Algebra and Trigonometry 11th edition Sullivan Solutions Manual

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Chapter 1

Equations and Inequalities

Section 1.1

1. Distributive

2. Zero-Product

3. $\{x \mid x \neq 4\}$

4. False. Multiplying both sides of an equation by zero will not result in an equivalent equation.

5. identity

6. linear; first-degree

7. False. The solution is $\frac{8}{3}$.

8. True

9. b

10. d

11. $7x = 21$

$\frac{7x}{7} = \frac{21}{7}$

$x = 3$

The solution set is $\{3\}$.

12. $6x = -24$

$\frac{6x}{6} = \frac{-24}{6}$

$x = -4$

The solution set is $\{-4\}$.

13. $3x + 15 = 0$

$3x + 15 - 15 = 0 - 15$

$3x = -15$

$\frac{3x}{3} = \frac{-15}{3}$

$x = -5$

The solution set is $\{-5\}$.

14. $6x + 18 = 0$

$6x + 18 - 18 = 0 - 18$

$6x = -18$

$\frac{6x}{6} = \frac{-18}{6}$

$x = -3$

The solution set is $\{-3\}$.

15. $2x - 3 = 0$

$2x - 3 + 3 = 0 + 3$

$2x = 3$

$\frac{2x}{2} = \frac{3}{2}$

$x = \frac{3}{2}$

The solution set is $\left\{\frac{3}{2}\right\}$.

16. $3x + 4 = 0$

$3x + 4 - 4 = 0 - 4$

$3x = -4$

$\frac{3x}{3} = \frac{-4}{3}$

$x = -\frac{4}{3}$

The solution set is $\left\{-\frac{4}{3}\right\}$.

17. $\frac{1}{4}x = \frac{7}{20}$

$4\left(\frac{1}{4}x\right) = 4\left(\frac{7}{20}\right)$

$x = \frac{28}{20} = \frac{7}{5}$

The solution set is $\left\{\frac{7}{5}\right\}$.

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18. $\frac{2}{3}x = \frac{9}{2}$

$6\left(\frac{2}{3}x\right) = 6\left(\frac{9}{2}\right)$

$4x = 27$

$\frac{4x}{4} = \frac{27}{4}$

$x = \frac{27}{4}$

The solution set is $\left\{\frac{27}{4}\right\}$.

19. $3x + 4 = x$

$3x + 4 - 4 = x - 4$

$3x = x - 4$

$3x - x = x - 4 - x$

$2x = -4$

$\frac{2x}{2} = \frac{-4}{2}$

$x = -2$

The solution set is $\{-2\}$.

20. $2x + 9 = 5x$

$2x + 9 - 9 = 5x - 9$

$2x = 5x - 9$

$2x - 5x = 5x - 9 - 5x$

$-3x = -9$

$\frac{-3x}{-3} = \frac{-9}{-3}$

$x = 3$

The solution set is $\{3\}$.

21. $2t - 6 = 3 - t$

$2t - 6 + 6 = 3 - t + 6$

$2t = 9 - t$

$2t + t = 9 - t + t$

$3t = 9$

$\frac{3t}{3} = \frac{9}{3}$

$t = 3$

The solution set is $\{3\}$.

22. $5y + 6 = -18 - y$

$5y + 6 - 6 = -18 - y - 6$

$5y = -y - 24$

$5y + y = -y - 24 + y$

$6y = -24$

$\frac{6y}{6} = \frac{-24}{6}$

$y = -4$

The solution set is $\{-4\}$.

23. $6 - x = 2x + 9$

$6 - x - 6 = 2x + 9 - 6$

$-x = 2x + 3$

$-x - 2x = 2x + 3 - 2x$

$-3x = 3$

$\frac{-3x}{-3} = \frac{3}{-3}$

$x = -1$

The solution set is $\{-1\}$.

24. $3 - 2x = 2 - x$

$3 - 2x - 3 = 2 - x - 3$

$-2x = -x - 1$

$-2x + x = -x - 1 + x$

$-x = -1$

$\frac{-x}{-1} = \frac{-1}{-1}$

$x = 1$

The solution set is $\{1\}$.

25. $3 + 2n = 4n + 7$

$3 + 2n - 3 = 4n + 7 - 3$

$2n = 4n + 4$

$2n - 4n = 4n + 4 - 4n$

$-2n = 4$

$\frac{-2n}{-2} = \frac{4}{-2}$

$n = -2$

The solution set is $\{-2\}$.

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26. $6-2m=3m+1$

$6-2m-6=3m+1-6$

$-2m=3m-5$

$-2m-3m=3m-5-3m$

$-5m=-5$

$\frac{-5m}{-5}=\frac{-5}{-5}$

$m=1$

The solution set is $\{1\}$.

27. $3(5+3x)=8(x-1)$

$15+9x=8x-8$

$9x-8x+15=8x-8x-8$

$x+15-15=-8-15$

$x=-23$

The solution set is $\{-23\}$.

28. $3(2-x)=2x-1$

$6-3x=2x-1$

$6-3x-6=2x-1-6$

$-3x=2x-7$

$-3x-2x=2x-7-2x$

$-5x=-7$

$\frac{-5x}{-5}=\frac{-7}{-5}$

$x=\frac{7}{5}$

The solution set is $\left\{\frac{7}{5}\right\}$.

29. $8x-(3x+2)=3x-10$

$8x-3x-2=3x-10$

$5x-2=3x-10$

$5x-2+2=3x-10+2$

$5x=3x-8$

$5x-3x=3x-8-3x$

$2x=-8$

$\frac{2x}{2}=\frac{-8}{2}$

$x=-4$

The solution set is $\{-4\}$.

30. $7-(2x-1)=10$

$7-2x+1=10$

$8-2x=10$

$8-2x-8=10-8$

$-2x=2$

$\frac{-2x}{-2}=\frac{2}{-2}$

$x=-1$

The solution set is $\{-1\}$.

31. $\frac{3}{2}x+2=\frac{1}{2}-\frac{1}{2}x$

$2\left(\frac{3}{2}x+2\right)=2\left(\frac{1}{2}-\frac{1}{2}x\right)$

$3x+4=1-x$

$3x+4-4=1-x-4$

$3x=-3-x$

$3x+x=-3-x+x$

$4x=-3$

$\frac{4x}{4}=\frac{-3}{4}$

$x=-\frac{3}{4}$

The solution set is $\left\{-\frac{3}{4}\right\}$.

32. $\frac{1}{3}x=2-\frac{2}{3}x$

$3\left(\frac{1}{3}x\right)=3\left(2-\frac{2}{3}x\right)$

$x=6-2x$

$x+2x=6-2x+2x$

$3x=6$

$\frac{3x}{3}=\frac{6}{3}$

$x=2$

The solution set is $\{2\}$.

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33.
$$\frac{1}{2}x-5=\frac{3}{4}x$$
$$4\left(\frac{1}{2}x-5\right)=4\left(\frac{3}{4}x\right)$$
$$2x-20=3x$$
$$2x-20-2x=3x-2x$$
$$-20=x$$
$$x=-20$$
The solution set is $\{-20\}$.

34.
$$1-\frac{1}{2}x=6$$
$$2\left(1-\frac{1}{2}x\right)=2(6)$$
$$2-x=12$$
$$2-x-2=12-2$$
$$-x=10$$
$$\frac{-x}{-1}=\frac{10}{-1}$$
$$x=-10$$
The solution set is $\{-10\}$.

