T_{DB} = 98.4$ lb ◀

$T_{DC} = 98.4$ lb ◀

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PROBLEM 2.121

A container of weight W is suspended from ring A, to which cables AC and AE are attached. A force **P** is applied to the end F of a third cable that passes over a pulley at B and through ring A and that is attached to a support at D. Knowing that $W = 1000$ N, determine the magnitude of P. (*Hint:* The tension is the same in all portions of cable $FBAD$.)

SOLUTION

The (vector) force in each cable can be written as the product of the (scalar) force and the unit vector along the cable. That is, with

$$\overrightarrow{AB} = -(0.78\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} + (0\text{ m})\mathbf{k}$$

$$AB = \sqrt{(-0.78\text{ m})^2 + (1.6\text{ m})^2 + (0)^2}$$

$$= 1.78\text{ m}$$

$$\mathbf{T}_{AB} = T\boldsymbol{\lambda}_{AB} = T_{AB}\frac{\overrightarrow{AB}}{AB}$$

$$= \frac{T_{AB}}{1.78\text{ m}}[-(0.78\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} + (0\text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AB} = T_{AB}(-0.4382\mathbf{i} + 0.8989\mathbf{j} + 0\mathbf{k})$$

and

$$\overrightarrow{AC} = (0)\mathbf{i} + (1.6\text{ m})\mathbf{j} + (1.2\text{ m})\mathbf{k}$$

$$AC = \sqrt{(0\text{ m})^2 + (1.6\text{ m})^2 + (1.2\text{ m})^2} = 2\text{ m}$$

$$\mathbf{T}_{AC} = T\boldsymbol{\lambda}_{AC} = T_{AC}\frac{\overrightarrow{AC}}{AC} = \frac{T_{AC}}{2\text{ m}}[(0)\mathbf{i} + (1.6\text{ m})\mathbf{j} + (1.2\text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AC} = T_{AC}(0.8\mathbf{j} + 0.6\mathbf{k})$$

and

$$\overrightarrow{AD} = (1.3\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} + (0.4\text{ m})\mathbf{k}$$

$$AD = \sqrt{(1.3\text{ m})^2 + (1.6\text{ m})^2 + (0.4\text{ m})^2} = 2.1\text{ m}$$

$$\mathbf{T}_{AD} = T\boldsymbol{\lambda}_{AD} = T_{AD}\frac{\overrightarrow{AD}}{AD} = \frac{T_{AD}}{2.1\text{ m}}[(1.3\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} + (0.4\text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AD} = T_{AD}(0.6190\mathbf{i} + 0.7619\mathbf{j} + 0.1905\mathbf{k})$$

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PROBLEM 2.121 (Continued)

Finally,

$$\overrightarrow{AE} = -(0.4\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} - (0.86\text{ m})\mathbf{k}$$

$$AE = \sqrt{(-0.4\text{ m})^2 + (1.6\text{ m})^2 + (-0.86\text{ m})^2} = 1.86\text{ m}$$

$$\mathbf{T}_{AE} = T\boldsymbol{\lambda}_{AE} = T_{AE}\frac{\overrightarrow{AE}}{AE}$$

$$= \frac{T_{AE}}{1.86\text{ m}}[-(0.4\text{ m})\mathbf{i} + (1.6\text{ m})\mathbf{j} - (0.86\text{ m})\mathbf{k}]$$

$$\mathbf{T}_{AE} = T_{AE}(-0.2151\mathbf{i} + 0.8602\mathbf{j} - 0.4624\mathbf{k})$$

With the weight of the container $\mathbf{W} = -W\mathbf{j}$, at A we have:

$$\Sigma\mathbf{F} = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} - W\mathbf{j} = 0$$

Equating the factors of **i**, **j**, and **k** to zero, we obtain the following linear algebraic equations:

$$-0.4382T_{AB} + 0.6190T_{AD} - 0.2151T_{AE} = 0 \tag{1}$$

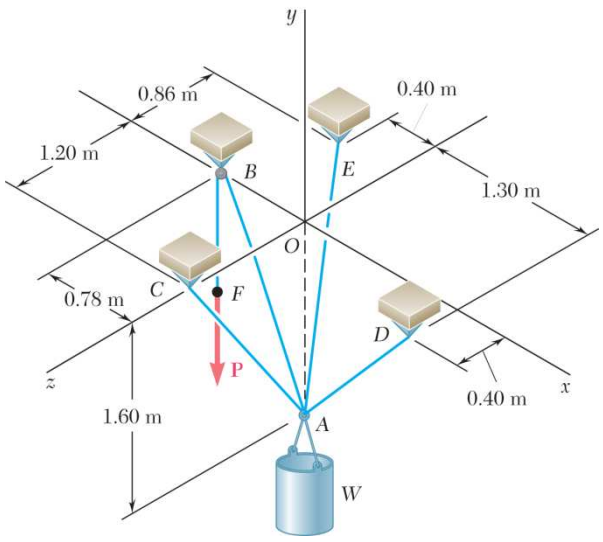
$$0.8989T_{AB} + 0.8T_{AC} + 0.7619T_{AD} + 0.8602T_{AE} - W = 0 \tag{2}$$

$$0.6T_{AC} + 0.1905T_{AD} - 0.4624T_{AE} = 0 \tag{3}$$

Knowing that $W = 1000$ N and that because of the pulley system at B $T_{AB} = T_{AD} = P$, where P is the externally applied (unknown) force, we can solve the system of linear Equations (1), (2) and (3) uniquely for P.

$P = 378$ N ◀

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PROBLEM 2.122

Knowing that the tension in cable AC of the system described in Problem 2.121 is 150 N, determine (*a*) the magnitude of the force **P**, (*b*) the weight W of the container.

PROBLEM 2.121 A container of weight W is suspended from ring A, to which cables AC and AE are attached. A force **P** is applied to the end F of a third cable that passes over a pulley at B and through ring A and that is attached to a support at D. Knowing that $W = 1000$ N, determine the magnitude of P. (*Hint:* The tension is the same in all portions of cable $FBAD$.)

SOLUTION

Here, as in Problem 2.121, the support of the container consists of the four cables AE, AC, AD, and AB, with the condition that the force in cables AB and AD is equal to the externally applied force P. Thus, with the condition

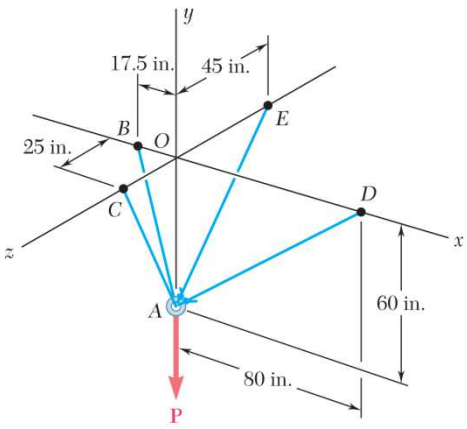
$$T_{AB} = T_{AD} = P$$

and using the linear algebraic equations of Problem 2.131 with $T_{AC} = 150$ N, we obtain

(*a*) $P = 454$ N ◀

(*b*) $W = 1202$ N ◀

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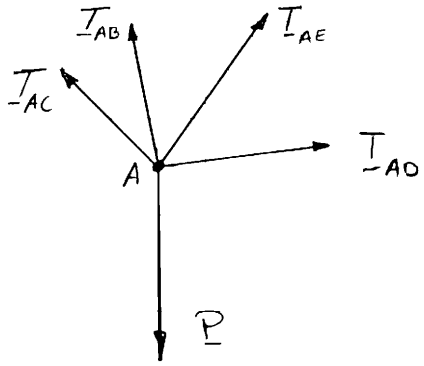


PROBLEM 2.123

Cable *BAC* passes through a frictionless ring *A* and is attached to fixed supports at *B* and *C*, while cables *AD* and *AE* are both tied to the ring and are attached, respectively, to supports at *D* and *E*. Knowing that a 200-lb vertical load **P** is applied to ring *A*, determine the tension in each of the three cables.

SOLUTION

Free Body Diagram at *A*:



Since T_{BAC} = tension in cable *BAC*, it follows that

$$T_{AB} = T_{AC} = T_{BAC}$$

$$\mathbf{T}_{AB} = T_{BAC}\boldsymbol{\lambda}_{AB} = T_{BAC}\frac{(-17.5\text{ in.})\mathbf{i} + (60\text{ in.})\mathbf{j}}{62.5\text{ in.}} = T_{BAC}\left(\frac{-17.5}{62.5}\mathbf{i} + \frac{60}{62.5}\mathbf{j}\right)$$

$$\mathbf{T}_{AC} = T_{BAC}\boldsymbol{\lambda}_{AC} = T_{BAC}\frac{(60\text{ in.})\mathbf{i} + (25\text{ in.})\mathbf{k}}{65\text{ in.}} = T_{BAC}\left(\frac{60}{65}\mathbf{j} + \frac{25}{65}\mathbf{k}\right)$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD}\frac{(80\text{ in.})\mathbf{i} + (60\text{ in.})\mathbf{j}}{100\text{ in.}} = T_{AD}\left(\frac{4}{5}\mathbf{i} + \frac{3}{5}\mathbf{j}\right)$$

$$\mathbf{T}_{AE} = T_{AE}\boldsymbol{\lambda}_{AE} = T_{AE}\frac{(60\text{ in.})\mathbf{j} - (45\text{ in.})\mathbf{k}}{75\text{ in.}} = T_{AE}\left(\frac{4}{5}\mathbf{j} - \frac{3}{5}\mathbf{k}\right)$$

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PROBLEM 2.123 (Continued)

Substituting into $\Sigma \mathbf{F}_A = 0$, setting $\mathbf{P} = (-200 \text{ lb})\mathbf{j}$, and setting the coefficients of **i**, **j**, **k** equal to ϕ, we obtain the following three equilibrium equations:

From **i**: $$-\frac{17.5}{62.5}T_{BAC} + \frac{4}{5}T_{AD} = 0 \tag{1}$$

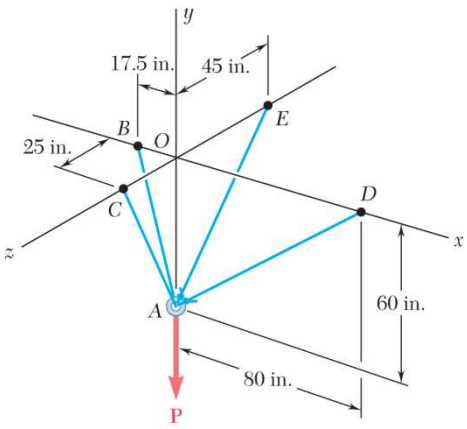
From **j**: $$\left(\frac{60}{62.5} + \frac{60}{65}\right)T_{BAC} + \frac{3}{5}T_{AD} + \frac{4}{5}T_{AE} - 200 \text{ lb} = 0 \tag{2}$$

From **k**: $$\frac{25}{65}T_{BAC} - \frac{3}{5}T_{AE} = 0 \tag{3}$$

Solving the system of linear equations using conventional algorithms gives:

$$T_{BAC} = 76.7 \text{ lb}; \; T_{AD} = 26.9 \text{ lb}; \; T_{AE} = 49.2 \text{ lb} \blacktriangleleft$$

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PROBLEM 2.124

Knowing that the tension in cable *AE* of Prob. 2.123 is 75 lb, determine (*a*) the magnitude of the load **P**, (*b*) the tension in cables *BAC* and *AD*.

PROBLEM 2.123 Cable *BAC* passes through a frictionless ring *A* and is attached to fixed supports at *B* and *C*, while cables *AD* and *AE* are both tied to the ring and are attached, respectively, to supports at *D* and *E*. Knowing that a 200-lb vertical load **P** is applied to ring *A*, determine the tension in each of the three cables.

SOLUTION

Refer to the solution to Problem 2.123 for the figure and analysis leading to the following set of equilibrium equations, Equation (2) being modified to include $P\mathbf{j}$ as an unknown quantity:

$$-\frac{17.5}{62.5}T_{BAC}+\frac{4}{5}T_{AD}=0 \tag{1}$$

$$\left(\frac{60}{62.5}+\frac{60}{65}\right)T_{BAC}+\frac{3}{5}T_{AD}+\frac{4}{5}T_{AE}-P=0 \tag{2}$$

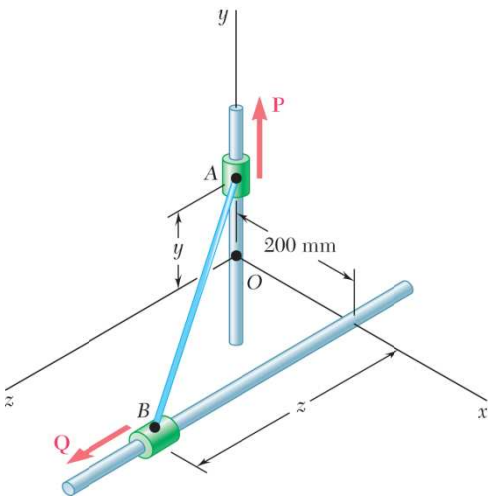
$$\frac{25}{65}T_{BAC}-\frac{3}{5}T_{AE}=0 \tag{3}$$

Substituting for $T_{AE}=75$ lb and solving simultaneously gives:

(*a*) $P=305$ lb ◀

(*b*) $T_{BAC}=117.0$ lb; $T_{AD}=40.9$ lb ◀

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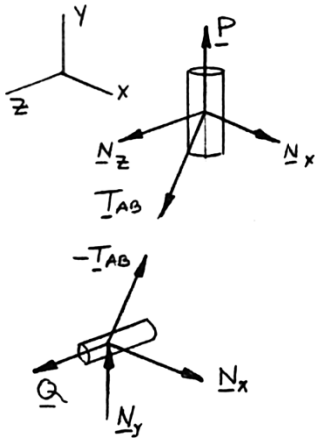
PROBLEM 2.125

Collars A and B are connected by a 525-mm-long wire and can slide freely on frictionless rods. If a force $\mathbf{P} = (341\text{ N})\mathbf{j}$ is applied to collar A, determine (a) the tension in the wire when $y = 155$ mm, (b) the magnitude of the force $\mathbf{Q}$ required to maintain the equilibrium of the system.

SOLUTION

For both Problems 2.125 and 2.126:

Free-Body Diagrams of Collars:



$$(AB)^2 = x^2 + y^2 + z^2$$

Here $$(0.525\text{ m})^2 = (0.20\text{ m})^2 + y^2 + z^2$$

or $$y^2 + z^2 = 0.23563\text{ m}^2$$

Thus, when y given, z is determined,

Now $$\boldsymbol{\lambda}_{AB} = \frac{\overrightarrow{AB}}{AB}$$

$$= \frac{1}{0.525\text{ m}}(0.20\mathbf{i} - y\mathbf{j} + z\mathbf{k})\text{m}$$

$$= 0.38095\mathbf{i} - 1.90476y\mathbf{j} + 1.90476z\mathbf{k}$$

Where y and z are in units of meters, m.