35.
$$\frac{2}{3}p=\frac{1}{2}p+\frac{1}{3}$$
$$6\left(\frac{2}{3}p\right)=6\left(\frac{1}{2}p+\frac{1}{3}\right)$$
$$4p=3p+2$$
$$4p-3p=3p+2-3p$$
$$p=2$$
The solution set is $\{2\}$.

36.
$$\frac{1}{2}-\frac{1}{3}p=\frac{4}{3}$$
$$6\left(\frac{1}{2}-\frac{1}{3}p\right)=6\left(\frac{4}{3}\right)$$
$$3-2p=8$$
$$3-2p-3=8-3$$
$$-2p=5$$
$$\frac{-2p}{-2}=\frac{5}{-2}$$
$$p=-\frac{5}{2}$$
The solution set is $\left\{-\frac{5}{2}\right\}$.

37.
$$0.2m=0.9+0.5m$$
$$0.2m-0.5m=0.9+0.5m-0.5m$$
$$-0.3m=0.9$$
$$\frac{-0.3m}{-0.3}=\frac{0.9}{-0.3}$$
$$m=-3$$
The solution set is $\{-3\}$.

38.
$$0.9t=1+t$$
$$0.9t-t=1+t-t$$
$$-0.1t=1$$
$$\frac{-0.1t}{-0.1}=\frac{1}{-0.1}$$
$$t=-10$$
The solution set is $\{-10\}$.

39.
$$\frac{x+1}{3}+\frac{x+2}{7}=2$$
$$21\left(\frac{x+1}{3}+\frac{x+2}{7}\right)=21(2)$$
$$7(x+1)+(3)(x+2)=42$$
$$7x+7+3x+6=42$$
$$10x+13=42$$
$$10x+13-13=42-13$$
$$10x=29$$
$$\frac{10x}{10}=\frac{29}{10}$$
$$x=\frac{29}{10}$$
The solution set is $\left\{\frac{29}{10}\right\}$.

40.
$$\frac{2x+1}{3}+16=3x$$
$$3\left(\frac{2x+1}{3}+16\right)=3(3x)$$
$$2x+1+48=9x$$
$$2x+49=9x$$
$$2x+49-2x=9x-2x$$
$$49=7x$$
$$\frac{49}{7}=\frac{7x}{7}$$
$$x=7$$
The solution set is $\{7\}$.

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41. $\frac{5}{8}(p+3)-2=\frac{1}{4}(2p-3)+\frac{11}{16}$

$10(p+3)-32=4(2p-3)+11$

$10p+30-32=8p-12+11$

$10p-2=8p-1$

$10p-8p-2=8p-8p-1$

$2p-2+2=-1+2$

$2p=1$

$\frac{2}{2}p=\frac{1}{2}$

$p=\frac{1}{2}$

The solution set is $\left\{\frac{1}{2}\right\}$.

42. $\frac{1}{3}(w+1)-3=\frac{2}{5}(w-4)-\frac{2}{15}$

$5(w+1)-45=6(w-4)-2$

$5w+5-45=6w-24-2$

$5w-40=6w-26$

$5w-6w-40=6w-6w-26$

$-w-40+40=-26+40$

$-w=14$

$\frac{-1}{-1}w=14$

$w=-14$

The solution set is $\{-14\}$.

43. $\frac{2}{y}+\frac{4}{y}=3$

$y\left(\frac{2}{y}+\frac{4}{y}\right)=y(3)$

$2+4=3y$

$6=3y$

$\frac{6}{3}=\frac{3y}{3}$

$2=y$

Since $y=2$ does not cause a denominator to equal zero, the solution set is $\{2\}$.

44. $\frac{4}{y}-5=\frac{5}{2y}$

$2y\left(\frac{4}{y}-5\right)=2y\left(\frac{5}{2y}\right)$

$8-10y=5$

$8-10y-8=5-8$

$-10y=-3$

$\frac{-10y}{-10}=\frac{-3}{-10}$

$y=\frac{3}{10}$

Since $y=\frac{3}{10}$ does not cause a denominator to equal zero, the solution set is $\left\{\frac{3}{10}\right\}$.

45. $\frac{1}{2}+\frac{2}{x}=\frac{3}{4}$

$4x\left(\frac{1}{2}+\frac{2}{x}\right)=4x\left(\frac{3}{4}\right)$

$2x+8=3x$

$2x+8-2x=3x-2x$

$8=x$

Since $x=8$ does not cause any denominator to equal zero, the solution set is $\{8\}$.

46. $\frac{3}{x}-\frac{1}{3}=\frac{1}{6}$

$6x\left(\frac{3}{x}-\frac{1}{3}\right)=6x\left(\frac{1}{6}\right)$

$18-2x=x$

$18-2x+2x=x+2x$

$18=3x$

$\frac{18}{3}=\frac{3x}{3}$

$6=x$

Since $x=6$ does not cause a denominator to equal zero, the solution set is $\{6\}$.

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47.
$$(x+7)(x-1)=(x+1)^2$$
$$x^2+6x-7=x^2+2x+1$$
$$x^2+6x-7-x^2=x^2+2x+1-x^2$$
$$6x-7=2x+1$$
$$6x-7+7=2x+1+7$$
$$6x=2x+8$$
$$6x-2x=2x+8-2x$$
$$4x=8$$
$$\frac{4x}{4}=\frac{8}{4}$$
$$x=2$$
The solution set is $\{2\}$.

48.
$$(x+2)(x-3)=(x+3)^2$$
$$x^2-x-6=x^2+6x+9$$
$$x^2-x-6-x^2=x^2+6x+9-x^2$$
$$-x-6=6x+9$$
$$-x-6+6=6x+9+6$$
$$-x=6x+15$$
$$-x-6x=6x+15-6x$$
$$-7x=15$$
$$\frac{-7x}{-7}=\frac{15}{-7}$$
$$x=-\frac{15}{7}$$
The solution set is $\left\{-\frac{15}{7}\right\}$.

49.
$$x(2x-3)=(2x+1)(x-4)$$
$$2x^2-3x=2x^2-7x-4$$
$$2x^2-3x-2x^2=2x^2-7x-4-2x^2$$
$$-3x=-7x-4$$
$$-3x+7x=-7x-4+7x$$
$$4x=-4$$
$$\frac{4x}{4}=\frac{-4}{4}$$
$$x=-1$$
The solution set is $\{-1\}$.

50.
$$x(1+2x)=(2x-1)(x-2)$$
$$x+2x^2=2x^2-5x+2$$
$$x+2x^2-2x^2=2x^2-5x+2-2x^2$$
$$x=-5x+2$$
$$x+5x=-5x+2+5x$$
$$6x=2$$
$$\frac{6x}{6}=\frac{2}{6}\Rightarrow x=\frac{1}{3}$$
The solution set is $\left\{\frac{1}{3}\right\}$.

51.
$$p\left(p^2+3\right)=12+p^3$$
$$p^3+3p=12+p^3$$
$$p^3-p^3+3p=12+p^3-p^3$$
$$3p=12$$
$$\frac{3p}{3}=\frac{12}{3}\Rightarrow p=4$$
The solution set is $\{4\}$.

52.
$$w(4-w^2)=8-w^3$$
$$4w-w^3=8-w^3$$
$$4w-w^3+w^3=8-w^3+w^3$$
$$4w=8$$
$$\frac{4w}{4}=\frac{8}{4}$$
$$w=2$$
The solution set is $\{2\}$.