From the F.B. Diagram of collar A: $\Sigma\mathbf{F} = 0$: $N_x\mathbf{i} + N_z\mathbf{k} + P\mathbf{j} + T_{AB}\boldsymbol{\lambda}_{AB} = 0$

Setting the **j** coefficient to zero gives $P - (1.90476y)T_{AB} = 0$

With $$P = 341\text{ N}$$

$$T_{AB} = \frac{341\text{ N}}{1.90476y}$$

Now, from the free body diagram of collar B: $\Sigma\mathbf{F} = 0$: $N_x\mathbf{i} + N_y\mathbf{j} + Q\mathbf{k} - T_{AB}\boldsymbol{\lambda}_{AB} = 0$

Setting the **k** coefficient to zero gives $Q - T_{AB}(1.90476z) = 0$

And using the above result for T_{AB}, we have $$Q = T_{AB}z = \frac{341\text{ N}}{(1.90476)y}(1.90476z) = \frac{(341\text{ N})(z)}{y}$$

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PROBLEM 2.125 (Continued)

Then from the specifications of the problem, $y = 155 \text{ mm} = 0.155 \text{ m}$

$$z^2 = 0.23563 \text{ m}^2 - (0.155 \text{ m})^2$$
$$z = 0.46 \text{ m}$$

and

(*a*)
$$T_{AB} = \frac{341 \text{ N}}{0.155(1.90476)}$$
$$= 1155.00 \text{ N}$$

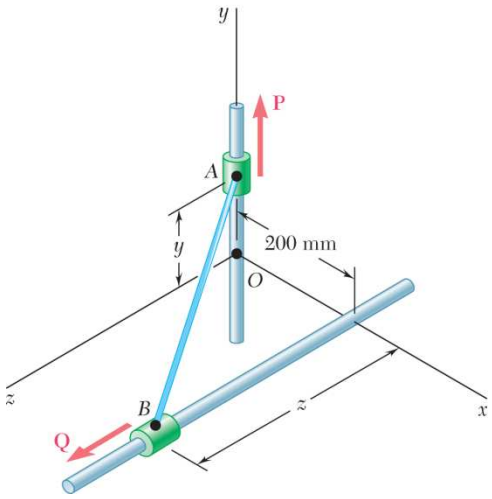
or
$$T_{AB} = 1155 \text{ N} \blacktriangleleft$$

and

(*b*)
$$Q = \frac{341 \text{ N}(0.46 \text{ m})(0.866)}{(0.155 \text{ m})}$$
$$= (1012.00 \text{ N})$$

or
$$Q = 1012 \text{ N} \blacktriangleleft$$

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PROBLEM 2.126

Solve Problem 2.125 assuming that $y = 275$ mm.

PROBLEM 2.125 Collars A and B are connected by a 525-mm-long wire and can slide freely on frictionless rods. If a force $\mathbf{P} = (341\text{ N})\mathbf{j}$ is applied to collar A, determine (a) the tension in the wire when $y = 155$ mm, (b) the magnitude of the force **Q** required to maintain the equilibrium of the system.

SOLUTION

From the analysis of Problem 2.125, particularly the results:

$$y^2 + z^2 = 0.23563\text{ m}^2$$

$$T_{AB} = \frac{341\text{ N}}{1.90476y}$$

$$Q = \frac{341\text{ N}}{y}z$$

With $y = 275\text{ mm} = 0.275\text{ m}$, we obtain:

$$z^2 = 0.23563\text{ m}^2 - (0.275\text{ m})^2$$

$$z = 0.40\text{ m}$$

and

(a) $$T_{AB} = \frac{341\text{ N}}{(1.90476)(0.275\text{ m})} = 651.00$$

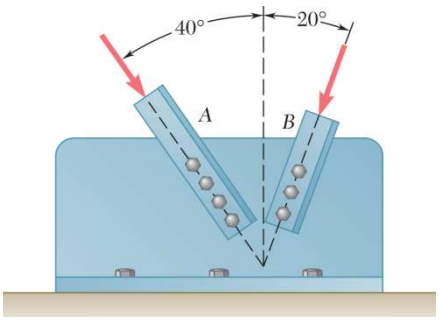
or $$T_{AB} = 651\text{ N} \blacktriangleleft$$

and

(b) $$Q = \frac{341\text{ N}(0.40\text{ m})}{(0.275\text{ m})}$$

or $$Q = 496\text{ N} \blacktriangleleft$$

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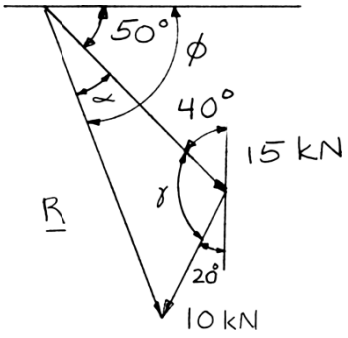


PROBLEM 2.127

Two structural members A and B are bolted to a bracket as shown. Knowing that both members are in compression and that the force is 15 kN in member A and 10 kN in member B, determine by trigonometry the magnitude and direction of the resultant of the forces applied to the bracket by members A and B.

SOLUTION

Using the force triangle and the laws of cosines and sines,



we have
$$\gamma = 180° - (40° + 20°)$$
$$= 120°$$

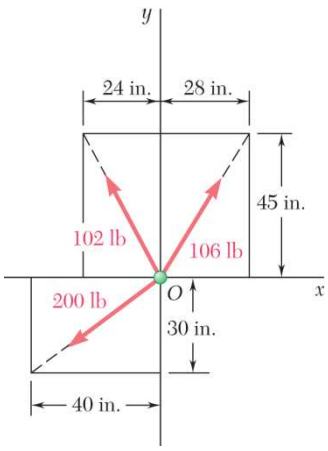
Then
$$R^2 = (15\text{ kN})^2 + (10\text{ kN})^2 - 2(15\text{ kN})(10\text{ kN})\cos 120°$$
$$= 475\text{ kN}^2$$
$$R = 21.794\text{ kN}$$

and
$$\frac{10\text{ kN}}{\sin\alpha} = \frac{21.794\text{ kN}}{\sin 120°}$$
$$\sin\alpha = \left(\frac{10\text{ kN}}{21.794\text{ kN}}\right)\sin 120°$$
$$= 0.39737$$
$$\alpha = 23.414$$

Hence:
$$\phi = \alpha + 50° = 73.414$$

R = 21.8 kN ⦤ 73.4° ◀

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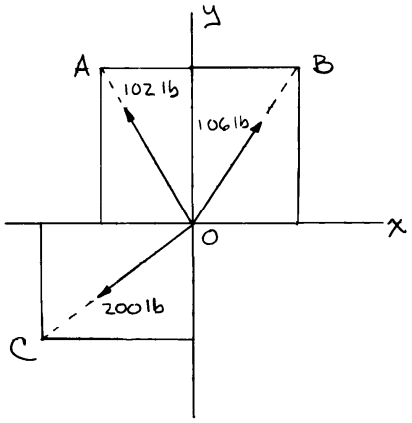


PROBLEM 2.128

Determine the x and y components of each of the forces shown.

SOLUTION

Compute the following distances:



$$OA = \sqrt{(24\text{ in.})^2 + (45\text{ in.})^2} = 51.0\text{ in.}$$

$$OB = \sqrt{(28\text{ in.})^2 + (45\text{ in.})^2} = 53.0\text{ in.}$$

$$OC = \sqrt{(40\text{ in.})^2 + (30\text{ in.})^2} = 50.0\text{ in.}$$

102-lb Force:

$$F_x = -102\text{ lb}\frac{24\text{ in.}}{51.0\text{ in.}} \qquad F_x = -48.0\text{ lb} \blacktriangleleft$$

$$F_y = +102\text{ lb}\frac{45\text{ in.}}{51.0\text{ in.}} \qquad F_y = +90.0\text{ lb} \blacktriangleleft$$

106-lb Force:

$$F_x = +106\text{ lb}\frac{28\text{ in.}}{53.0\text{ in.}} \qquad F_x = +56.0\text{ lb} \blacktriangleleft$$

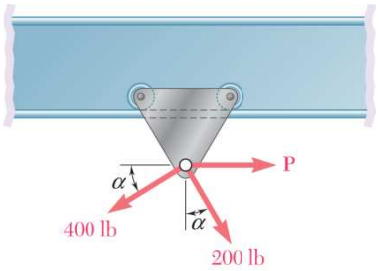
$$F_y = +106\text{ lb}\frac{45\text{ in.}}{53.0\text{ in.}} \qquad F_y = +90.0\text{ lb} \blacktriangleleft$$

200-lb Force:

$$F_x = -200\text{ lb}\frac{40\text{ in.}}{50.0\text{ in.}} \qquad F_x = -160.0\text{ lb} \blacktriangleleft$$

$$F_y = -200\text{ lb}\frac{30\text{ in.}}{50.0\text{ in.}} \qquad F_y = -120.0\text{ lb} \blacktriangleleft$$

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PROBLEM 2.129

A hoist trolley is subjected to the three forces shown. Knowing that $\alpha = 40°$, determine (*a*) the required magnitude of the force **P** if the resultant of the three forces is to be vertical, (*b*) the corresponding magnitude of the resultant.