53.
$$\frac{x}{x-2}+3=\frac{2}{x-2}$$
$$\left(\frac{x}{x-2}+3\right)(x-2)=\left(\frac{2}{x-2}\right)(x-2)$$
$$x+3(x-2)=2$$
$$x+3x-6=2$$
$$4x-6=2$$
$$4x-6+6=2+6$$
$$4x=8$$
$$\frac{4x}{4}=\frac{8}{4}$$
$$x=2$$
Since $x=2$ causes a denominator to equal zero, we must discard it. Therefore the original equation has no solution.

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54.
$$\frac{2x}{x+3}=\frac{-6}{x+3}-2$$
$$\left(\frac{2x}{x+3}\right)(x+3)=\left(\frac{-6}{x+3}-2\right)(x+3)$$
$$2x=-6-(2)(x+3)$$
$$2x=-6-2x-6$$
$$2x=-12-2x$$
$$2x+2x=-12-2x+2x$$
$$4x=-12$$
$$\frac{4x}{4}=\frac{-12}{4}$$
$$x=-3$$

Since $x = -3$ causes a denominator to equal zero, we must discard it. Therefore the original equation has no solution.

55.
$$\frac{2x}{x^2-4}=\frac{4}{x^2-4}-\frac{3}{x+2}$$
$$\frac{2x}{(x+2)(x-2)}=\frac{4}{(x+2)(x-2)}-\frac{3}{x+2}$$
$$\left(\frac{2x}{(x+2)(x-2)}\right)(x+2)(x-2)=\left(\frac{4}{(x+2)(x-2)}-\frac{3}{x+2}\right)(x+2)(x-2)$$
$$2x=4-3(x-2)$$
$$2x=4-3x+6$$
$$2x=10-3x$$
$$2x+3x=10-3x+3x$$
$$5x=10$$
$$\frac{5x}{5}=\frac{10}{5}$$
$$x=2$$

Since $x = 2$ causes a denominator to equal zero, we must discard it. Therefore the original equation has no solution.

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56.
$$\frac{x}{x^2-9}+\frac{4}{x+3}=\frac{3}{x^2-9}$$
$$\frac{x}{(x+3)(x-3)}+\frac{4}{x+3}=\frac{3}{(x+3)(x-3)}$$
$$\left(\frac{x}{(x+3)(x-3)}+\frac{4}{x+3}\right)(x+3)(x-3)=\left(\frac{3}{(x+3)(x-3)}\right)(x+3)(x-3)$$
$$x+4(x-3)=3$$
$$x+4x-12=3$$
$$5x-12=3$$
$$5x-12+12=3+12$$
$$5x=15$$
$$\frac{5x}{5}=\frac{15}{5}$$
$$x=3$$
Since $x = 3$ causes a denominator to equal zero, we must discard it. Therefore the original equation has no solution.

57.
$$\frac{x}{x+2}=\frac{3}{2}$$
$$2(x+2)\left(\frac{x}{x+2}\right)=2(x+2)\left(\frac{3}{2}\right)$$
$$2x=3(x+2)$$
$$2x=3x+6$$
$$2x-3x=3x+6-3x$$
$$-x=6$$
$$\frac{-x}{-1}=\frac{6}{-1}$$
$$x=-6$$
Since $x = -6$ does not cause any denominator to equal zero, the solution set is $\{-6\}$.

58.
$$\frac{3x}{x-1}=2$$
$$\left(\frac{3x}{x-1}\right)(x-1)=2(x-1)$$
$$3x=2x-2$$
$$3x-2x=2x-2-2x$$
$$x=-2$$
Since $x = -2$ does not cause any denominator to equal zero, the solution set is $\{-2\}$.

59.
$$\frac{7}{3x+10}=\frac{2}{x-3}$$
$$\left(\frac{7}{3x+10}\right)(3x+10)(x-3)=\left(\frac{2}{x-3}\right)(3x+10)(x-3)$$
$$7(x-3)=2(3x+10)$$
$$7x-21=6x+20$$
$$7x-21-6x=6x+20-6x$$
$$-21+x=20$$
$$-21+x+21-25=20+21$$
$$x=41$$
Since $x = 41$ does not cause any denominator to equal zero, the solution is $\{41\}$.

60.
$$\frac{-4}{x+4}=\frac{-3}{x+6}$$
$$\left(\frac{-4}{x+4}\right)(x+6)(x+4)=\left(\frac{-3}{x+6}\right)(x+6)(x+4)$$
$$-4(x+6)=-3(x+4)$$
$$-4x-24=-3x-12$$
$$-4x-24+4x=-3x-12+4x$$
$$-24=-12+x$$
$$-24+12=-12+x+12$$
$$-12=x$$
Since $x = -12$ does not cause any denominator to equal zero, the solution set is $\{-12\}$.

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61.
$$\frac{6t+7}{4t-1}=\frac{3t+8}{2t-4}$$
$$\left(\frac{6t+7}{4t-1}\right)(4t-1)(2t-4)=\left(\frac{3t+8}{2t-4}\right)(4t-1)(2t-4)$$
$$(6t+7)(2t-4)=(3t+8)(4t-1)$$
$$12t^2-24t+14t-28=12t^2-3t+32t-8$$
$$12t^2-10t-28=12t^2+29t-8$$
$$12t^2-10t-28-12t^2=12t^2+29t-8-12t^2$$
$$-10t-28=29t-8$$
$$-10t-28-29t=29t-8-29t$$
$$-28-39t=-8$$
$$-28-39t+28=-8+28$$
$$-39t=20$$
$$\frac{-39t}{-39}=\frac{20}{-39}$$
$$t=-\frac{20}{39}$$

Since $t=-\frac{20}{39}$ does not cause any denominator to equal zero, the solution set is $\left\{-\frac{20}{39}\right\}$.

62.
$$\frac{8w+5}{10w-7}=\frac{4w-3}{5w+7}$$
$$\left(\frac{8w+5}{10w-7}\right)(10w-7)(5w+7)=\left(\frac{4w-3}{5w+7}\right)(10w-7)(5w+7)$$
$$(8w+5)(5w+7)=(4w-3)(10w-7)$$
$$40w^2+56w+25w+35=40w^2-28w-30w+21$$
$$40w^2+81w+35=40w^2-58w+21$$
$$40w^2+81w+35-40w^2=40w^2-58w+21-40w^2$$
$$81w+35=-58w+21$$
$$81w+35+58w=-58w+21+58w$$
$$139w+35=21$$
$$139w+35-35=21-35$$
$$139w=-14$$
$$\frac{139w}{139}=\frac{-14}{139}$$
$$w=-\frac{14}{139}$$

Since $w=-\frac{14}{139}$ does not cause any denominator to equal zero, the solution set is $\left\{-\frac{14}{139}\right\}$.

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63.
$$\frac{4}{x-2}=\frac{-3}{x+5}+\frac{7}{(x+5)(x-2)}$$
$$\left(\frac{4}{x-2}\right)(x+5)(x-2)=\left(\frac{-3}{x+5}+\frac{7}{(x+5)(x-2)}\right)(x+5)(x-2)$$
$$4(x+5)=-3(x-2)+7$$
$$4x+20=-3x+6+7$$
$$4x+20=-3x+13$$
$$4x+20+3x=-3x+13+3x$$
$$7x+20=13$$
$$7x+20-20=13-20$$
$$7x=-7$$
$$\frac{7x}{7}=\frac{-7}{7}$$
$$x=-1$$
Since $x=-1$ does not cause any denominator to equal zero, the solution set is $\{-1\}$.

64.
$$\frac{-4}{2x+3}+\frac{1}{x-1}=\frac{1}{(2x+3)(x-1)}$$
$$\left(\frac{-4}{2x+3}+\frac{1}{x-1}\right)(2x+3)(x-1)=\left(\frac{1}{(2x+3)(x-1)}\right)(2x+3)(x-1)$$
$$-4(x-1)+1(2x+3)=1$$
$$-4x+4+2x+3=1$$
$$-2x+7=1$$
$$-2x+7-7=1-7$$
$$-2x=-6$$
$$\frac{-2x}{-2}=\frac{-6}{-2}$$
$$x=3$$
Since $x=3$ does not cause any denominator to equal zero, the solution set is $\{3\}$.

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65.
$$\frac{2}{y+3}+\frac{3}{y-4}=\frac{5}{y+6}$$
$$\left(\frac{2}{y+3}+\frac{3}{y-4}\right)(y+3)(y-4)(y+6)=\left(\frac{5}{y+6}\right)(y+3)(y-4)(y+6)$$
$$2(y-4)(y+6)+3(y+3)(y+6)=5(y+3)(y-4)$$
$$2\left(y^2+6y-4y-24\right)+3\left(y^2+6y+3y+18\right)=5\left(y^2-4y+3y-12\right)$$
$$2\left(y^2+2y-24\right)+3\left(y^2+9y+18\right)=5\left(y^2-y-12\right)$$
$$2y^2+4y-48+3y^2+27y+54=5y^2-5y-60$$
$$5y^2+31y+6=5y^2-5y-60$$
$$5y^2+31y+6-5y^2=5y^2-5y-60-5y^2$$
$$31y+6=-5y-60$$
$$31y+6+5y=-5y-60+5y$$
$$36y+6=-60$$
$$36y+6-6=-60-6$$
$$36y=-66$$
$$\frac{36y}{36}=\frac{-66}{36}$$
$$y=-\frac{11}{6}$$

Since $y=-\frac{11}{6}$ does not cause any denominator to equal zero, the solution set is $\left\{-\frac{11}{6}\right\}$.

66.
$$\frac{5}{5z-11}+\frac{4}{2z-3}=\frac{-3}{5-z}$$
$$\left(\frac{5}{5z-11}+\frac{4}{2z-3}\right)(5z-11)(2z-3)(5-z)=\left(\frac{-3}{5-z}\right)(5z-11)(2z-3)(5-z)$$
$$5(2z-3)(5-z)+4(5z-11)(5-z)=-3(5z-11)(2z-3)$$
$$5\left(10z-2z^2-15+3z\right)+4\left(25z-5z^2-55+11z\right)=-3\left(10z^2-15z-22z+33\right)$$
$$5\left(-2z^2+13z-15\right)+4\left(-5z^2+36z-55\right)=-3\left(10z^2-37z+33\right)$$
$$-10z^2+65z-75-20z^2+144z-220=-30z^2+111z-99$$
$$-30z^2+209z-295=-30z^2+111z-99$$
$$-30z^2+209z-295+30z^2=-30z^2+111z-99+30z^2$$
$$209z-295=111z-99$$
$$209z-295-209z=111z-99-209z$$
$$-295=-98z-99$$
$$-295+99=-98z-99+99$$
$$-196=-98z$$
$$\frac{-196}{-98}=\frac{-118z}{-98}$$
$$2=z$$

Since $z=2$ does not cause any denominator to equal zero, the solution set is $\{2\}$.

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67.

$$\frac{x}{x^2-9}-\frac{x-4}{x^2+3x}=\frac{10}{x^2-3x}$$
$$\frac{x}{(x+3)(x-3)}-\frac{x-4}{x(x+3)}=\frac{10}{x(x-3)}$$
$$\left(\frac{x}{(x+3)(x-3)}-\frac{x-4}{x(x+3)}\right)x(x+3)(x-3)=\left(\frac{10}{x(x-3)}\right)x(x+3)(x-3)$$
$$(x)(x)-(x-4)(x-3)=10(x+3)$$
$$x^2-\left(x^2-3x-4x+12\right)=10x+30$$
$$x^2-\left(x^2-7x+12\right)=10x+30$$
$$x^2-x^2+7x-12=10x+30$$
$$7x-12=10x+30$$
$$7x-12+12=10x+30+12$$
$$7x=10x+42$$
$$7x-10x=10x-10x+42$$
$$-3x=42$$
$$\frac{-3x}{-3}=\frac{42}{-3}$$
$$x=-14$$

Since $x=-6$ does not cause any denominator to equal zero, the solution set is $\{-14\}$.

68.

$$\frac{x+1}{x^2+2x}-\frac{x+4}{x^2+x}=\frac{-3}{x^2+3x+2}$$
$$\frac{x+1}{x(x+2)}-\frac{x+4}{x(x+1)}=\frac{-3}{(x+2)(x+1)}$$
$$\left(\frac{x+1}{x(x+2)}-\frac{x+4}{x(x+1)}\right)x(x+2)(x+1)=\left(\frac{-3}{(x+2)(x+1)}\right)x(x+2)(x+1)$$
$$(x+1)(x+1)-(x+4)(x+2)=-3x$$
$$\left(x^2+x+x+1\right)-\left(x^2+2x+4x+8\right)=-3x$$
$$x^2+2x+1-\left(x^2+6x+8\right)=-3x$$
$$x^2+2x+1-x^2-6x-8=-3x$$
$$2x+1-6x-8=-3x$$
$$-4x-7=-3x$$
$$-4x-7+4x=-3x+4x$$
$$-7=x$$

Since $x=-7$ does not cause any denominator to equal zero, the solution set is $\{-7\}$.

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69.
$$3.2x+\frac{21.3}{65.871}=19.23$$
$$3.2x+\frac{21.3}{65.871}-\frac{21.3}{65.871}=19.23-\frac{21.3}{65.871}$$
$$3.2x=19.23-\frac{21.3}{65.871}$$
$$\left(\frac{1}{3.2}\right)(3.2x)=\left(19.23-\frac{21.3}{65.871}\right)\left(\frac{1}{3.2}\right)$$
$$x=\left(19.23-\frac{21.3}{65.871}\right)\left(\frac{1}{3.2}\right)\approx 5.91$$

The solution set is approximately $\{5.91\}$.

70.
$$6.2x-\frac{19.1}{83.72}=0.195$$
$$6.2x-\frac{19.1}{83.72}+\frac{19.1}{83.72}=0.195+\frac{19.1}{83.72}$$
$$6.2x=0.195+\frac{19.1}{83.72}$$
$$\left(\frac{1}{6.2}\right)(6.2x)=\left(0.195+\frac{19.1}{83.72}\right)\left(\frac{1}{6.2}\right)$$
$$x=\left(0.195+\frac{19.1}{83.72}\right)\left(\frac{1}{6.2}\right)\approx 0.07$$

The solution set is approximately $\{0.07\}$.

71.
$$14.72-21.58x=\frac{18}{2.11}x+2.4$$
$$14.72-21.58x-\frac{18}{2.11}x=\frac{18}{2.11}x+2.4-\frac{18}{2.11}x$$
$$14.72-21.58x-\frac{18}{2.11}x=2.4$$
$$14.72-21.58x-\frac{18}{2.11}x-14.72=2.4-14.72$$
$$-21.58x-\frac{18}{2.11}x=-12.32$$
$$\left(-21.58-\frac{18}{2.11}\right)x=-12.32$$
$$\left(\frac{1}{-21.58-\frac{18}{2.11}}\right)\left(-21.58-\frac{18}{2.11}\right)x=-12.32\left(\frac{1}{-21.58-\frac{18}{2.11}}\right)$$
$$x=-12.32\left(\frac{1}{-21.58-\frac{18}{2.11}}\right)\approx 0.41$$

The solution set is approximately $\{0.41\}$.