SOLUTION

$$R_x = \overset{+}{\rightarrow} \Sigma F_x = P + (200 \text{ lb}) \sin 40° - (400 \text{ lb}) \cos 40°$$

$$R_x = P - 177.860 \text{ lb} \tag{1}$$

$$R_y = +\downarrow \Sigma F_y = (200 \text{ lb}) \cos 40° + (400 \text{ lb}) \sin 40°$$

$$R_y = 410.32 \text{ lb} \tag{2}$$

(*a*) For **R** to be vertical, we must have $R_x = 0$.

Set $R_x = 0$ in Eq. (1)

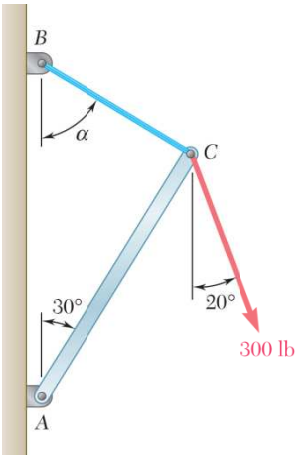
$$0 = P - 177.860 \text{ lb}$$

$$P = 177.860 \text{ lb} \qquad P = 177.9 \text{ lb} \blacktriangleleft$$

(*b*) Since **R** is to be vertical:

$$R = R_y = 410 \text{ lb} \qquad R = 410 \text{ lb} \blacktriangleleft$$

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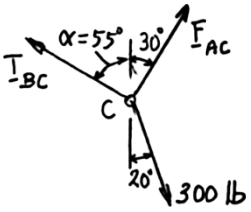


PROBLEM 2.130

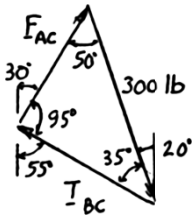
Knowing that $\alpha = 55°$ and that boom AC exerts on pin C a force directed along line AC, determine (*a*) the magnitude of that force, (*b*) the tension in cable BC.

SOLUTION

Free-Body Diagram



Force Triangle

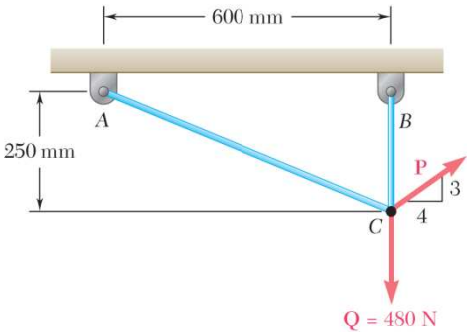


Law of sines:
$$\frac{F_{AC}}{\sin 35°} = \frac{T_{BC}}{\sin 50°} = \frac{300 \text{ lb}}{\sin 95°}$$

(*a*)
$$F_{AC} = \frac{300 \text{ lb}}{\sin 95°} \sin 35°$$
$$F_{AC} = 172.7 \text{ lb} \blacktriangleleft$$

(*b*)
$$T_{BC} = \frac{300 \text{ lb}}{\sin 95°} \sin 50°$$
$$T_{BC} = 231 \text{ lb} \blacktriangleleft$$

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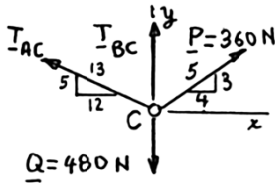


PROBLEM 2.131

Two cables are tied together at C and loaded as shown. Knowing that $P = 360$ N, determine the tension (*a*) in cable AC, (*b*) in cable BC.

SOLUTION

Free Body: *C*



(*a*) $\Sigma \mathbf{F}_x = 0$: $-\frac{12}{13} T_{AC} + \frac{4}{5}(360 \text{ N}) = 0$

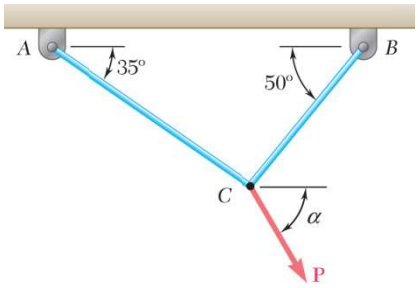
$T_{AC} = 312 \text{ N}$ ◀

(*b*) $\Sigma \mathbf{F}_y = 0$: $\frac{5}{13}(312 \text{ N}) + T_{BC} + \frac{3}{5}(360 \text{ N}) - 480 \text{ N} = 0$

$T_{BC} = 480 \text{ N} - 120 \text{ N} - 216 \text{ N}$

$T_{BC} = 144.0 \text{ N}$ ◀

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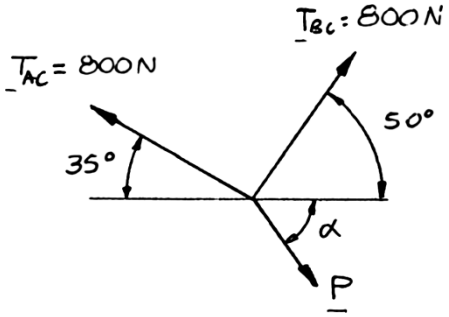


PROBLEM 2.132

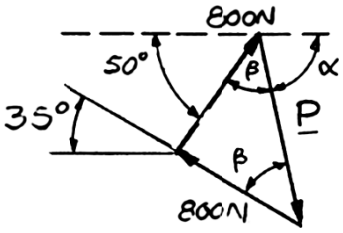
Two cables tied together at C are loaded as shown. Knowing that the maximum allowable tension in each cable is 800 N, determine (a) the magnitude of the largest force **P** that can be applied at C, (b) the corresponding value of α.

SOLUTION

Free-Body Diagram: *C*



Force Triangle



Force triangle is isosceles with

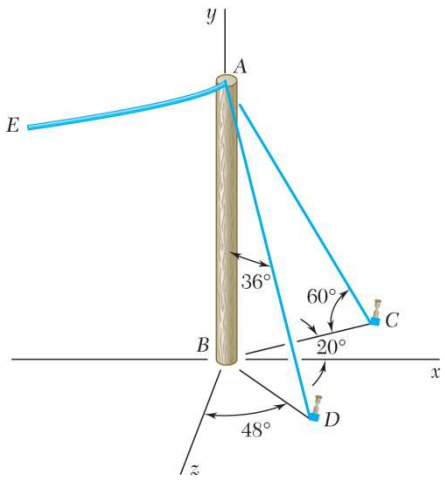
$$2\beta = 180° - 85°$$
$$\beta = 47.5°$$

(a) $$P = 2(800\text{ N})\cos 47.5° = 1081\text{ N}$$

Since $P > 0$, the solution is correct. $P = 1081\text{ N}$ ◀

(b) $\alpha = 180° - 50° - 47.5° = 82.5°$ $\alpha = 82.5°$ ◀

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PROBLEM 2.133

The end of the coaxial cable AE is attached to the pole AB, which is strengthened by the guy wires AC and AD. Knowing that the tension in wire AC is 120 lb, determine (*a*) the components of the force exerted by this wire on the pole, (*b*) the angles θ_x, θ_y, and θ_z that the force forms with the coordinate axes.