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72.
$$18.63x-\frac{21.2}{2.6}=\frac{14}{2.32}x-20$$
$$18.63x-\frac{21.2}{2.6}-\frac{14}{2.32}x=\frac{14}{2.32}x-20-\frac{14}{2.32}x$$
$$18.63x-\frac{21.2}{2.6}-\frac{14}{2.32}x=-20$$
$$18.63x-\frac{21.2}{2.6}-\frac{14}{2.32}x+\frac{21.2}{2.6}=-20+\frac{21.2}{2.6}$$
$$18.63x-\frac{14}{2.32}x=-20+\frac{21.2}{2.6}$$
$$\left(18.63-\frac{14}{2.32}\right)x=-20+\frac{21.2}{2.6}$$
$$\left(\frac{1}{18.63-\frac{14}{2.32}}\right)\left(18.63-\frac{14}{2.32}\right)x=\left(-20+\frac{21.2}{2.6}\right)\left(\frac{1}{18.63-\frac{14}{2.32}}\right)$$
$$x=\left(-20+\frac{21.2}{2.6}\right)\left(\frac{1}{18.63-\frac{14}{2.32}}\right)\approx -0.94$$

The solution set is approximately $\{-0.94\}$.

73. $ax-b=c,\quad a\neq 0$
$$ax-b+b=c+b$$
$$ax=b+c$$
$$\frac{ax}{a}=\frac{b+c}{a}$$
$$x=\frac{b+c}{a}$$

74. $1-ax=b,\quad a\neq 0$
$$1-ax-1=b-1$$
$$-ax=b-1$$
$$\frac{-ax}{-a}=\frac{b-1}{-a}$$
$$x=\frac{b-1}{-a}=\frac{1-b}{a}$$

75. $\frac{x}{a}+\frac{x}{b}=c,\quad a\neq 0, b\neq 0, a\neq -b$
$$ab\left(\frac{x}{a}+\frac{x}{b}\right)=ab\cdot c$$
$$bx+ax=abc$$
$$(a+b)x=abc$$
$$\frac{(a+b)x}{a+b}=\frac{abc}{a+b}$$
$$x=\frac{abc}{a+b}$$

76. $\frac{a}{x}+\frac{b}{x}=c,\quad c\neq 0$
$$x\left(\frac{a}{x}+\frac{b}{x}\right)=x\cdot c$$
$$a+b=cx$$
$$\frac{a+b}{c}=\frac{cx}{c}$$
$$x=\frac{a+b}{c}$$

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77. $x+2a=16+ax-6a,$ if $x=4$

$$4+2a=16+a(4)-6a$$
$$4+2a=16+4a-6a$$
$$4+2a=16-2a$$
$$4a=12$$
$$\frac{4a}{4}=\frac{12}{4}$$
$$a=3$$

78. $x+2b=x-4+2bx,$ for $x=2$

$$2+2b=2-4+2b(2)$$
$$2+2b=2-4+4b$$
$$2+2b=-2+4b$$
$$4=2b$$
$$\frac{4}{2}=b$$
$$b=2$$

79. $$\frac{1}{R}=\frac{1}{R_1}+\frac{1}{R_2}$$

$$RR_1R_2\left(\frac{1}{R}\right)=RR_1R_2\left(\frac{1}{R_1}+\frac{1}{R_2}\right)$$
$$R_1R_2=RR_2+RR_1$$
$$R_1R_2=R(R_2+R_1)$$
$$\frac{R_1R_2}{R_2+R_1}=\frac{R(R_2+R_1)}{R_2+R_1}$$
$$\frac{R_1R_2}{R_2+R_1}=R$$

80. $$A=P(1+rt)$$

$$A=P+Prt$$
$$A-P=Prt$$
$$\frac{A-P}{Pt}=\frac{Prt}{Pt}$$
$$\frac{A-P}{Pt}=r$$

81. $$F=\frac{mv^2}{R}$$

$$RF=R\left(\frac{mv^2}{R}\right)$$
$$RF=mv^2$$
$$\frac{RF}{F}=\frac{mv^2}{F}$$
$$R=\frac{mv^2}{F}$$

82. $$PV=nRT$$

$$\frac{PV}{nR}=\frac{nRT}{nR}$$
$$\frac{PV}{nR}=T$$

83. $$S=\frac{a}{1-r}$$

$$S(1-r)=\left(\frac{a}{1-r}\right)(1-r)$$
$$S-Sr=a$$
$$S-Sr-S=a-S$$
$$-Sr=a-S$$
$$\frac{-Sr}{-S}=\frac{a-S}{-S}$$
$$r=\frac{S-a}{S}$$

84. $$v=-gt+v_0$$

$$v-v_0=-gt$$
$$\frac{v-v_0}{-g}=\frac{-gt}{-g}$$
$$t=\frac{v-v_0}{-g}=\frac{v_0-v}{g}$$

85.

Amount in bonds	Amount in CDs	Total
x	$x-3000$	20,000

$$x+(x-3000)=20{,}000$$
$$2x-3000=20{,}000$$
$$2x=23{,}000$$
$$x=11{,}500$$

$11,500 will be invested in bonds and $8500 will be invested in CD's.

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86.

Sean's Amount	George's Amount	Total
x	$x-3000$	10,000

$$x+(x-3000)=10,000$$
$$2x-3000=10,000$$
$$2x=13,000$$
$$x=6500$$

Sean will receive \$6500 and George will receive \$3500.

87.

	Dollars per hour	Hours worked	Money earned
Regular wage	x	40	$40x$
Overtime wage	$1.5x$	8	$8(1.5x)$

$$40x+8(1.5x)=910$$
$$40x+12x=910$$
$$52x=910$$
$$x=\frac{910}{52}=17.50$$

Sandra's regular hourly wage is \$17.50.

88.

	Dollars per hour	Hours worked	Money earned
Regular wage	x	40	$40x$
Overtime wage	$1.5x$	6	$6(1.5x)$
Sunday wage	$2x$	4	$4(2x)$

$$40x+6(1.5x)+4(2x)=1083$$
$$40x+9x+8x=1083$$
$$57x=1083$$
$$x=\frac{1083}{57}=19$$

Leigh's regular hourly wage is \$19.00.

89. Let x represent the score on the final exam.

$$\frac{80+83+71+61+95+x+x}{7}=80$$
$$\frac{390+2x}{7}=80$$
$$390+2x=560$$
$$2x=170$$
$$x=85$$

Brooke needs a score of 85 on the final exam.

90. Let x represent the score on the final exam.
Note: since the final exam counts for two-thirds of the overall grade, the average of the four test scores count for one-third of the overall grade.
For a B, the average score must be 80.

$$\frac{1}{3}\left(\frac{86+80+84+90}{4}\right)+\frac{2}{3}x=80$$
$$\frac{1}{3}\left(\frac{340}{4}\right)+\frac{2}{3}x=80$$
$$\frac{85}{3}+\frac{2}{3}x=80$$
$$3\left(\frac{85}{3}+\frac{2}{3}x\right)=3(80)$$
$$85+2x=240$$
$$2x=155$$
$$x=77.5$$

Mike needs a score of 78 to earn a B.

For an A, the average score must be 90.

$$\frac{1}{3}\left(\frac{86+80+84+90}{4}\right)+\frac{2}{3}x=90$$
$$\frac{1}{3}\left(\frac{340}{4}\right)+\frac{2}{3}x=90$$
$$\frac{85}{3}+\frac{2}{3}x=90$$
$$3\left(\frac{85}{3}+\frac{2}{3}x\right)=3(90)$$
$$85+2x=270$$
$$2x=185$$
$$x=92.5$$

Mike needs a score of 93 to earn an A.

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91. Let x represent the original price of the phone.
Then $0.12x$ represents the reduction in the price of the phone.
The new price of the phone is \$572.
original price – reduction = new price

$$x - 0.12x = 572$$
$$0.88x = 572$$
$$x = 650$$

The original price of the phone was \$650.
The amount of the reduction (i.e., the savings) is $0.12(\$650) = \$78$.

92. Let x represent the original price of the car.
Then $0.15x$ represents the reduction in the price of the car.
The new price of the car is \$8000.
list price – reduction = new price

$$x - 0.15x = 18000$$
$$0.85x = 18000$$
$$x \approx 21176.47$$

The list price of the car was \$21,176.47.
The amount of the reduction (i.e., the savings) is $0.15(\$21176.47) \approx \$3176.47$.

93. Let x represent the price the theater pays for the candy.
Then $2.75x$ represents the markup on the candy.
The selling price of the candy is \$4.50.
suppier price + markup = selling price

$$x + 2.75x = 4.50$$
$$3.75x = 4.50$$
$$x = 1.20$$

The theater paid \$1.20 for the candy.

94. Let x represent selling price for the new car.
The dealer's cost is $0.85(\$24,000) = \$20,400$.
The markup is \$300.
selling price = dealer's cost + markup
$x = 20,400 + 300 = \$20,700$
At \$300 over the dealer's cost, the price of the care is \$20,700.

95.

	Tickets sold	Price per ticket	Money earned
Adults	x	7.50	$7.50x$
Children	$5200 - x$	4.50	$4.50(5200 - x)$

$$7.50x + 4.50(5200 - x) = 29,961$$
$$7.50x + 23,400 - 4.50x = 29,961$$
$$3.00x + 23,400 = 29,961$$
$$3.00x = 6561$$
$$x = 2187$$

There were 2187 adult patrons.

96. Let p represent the original price for the boots.
Then, $0.30p$ represents the discounted amount.
original price – discount = clearance price

$$p - 0.30p = 399$$
$$0.70p = 399$$
$$p = 570$$

The boots originally cost \$570.

97. Let w represent the width of the rectangle.
Then $w + 8$ is the length.
Perimeter is given by the formula $P = 2l + 2w$.

$$2(w + 8) + 2w = 60$$
$$2w + 16 + 2w = 60$$
$$4w + 16 = 60$$
$$4w = 44$$
$$w = 11$$

Now, 11 + 8 = 19.
The width of the rectangle is 11 feet and the length is 19 feet.

98. Let w represent the width of the rectangle.
Then $2w$ is the length.
Perimeter is given by the formula $P = 2l + 2w$.

$$2(2w) + 2w = 42$$
$$4w + 2w = 42$$
$$6w = 42$$
$$w = 7$$

Now, 2(7) = 14.
The width of the rectangle is 7 meters and the length is 14 meters.

99. We will let B be the calories from breakfast, L the calories from lunch and D the calories from dinner. So we have the following equations:

$$B = L + 125$$
$$D = 2L - 300$$
$$2025 = B + L + D$$

Now we substitute the first two into the last one and solve for L.

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$2025 = (L+125) + L + (2L-300)$

$2025 = 4L - 175$

$2200 = 4L$

$L = 550$

Now we substitute L into the first two equations to get B and D.

$B = 550 + 125 = 675$

$D = 2(550) - 300 = 800$

So Herschel took in 675 calories from breakfast, 550 calories from lunch and 800 calories from dinner.

100. We will let B be the calories from breakfast, L the calories from lunch, D the calories from dinner and S the calories from snacks. So we have the following equations:

$L = 0.5B \quad D = B + 200$

$S = B - 120 \quad E = 700$

$1480 = B + L + D - E$

Now we substitute the first four into the last one and solve for B.

$1480 = B + 0.5B + (B + 200) + (B - 200) - 700$

$1480 = 3.5B - 620$

$2100 = 3.5B$

$B = 600$

Now we substitute B to get S.

$S = B - 120 = 600 - 120 = 480$

So Tyshira took in 480 calories from snacks.

101.

Judy's Amount	Tom's Amount	Total
x	$\frac{2}{3}x$	18

$x + \frac{2}{3}x = 18$

$\frac{5}{3}x = 18$

$x = \frac{3}{5}(18)$

$x = 10.80$

Judy pays \$10.80 and Tom pays \$7.20.

102. An isosceles triangle has three equal sides. Therefore: $4x + 10 = 2x + 40 = 3x + 18$. Solve each set separately:

$4x + 10 = 2x + 40$

$2x = 30$

$x = 15$

$4x + 10 = 3x + 18$

$x = 8$

$2x + 40 = 3x + 18$

$-x = -22$

$x = 22$

Since 22 is the largest of the numbers then the largest perimeter is:

$4(22) + 10 + 2(22) + 40 + 3(22) + 18 = 266$

103. $\frac{3}{4}x - \frac{1}{5}\left(\frac{1}{2} - 3x\right) + 1 = \frac{1}{4}\left(\frac{1}{20}x + 6\right) - \frac{4}{5}$

$\frac{3}{4}x - \frac{1}{10} + \frac{3}{5}x + 1 = \frac{1}{80}x + \frac{3}{2} - \frac{4}{5}$

Multiply both sides by the LCD 80 to clear fractions.

$60x - 8 + 48x + 80 = x + 120 - 64$

$108x + 72 = x + 58$

$107x = -16$

$x = -\frac{16}{107}$

104. If a hexagon is inscribed in a circle then the sides of the hexagon are equal to the radius of the circle. Let the P = 6r be the perimeter of the hexagon. Let r be the radius of the circle.

$6r = r + 10$

$5r = 10$

$r = 2$

Thus r = 2 inches is the radius of the circle where the perimeter of the hexagon is 10 inches more than the radius.

105. To move from step (6) to step (7), we divided both sides of the equation by the expression $x - 2$. From step (1), however, we know $x = 2$, so this means we divided both sides of the equation by zero.

106– 107. Answers will vary.

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Section 1.2

1. $x^2 - 5x - 6 = (x-6)(x+1)$

2. $2x^2 - x - 3 = (2x-3)(x+1)$

3. $\left\{-\frac{5}{3}, 3\right\}$

4. True

5. $\frac{1}{2} \cdot 5 = \frac{5}{2}; \left(\frac{5}{2}\right)^2 = \frac{25}{4}; x^2 + 5x + \frac{25}{4}$

$x^2 + 5x + \frac{25}{4} = \left(x + \frac{5}{2}\right)^2$

6. discriminant; negative

7. False; a quadratic equation may have no real solutions.

8. False; If $x^2 = p$ then x could also be negative.

9. b

10. d

11. $x^2 - 9x = 0$

$x(x-9) = 0$

$x = 0$ or $x - 9 = 0$

$x = 0$ or $x = 9$

The solution set is $\{0, 9\}$.

12. $x^2 + 4x = 0$

$x(x+4) = 0$

$x = 0$ or $x + 4 = 0$

$x = 0$ or $x = -4$

The solution set is $\{-4, 0\}$.