SOLUTION

(*a*)

$$F_x = (120 \text{ lb})\cos 60° \cos 20°$$

$$F_x = 56.382 \text{ lb} \qquad F_x = +56.4 \text{ lb} \blacktriangleleft$$

$$F_y = -(120 \text{ lb})\sin 60°$$

$$F_y = -103.923 \text{ lb} \qquad F_y = -103.9 \text{ lb} \blacktriangleleft$$

$$F_z = -(120 \text{ lb})\cos 60° \sin 20°$$

$$F_z = -20.521 \text{ lb} \qquad F_z = -20.5 \text{ lb} \blacktriangleleft$$

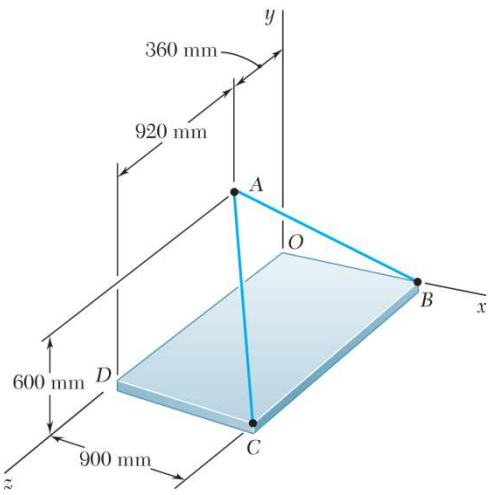
(*b*)

$$\cos\theta_x = \frac{F_x}{F} = \frac{56.382 \text{ lb}}{120 \text{ lb}} \qquad \theta_x = 62.0° \blacktriangleleft$$

$$\cos\theta_y = \frac{F_y}{F} = \frac{-103.923 \text{ lb}}{120 \text{ lb}} \qquad \theta_y = 150.0° \blacktriangleleft$$

$$\cos\theta_z = \frac{F_z}{F} = \frac{-20.52 \text{ lb}}{120 \text{ lb}} \qquad \theta_z = 99.8° \blacktriangleleft$$

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PROBLEM 2.134

Knowing that the tension in cable AC is 2130 N, determine the components of the force exerted on the plate at C.

SOLUTION

$$\overrightarrow{CA} = -(900\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j} - (920\text{ mm})\mathbf{k}$$

$$CA = \sqrt{(900\text{ mm})^2 + (600\text{ mm})^2 + (920\text{ mm})^2}$$

$$= 1420\text{ mm}$$

$$\mathbf{T}_{CA} = T_{CA}\boldsymbol{\lambda}_{CA}$$

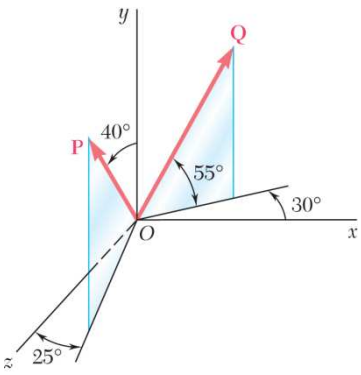
$$= T_{CA}\frac{\overrightarrow{CA}}{CA}$$

$$\mathbf{T}_{CA} = \frac{2130\text{ N}}{1420\text{ mm}}[-(900\text{ mm})\mathbf{i} + (600\text{ mm})\mathbf{j} - (920\text{ mm})\mathbf{k}]$$

$$= -(1350\text{ N})\mathbf{i} + (900\text{ N})\mathbf{j} - (1380\text{ N})\mathbf{k}$$

$$(T_{CA})_x = -1350\text{ N}, \quad (T_{CA})_y = 900\text{ N}, \quad (T_{CA})_z = -1380\text{ N} \blacktriangleleft$$

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PROBLEM 2.135

Find the magnitude and direction of the resultant of the two forces shown knowing that $P = 600$ N and $Q = 450$ N.

SOLUTION

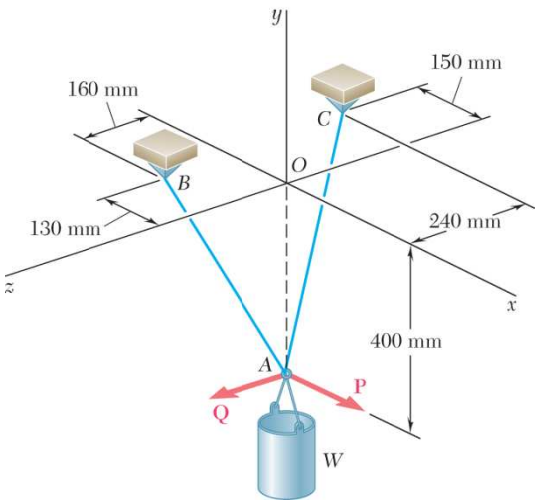
$$\mathbf{P} = (600\text{ N})[\sin 40^\circ \sin 25^\circ \mathbf{i} + \cos 40^\circ \mathbf{j} + \sin 40^\circ \cos 25^\circ \mathbf{k}]$$
$$= (162.992\text{ N})\mathbf{i} + (459.63\text{ N})\mathbf{j} + (349.54\text{ N})\mathbf{k}$$
$$\mathbf{Q} = (450\text{ N})[\cos 55^\circ \cos 30^\circ \mathbf{i} + \sin 55^\circ \mathbf{j} - \cos 55^\circ \sin 30^\circ \mathbf{k}]$$
$$= (223.53\text{ N})\mathbf{i} + (368.62\text{ N})\mathbf{j} - (129.055\text{ N})\mathbf{k}$$
$$\mathbf{R} = \mathbf{P} + \mathbf{Q}$$
$$= (386.52\text{ N})\mathbf{i} + (828.25\text{ N})\mathbf{j} + (220.49\text{ N})\mathbf{k}$$
$$R = \sqrt{(386.52\text{ N})^2 + (828.25\text{ N})^2 + (220.49\text{ N})^2}$$
$$= 940.22\text{ N} \qquad R = 940\text{ N} \blacktriangleleft$$

$$\cos\theta_x = \frac{R_x}{R} = \frac{386.52\text{ N}}{940.22\text{ N}} \qquad \theta_x = 65.7^\circ \blacktriangleleft$$

$$\cos\theta_y = \frac{R_y}{R} = \frac{828.25\text{ N}}{940.22\text{ N}} \qquad \theta_y = 28.2^\circ \blacktriangleleft$$

$$\cos\theta_z = \frac{R_z}{R} = \frac{220.49\text{ N}}{940.22\text{ N}} \qquad \theta_z = 76.4^\circ \blacktriangleleft$$

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PROBLEM 2.136

A container of weight W is suspended from ring A. Cable BAC passes through the ring and is attached to fixed supports at B and C. Two forces $\mathbf{P} = P\mathbf{i}$ and $\mathbf{Q} = Q\mathbf{k}$ are applied to the ring to maintain the container in the position shown. Knowing that $W = 376$ N, determine P and Q. (*Hint:* The tension is the same in both portions of cable BAC.)

SOLUTION

$$\mathbf{T}_{AB} = T\boldsymbol{\lambda}_{AB}$$

$$= T\frac{\overrightarrow{AB}}{AB}$$

$$= T\frac{(-130\text{ mm})\mathbf{i} + (400\text{ mm})\mathbf{j} + (160\text{ mm})\mathbf{k}}{450\text{ mm}}$$

$$= T\left(-\frac{13}{45}\mathbf{i} + \frac{40}{45}\mathbf{j} + \frac{16}{45}\mathbf{k}\right)$$

$$\mathbf{T}_{AC} = T\boldsymbol{\lambda}_{AC}$$

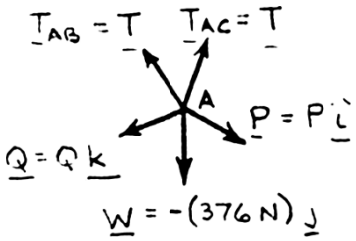
$$= T\frac{\overrightarrow{AC}}{AC}$$

$$= T\frac{(-150\text{ mm})\mathbf{i} + (400\text{ mm})\mathbf{j} + (-240\text{ mm})\mathbf{k}}{490\text{ mm}}$$

$$= T\left(-\frac{15}{49}\mathbf{i} + \frac{40}{49}\mathbf{j} - \frac{24}{49}\mathbf{k}\right)$$

$$\Sigma F = 0: \quad \mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{Q} + \mathbf{P} + \mathbf{W} = 0$$

Free-Body *A*:



Setting coefficients of **i**, **j**, **k** equal to zero:

$$\mathbf{i}: \quad -\frac{13}{45}T - \frac{15}{49}T + P = 0 \qquad 0.59501T = P \tag{1}$$

$$\mathbf{j}: \quad +\frac{40}{45}T + \frac{40}{49}T - W = 0 \qquad 1.70521T = W \tag{2}$$

$$\mathbf{k}: \quad +\frac{16}{45}T - \frac{24}{49}T + Q = 0 \qquad 0.134240T = Q \tag{3}$$

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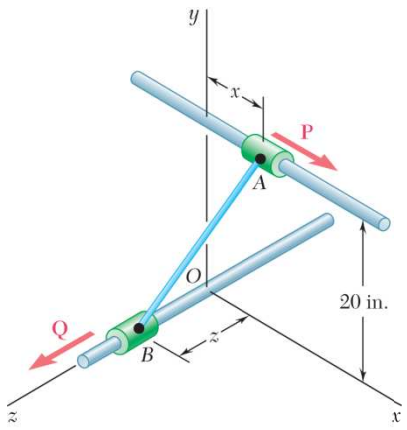
PROBLEM 2.136 (Continued)

Data: $W = 376$ N $\quad 1.70521T = 376$ N $\quad T = 220.50$ N

$0.59501(220.50 \text{ N}) = P$ $\qquad P = 131.2$ N ◀

$0.134240(220.50 \text{ N}) = Q$ $\qquad Q = 29.6$ N ◀

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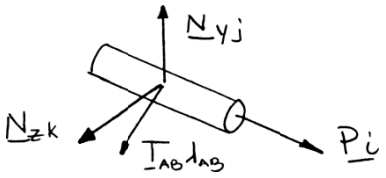
PROBLEM 2.137

Collars A and B are connected by a 25-in.-long wire and can slide freely on frictionless rods. If a 60-lb force **Q** is applied to collar B as shown, determine (*a*) the tension in the wire when $x = 9$ in., (*b*) the corresponding magnitude of the force **P** required to maintain the equilibrium of the system.

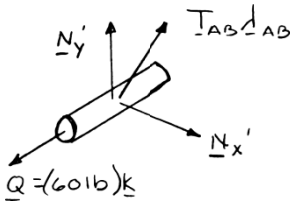
SOLUTION

Free-Body Diagrams of Collars:

***A*:**



***B*:**



$$\boldsymbol{\lambda}_{AB} = \frac{\overrightarrow{AB}}{AB} = \frac{-x\mathbf{i} - (20 \text{ in.})\mathbf{j} + z\mathbf{k}}{25 \text{ in.}}$$

Collar A: $\quad \Sigma\mathbf{F} = 0: \quad P\mathbf{i} + N_y\mathbf{j} + N_z\mathbf{k} + T_{AB}\boldsymbol{\lambda}_{AB} = 0$

Substitute for $\boldsymbol{\lambda}_{AB}$ and set coefficient of **i** equal to zero:

$$P - \frac{T_{AB}x}{25 \text{ in.}} = 0 \tag{1}$$

Collar B: $\quad \Sigma\mathbf{F} = 0: \quad (60 \text{ lb})\mathbf{k} + N'_x\mathbf{i} + N'_y\mathbf{j} - T_{AB}\boldsymbol{\lambda}_{AB} = 0$

Substitute for $\boldsymbol{\lambda}_{AB}$ and set coefficient of **k** equal to zero:

$$60 \text{ lb} - \frac{T_{AB}z}{25 \text{ in.}} = 0 \tag{2}$$

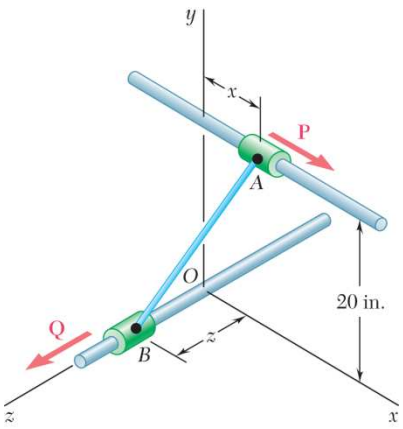
(*a*) $\quad x = 9$ in. $\quad (9 \text{ in.})^2 + (20 \text{ in.})^2 + z^2 = (25 \text{ in.})^2$

$$z = 12 \text{ in.}$$

From Eq. (2): $\quad \dfrac{60 \text{ lb} - T_{AB}(12 \text{ in.})}{25 \text{ in.}}$ $\qquad T_{AB} = 125.0 \text{ lb}$ ◀

(*b*) From Eq. (1): $\quad P = \dfrac{(125.0 \text{ lb})(9 \text{ in.})}{25 \text{ in.}}$ $\qquad P = 45.0 \text{ lb}$ ◀

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PROBLEM 2.138

Collars A and B are connected by a 25-in.-long wire and can slide freely on frictionless rods. Determine the distances x and z for which the equilibrium of the system is maintained when $P = 120$ lb and $Q = 60$ lb.

SOLUTION

See Problem 2.137 for the diagrams and analysis leading to Equations (1) and (2) below:

$$P = \frac{T_{AB}x}{25 \text{ in.}} = 0 \tag{1}$$

$$60 \text{ lb} - \frac{T_{AB}z}{25 \text{ in.}} = 0 \tag{2}$$

For $P = 120$ lb, Eq. (1) yields $T_{AB}x = (25 \text{ in.})(20 \text{ lb})$ (1′)

From Eq. (2): $T_{AB}z = (25 \text{ in.})(60 \text{ lb})$ (2′)

Dividing Eq. (1′) by (2′), $\frac{x}{z} = 2$ (3)

Now write $x^2 + z^2 + (20 \text{ in.})^2 = (25 \text{ in.})^2$ (4)

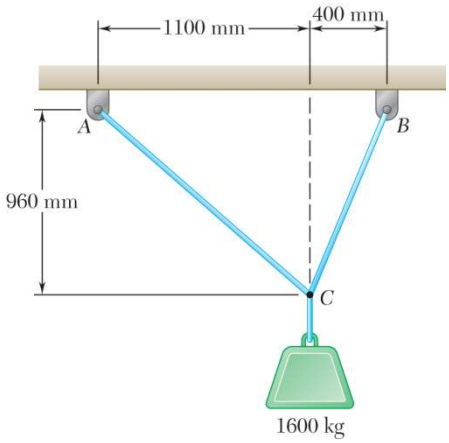
Solving (3) and (4) simultaneously,

$$4z^2 + z^2 + 400 = 625$$
$$z^2 = 45$$
$$z = 6.7082 \text{ in.}$$

From Eq. (3): $x = 2z = 2(6.7082 \text{ in.})$
$= 13.4164 \text{ in.}$

$$x = 13.42 \text{ in.}, \quad z = 6.71 \text{ in.} \blacktriangleleft$$

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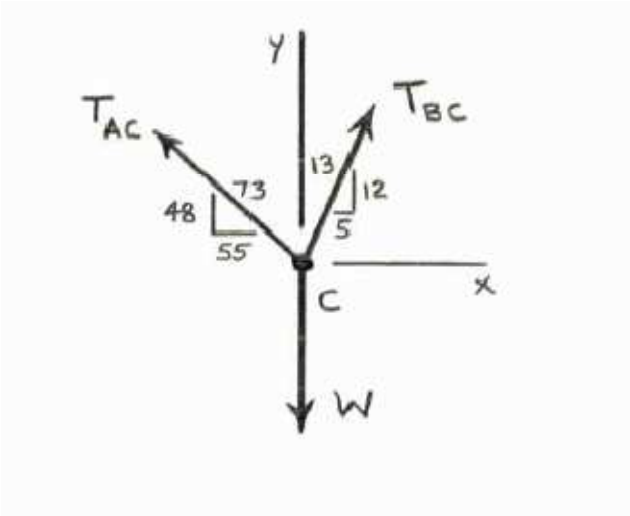


PROBLEM 2F1

Two cables are tied together at C and loaded as shown. Draw the free-body diagram needed to determine the tension in AC and BC.