13. $x^2 - 25 = 0$

$(x+5)(x-5) = 0$

$x + 5 = 0$ or $x - 5 = 0$

$x = -5$ or $x = 5$

The solution set is $\{-5, 5\}$.

14. $x^2 - 9 = 0$

$(x+3)(x-3) = 0$

$x + 3 = 0$ or $x - 3 = 0$

$x = -3$ or $x = 3$

The solution set is $\{-3, 3\}$.

15. $z^2 + z - 6 = 0$

$(z+3)(z-2) = 0$

$z + 3 = 0$ or $z - 2 = 0$

$z = -3$ or $z = 2$

The solution set is $\{-3, 2\}$.

16. $v^2 + 7v + 6 = 0$

$(v+6)(v+1) = 0$

$v + 6 = 0$ or $v + 1 = 0$

$v = -6$ or $v = -1$

The solution set is $\{-6, -1\}$

17. $2x^2 - 5x - 3 = 0$

$(2x+1)(x-3) = 0$

$2x + 1 = 0$ or $x - 3 = 0$

$x = -\frac{1}{2}$ or $x = 3$

The solution set is $\left\{-\frac{1}{2}, 3\right\}$

18. $3x^2 + 5x + 2 = 0$

$(3x+2)(x+1) = 0$

$3x + 2 = 0$ or $x + 1 = 0$

$x = -\frac{2}{3}$ or $x = -1$

The solution set is $\left\{-1, -\frac{2}{3}\right\}$.

19. $-5w^2 + 180 = 0$

$-5(w^2 - 36) = 0$

$-5(w+6)(w-6) = 0$

$w + 6 = 0$ or $w - 6 = 0$

$w = -6$ or $w = 6$

The solution set is $\{-6, 6\}$.

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20. $2y^2 - 50 = 0$

$2(y^2 - 25) = 0$

$2(y+5)(y-5) = 0$

$y+5=0 \quad \text{or} \quad y-5=0$

$y=-5 \quad \text{or} \quad y=5$

The solution set is $\{-5, 5\}$.

21. $x(x+3)-10=0$

$x^2+3x-10=0$

$(x-2)(x+5)=0$

$x-2=0 \quad \text{or} \quad x+5=0$

$x=2 \quad \text{or} \quad x=-5$

The solution set is $\{-5,2\}$.

22. $x(x+4)=12$

$x^2+4x-12=0$

$(x+6)(x-2)=0$

$x+6=0 \quad \text{or} \quad x-2=0$

$x=-6 \quad \text{or} \quad x=2$

The solution set is $\{-6,\ 2\}$.

23. $4x^2+9=12x$

$4x^2-12x+9=0$

$(2x-3)^2=0$

$2x-3=0$

$x=\frac{3}{2}$

The solution set is $\left\{\frac{3}{2}\right\}$.

24. $25x^2+16=40x$

$25x^2-40x+16=0$

$(5x-4)^2=0$

$5x-4=0$

$x=\frac{4}{5}$

The solution set is $\left\{\frac{4}{5}\right\}$.

25. $6(p^2-1)=5p$

$6p^2-6=5p$

$6p^2-5p-6=0$

$(3p+2)(2p-3)=0$

$3p+2=0 \quad \text{or} \quad 2p-3=0$

$p=-\frac{2}{3} \quad \text{or} \quad p=\frac{3}{2}$

The solution set is $\left\{-\frac{2}{3}, \frac{3}{2}\right\}$.

26. $2(2u^2-4u)+3=0$

$4u^2-8u+3=0$

$(2u-1)(2u-3)=0$

$2u-1=0 \quad \text{or} \quad 2u-3=0$

$u=\frac{1}{2} \quad \text{or} \quad u=\frac{3}{2}$

The solution set is $\left\{\frac{1}{2}, \frac{3}{2}\right\}$.

27. $6x-5=\frac{6}{x}$

$(6x-5)x=\left(\frac{6}{x}\right)x$

$6x^2-5x=6$

$6x^2-5x-6=0$

$(3x+2)(2x-3)=0$

$3x+2=0 \quad \text{or} \quad 2x-3=0$

$x=-\frac{2}{3} \quad \text{or} \quad x=\frac{3}{2}$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{-\frac{2}{3}, \frac{3}{2}\right\}$.

28. $x+\frac{12}{x}=7$

$\left(x+\frac{12}{x}\right)x=7x$

$x^2+12=7x$

$x^2-7x+12=0$

$(x-3)(x-4)=0$

$x-3=0 \quad \text{or} \quad x-4=0$

$x=3 \quad \text{or} \quad x=4$

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Neither of these values causes a denominator to equal zero, so the solution set is $\{3, 4\}$.

29.
$$\frac{4(x-2)}{x-3}+\frac{3}{x}=\frac{-3}{x(x-3)}$$
$$\left(\frac{4(x-2)}{x-3}+\frac{3}{x}\right)x(x-3)=\left(\frac{-3}{x(x-3)}\right)x(x-3)$$
$$4x(x-2)+3(x-3)=-3$$
$$4x^2-8x+3x-9=-3$$
$$4x^2-5x-6=0$$
$$(4x+3)(x-2)=0$$
$$4x+3=0 \quad \text{or} \quad x-2=0$$
$$x=-\frac{3}{4} \quad \text{or} \quad x=2$$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{-\frac{3}{4}, 2\right\}$.

30.
$$\frac{5}{x+4}=4+\frac{3}{x-2}$$
$$\left(\frac{5}{x+4}\right)(x+4)(x-2)=\left(4+\frac{3}{x-2}\right)(x+4)(x-2)$$
$$5(x-2)=4(x+4)(x-2)+3(x+4)$$
$$5x-10=4(x^2+2x-8)+3x+12$$
$$5x-10=4x^2+8x-32+3x+12$$
$$0=4x^2+6x-10$$
$$0=2(2x^2+3x-5)$$
$$0=2(2x+5)(x-1)$$
$$2x+5=0 \quad \text{or} \quad x-1=0$$
$$x=-\frac{5}{2} \quad \text{or} \quad x=1$$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{-\frac{5}{2}, 1\right\}$.

31.
$$x^2=25$$
$$x=\pm\sqrt{25}$$
$$x=\pm5$$

The solution set is $\{-5, 5\}$.

32.
$$x^2=36$$
$$x=\pm\sqrt{36}$$
$$x=\pm6$$

The solution set is $\{-6, 6\}$.

33.
$$(x-1)^2=4$$
$$x-1=\pm\sqrt{4}$$
$$x-1=\pm2$$
$$x-1=2 \text{ or } x-1=-2$$
$$x=3 \text{ or } x=-1$$

The solution set is $\{-1, 3\}$.

34.
$$(x+2)^2=1$$
$$x+2=\pm\sqrt{1}$$
$$x+2=\pm1$$
$$x+2=1 \text{ or } x+2=-1$$
$$x=-1 \text{ or } x=-3$$

The solution set is $\{-3, -1\}$.

35.
$$\left(\frac{1}{3}h+4\right)^2=16$$
$$\frac{1}{3}h+4=\pm\sqrt{16}$$
$$\frac{1}{3}h+4=\pm4$$
$$\frac{1}{3}h+4=4 \text{ or } \frac{1}{3}h+4=-4$$
$$\frac{1}{3}h=0 \text{ or } \frac{1}{3}h=-8$$
$$h=0 \text{ or } h=-24$$

The solution set is $\{-24, 0\}$.