SOLUTION

Free-Body Diagram of Point *C*:

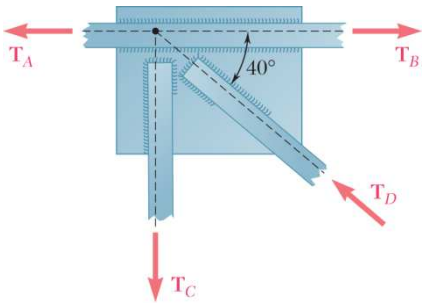


$W = (1600 \text{ kg})(9.81 \text{ m/s}^2)$

$W = 15.6960(10^3) \text{ N}$

$W = 15.696 \text{ kN}$

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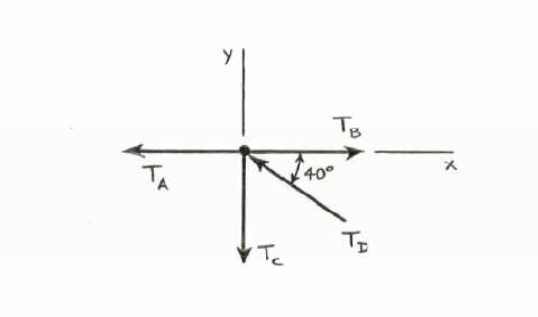


PROBLEM 2.F2

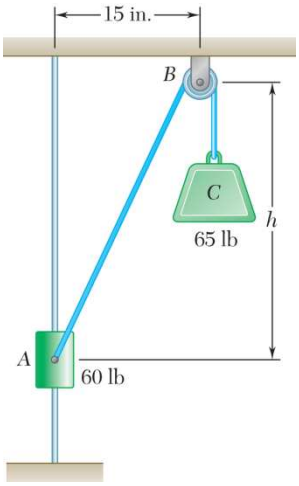
Two forces of magnitude T_A = 8 kips and T_B = 15 kips are applied as shown to a welded connection. Knowing that the connection is in equilibrium, draw the free-body diagram needed to determine the magnitudes of the forces T_C and T_D.

SOLUTION

Free-Body Diagram of Point *E*:



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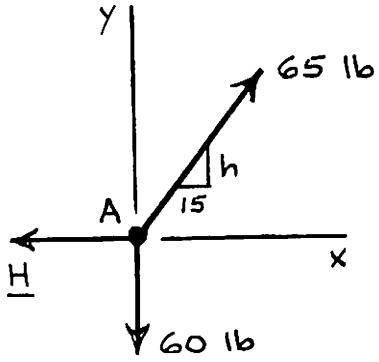


PROBLEM 2.F3

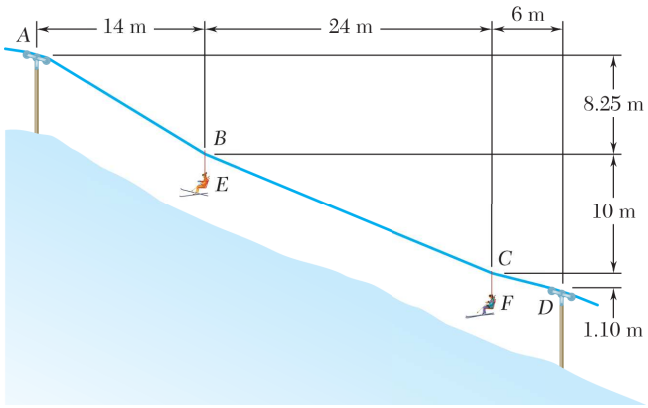
The 60-lb collar *A* can slide on a frictionless vertical rod and is connected as shown to a 65-lb counterweight *C*. Draw the free-body diagram needed to determine the value of *h* for which the system is in equilibrium.

SOLUTION

Free-Body Diagram of Point *A*:



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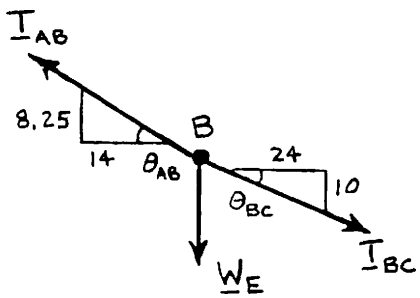


PROBLEM 2.F4

A chairlift has been stopped in the position shown. Knowing that each chair weighs 250 N and that the skier in chair E weighs 765 N, draw the free-body diagrams needed to determine the weight of the skier in chair F.

SOLUTION

Free-Body Diagram of Point *B*:



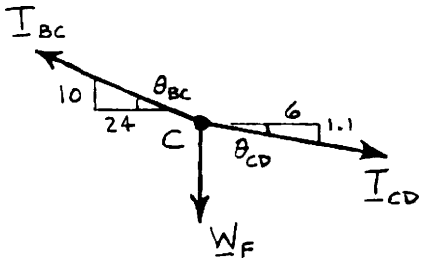
$$W_E = 250\text{ N} + 765\text{ N} = 1015\text{ N}$$

$$\theta_{AB} = \tan^{-1}\frac{8.25}{14} = 30.510°$$

$$\theta_{BC} = \tan^{-1}\frac{10}{24} = 22.620°$$

Use this free body to determine T_{AB} and T_{BC}.

Free-Body Diagram of Point *C*:



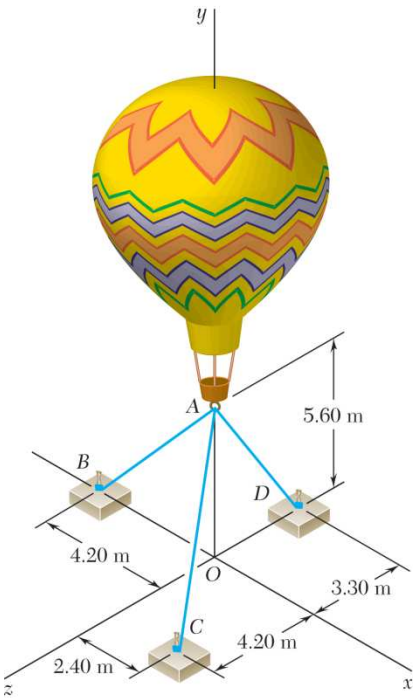
$$\theta_{CD} = \tan^{-1}\frac{1.1}{6} = 10.3889°$$

Use this free body to determine T_{CD} and W_F.

Then weight of skier W_S is found by

$$W_S = W_F - 250\text{ N} \blacktriangleleft$$

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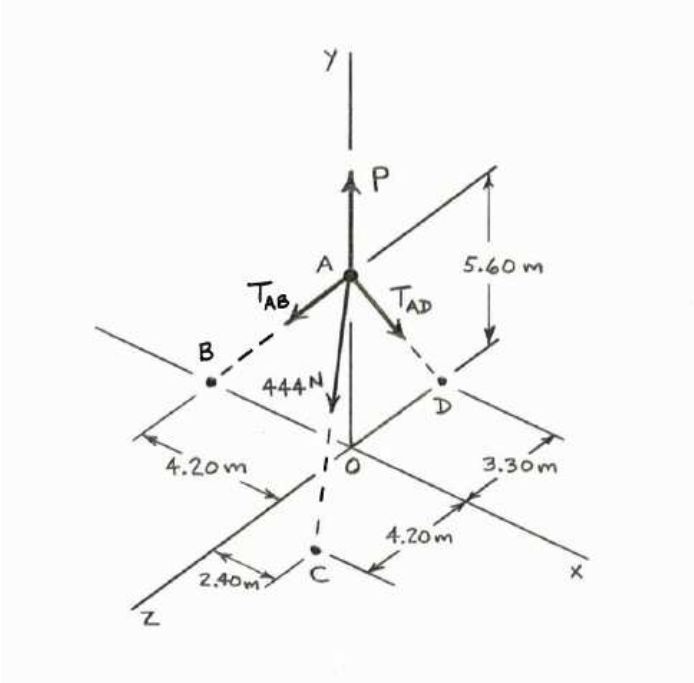


PROBLEM 2.F5

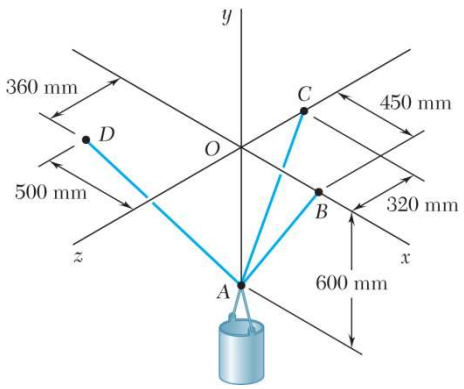
Three cables are used to tether a balloon as shown. Knowing that the tension in cable AC is 444 N, draw the free-body diagram needed to determine the vertical force **P** exerted by the balloon at A.

SOLUTION

Free-Body Diagram of Point A:



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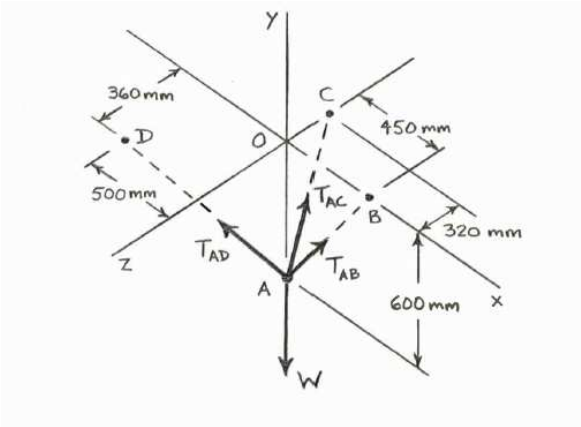


PROBLEM 2.F6

A container of mass m = 120 kg is supported by three cables as shown. Draw the free-body diagram needed to determine the tension in each cable

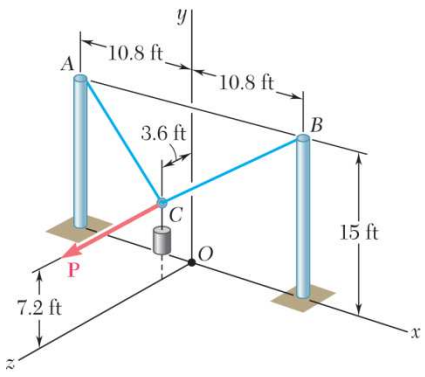
SOLUTION

Free-Body Diagram of Point *A*:



$$W = (120\text{ kg})(9.81\text{ m/s}^2)$$
$$= 1177.2\text{ N}$$

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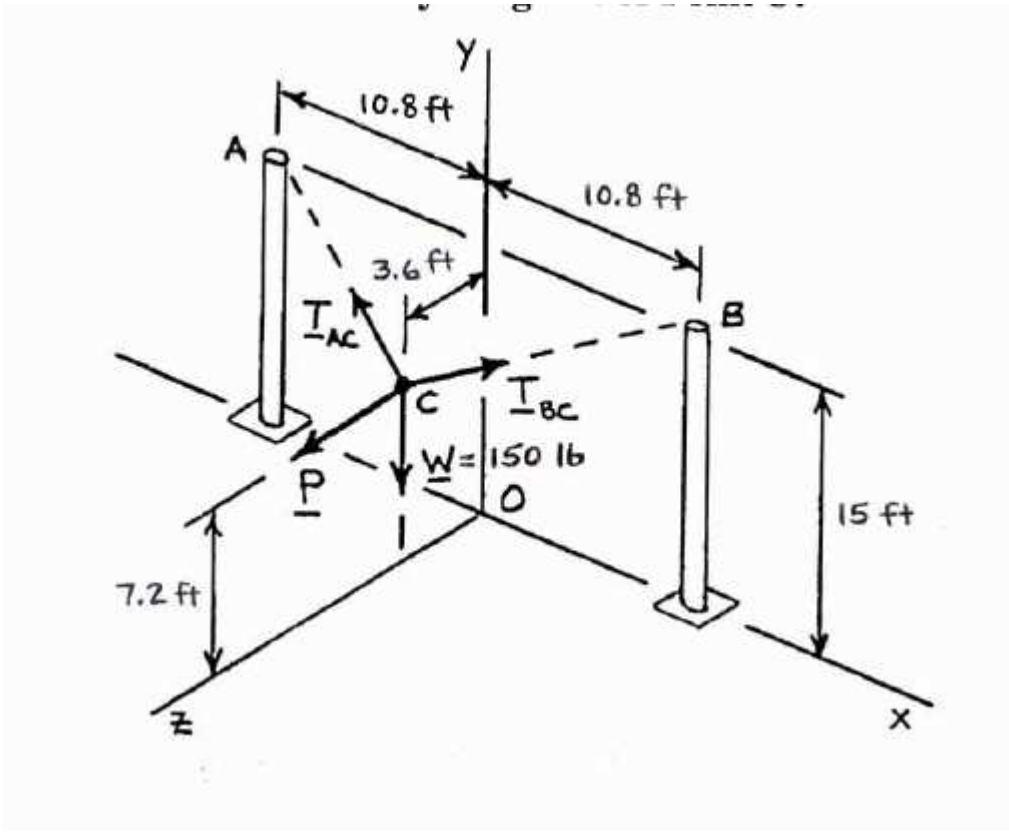


PROBLEM 2.F7

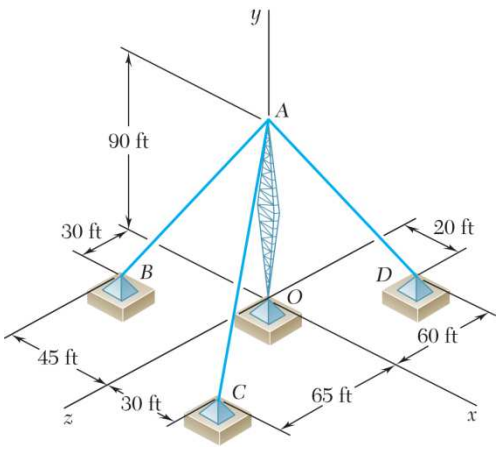
A 150-lb cylinder is supported by two cables *AC* and *BC* that are attached to the top of vertical posts. A horizontal force **P**, which is perpendicular to the plane containing the posts, holds the cylinder in the position shown. Draw the free-body diagram needed to determine the magnitude of **P** and the force in each cable.

SOLUTION

Free-Body Diagram of Point *C*:



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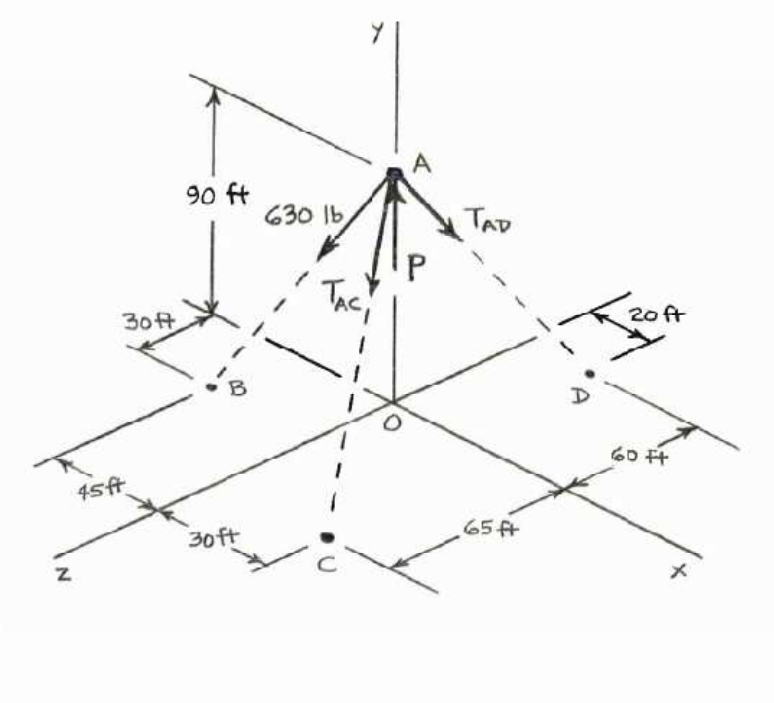


PROBLEM 2.F8

A transmission tower is held by three guy wires attached to a pin at *A* and anchored by bolts at *B*, *C*, and *D*. Knowing that the tension in wire *AB* is 630 lb, draw the free-body diagram needed to determine the vertical force **P** exerted by the tower on the pin at *A*.

SOLUTION

Free-Body Diagram of point *A*:



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