36.
$$(3z-2)^2=4$$
$$3z-2=\pm\sqrt{4}$$
$$3z-2=\pm2$$
$$3z-2=2 \text{ or } 3z-2=-2$$
$$3z=4 \text{ or } 3z=0$$
$$z=\frac{4}{3} \text{ or } z=0$$

The solution set is $\left\{0, \frac{4}{3}\right\}$.

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37. $x^2+4x=21$

$x^2+4x+4=21+4$

$(x+2)^2=25$

$x+2=\pm\sqrt{25}$

$x+2=\pm 5$

$x=-2\pm 5$

$x=3$ or $x=-7$

The solution set is $\{-7,3\}$.

38. $x^2-6x=13$

$x^2-6x+9=13+9$

$(x-3)^2=22$

$x-3=\pm\sqrt{22}$

$x=3\pm\sqrt{22}$

The solution set is $\left\{3-\sqrt{22},3+\sqrt{22}\right\}$.

39. $x^2-\frac{1}{2}x-\frac{3}{16}=0$

$x^2-\frac{1}{2}x=\frac{3}{16}$

$x^2-\frac{1}{2}x+\frac{1}{16}=\frac{3}{16}+\frac{1}{16}$

$\left(x-\frac{1}{4}\right)^2=\frac{1}{4}$

$x-\frac{1}{4}=\pm\sqrt{\frac{1}{4}}=\pm\frac{1}{2}$

$x=\frac{1}{4}\pm\frac{1}{2}$

$x=\frac{3}{4}$ or $x=-\frac{1}{4}$

The solution set is $\left\{-\frac{1}{4},\frac{3}{4}\right\}$.

40. $x^2+\frac{2}{3}x-\frac{1}{3}=0$

$x^2+\frac{2}{3}x=\frac{1}{3}$

$x^2+\frac{2}{3}x+\frac{1}{9}=\frac{1}{3}+\frac{1}{9}$

$\left(x+\frac{1}{3}\right)^2=\frac{4}{9}$

$x+\frac{1}{3}=\pm\sqrt{\frac{4}{9}}=\pm\frac{2}{3}$

$x=-\frac{1}{3}\pm\frac{2}{3}$

$x=\frac{1}{3}$ or $x=-1$

The solution set is $\left\{-1,\frac{1}{3}\right\}$.

41. $3x^2+x-\frac{1}{2}=0$

$x^2+\frac{1}{3}x-\frac{1}{6}=0$

$x^2+\frac{1}{3}x=\frac{1}{6}$

$x^2+\frac{1}{3}x+\frac{1}{36}=\frac{1}{6}+\frac{1}{36}$

$\left(x+\frac{1}{6}\right)^2=\frac{7}{36}$

$x+\frac{1}{6}=\pm\sqrt{\frac{7}{36}}$

$x+\frac{1}{6}=\pm\frac{\sqrt{7}}{6}$

$x=\frac{-1\pm\sqrt{7}}{6}$

The solution set is $\left\{\frac{-1-\sqrt{7}}{6},\frac{-1+\sqrt{7}}{6}\right\}$.

42. $2x^2-3x-1=0$

$x^2-\frac{3}{2}x-\frac{1}{2}=0$

$x^2-\frac{3}{2}x=\frac{1}{2}$

$x^2-\frac{3}{2}x+\frac{9}{16}=\frac{1}{2}+\frac{9}{16}$

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$$\left(x-\frac{3}{4}\right)^2=\frac{17}{16}$$

$$x-\frac{3}{4}=\pm\sqrt{\frac{17}{16}}$$

$$x-\frac{3}{4}=\pm\frac{\sqrt{17}}{4}$$

$$x=\frac{3\pm\sqrt{17}}{4}$$

The solution set is $\left\{\frac{3-\sqrt{17}}{4},\frac{3+\sqrt{17}}{4}\right\}$.

43. $x^2-4x+2=0$

$a=1,\quad b=2,\quad c=-13$

$$x=\frac{-(2)\pm\sqrt{(2)^2-4(1)(-13)}}{2(1)}=\frac{-2\pm\sqrt{4+52}}{2}$$

$$=\frac{-2\pm\sqrt{56}}{2}=\frac{-2\pm2\sqrt{14}}{2}=-1\pm\sqrt{14}$$

The solution set is $\left\{-1-\sqrt{14},-1+\sqrt{14}\right\}$.

44. $x^2+4x+2=0$

$a=1,\quad b=4,\quad c=2$

$$x=\frac{-4\pm\sqrt{4^2-4(1)(2)}}{2(1)}=\frac{-4\pm\sqrt{16-8}}{2}$$

$$=\frac{-4\pm\sqrt{8}}{2}=\frac{-4\pm2\sqrt{2}}{2}=-2\pm\sqrt{2}$$

The solution set is $\left\{-2-\sqrt{2},-2+\sqrt{2}\right\}$.

45. $x^2-4x-1=0$

$a=1,\quad b=-4,\quad c=-1$

$$x=\frac{-(-4)\pm\sqrt{(-4)^2-4(1)(-1)}}{2(1)}=\frac{4\pm\sqrt{16+4}}{2}$$

$$=\frac{4\pm\sqrt{20}}{2}=\frac{4\pm2\sqrt{5}}{2}=2\pm\sqrt{5}$$

The solution set is $\left\{2-\sqrt{5},2+\sqrt{5}\right\}$.

46. $x^2+6x+1=0$

$a=1,\quad b=6,\quad c=1$

$$x=\frac{-6\pm\sqrt{6^2-4(1)(1)}}{2(1)}=\frac{-6\pm\sqrt{36-4}}{2}$$

$$=\frac{-6\pm\sqrt{32}}{2}=\frac{-6\pm4\sqrt{2}}{2}=-3\pm2\sqrt{2}$$

The solution set is $\left\{-3-2\sqrt{2},-3+2\sqrt{2}\right\}$.

47. $2x^2-5x+3=0$

$a=2,\quad b=-5,\quad c=3$

$$x=\frac{-(-5)\pm\sqrt{(-5)^2-4(2)(3)}}{2(2)}$$

$$=\frac{5\pm\sqrt{25-24}}{4}=\frac{5\pm\sqrt{1}}{4}=\frac{5\pm1}{4}$$

$$x=\frac{5+1}{4}\text{ or }x=\frac{5-1}{4}$$

$$x=\frac{6}{4}\quad\text{or}\quad x=\frac{4}{4}$$

$$x=\frac{3}{2}\quad\text{or}\quad x=1$$

The solution set is $\left\{1,\frac{3}{2}\right\}$.

48. $2x^2+5x+3=0$

$a=2,\quad b=5,\quad c=3$

$$x=\frac{-5\pm\sqrt{5^2-4(2)(3)}}{2(2)}$$

$$=\frac{-5\pm\sqrt{25-24}}{4}=\frac{-5\pm\sqrt{1}}{4}=\frac{-5\pm1}{4}$$

$$x=\frac{-5+1}{4}\text{ or }x=\frac{-5-1}{4}$$

$$x=\frac{-4}{4}\quad\text{or}\quad x=\frac{-6}{4}$$

$$x=-1\quad\text{or}\quad x=-\frac{3}{2}$$

The solution set is $\left\{-\frac{3}{2},-1\right\}$.

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49. $4y^2 - y + 2 = 0$

$a = 4, \quad b = -1, \quad c = 2$

$$y = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(4)(2)}}{2(4)}$$

$$= \frac{1 \pm \sqrt{1-32}}{8} = \frac{1 \pm \sqrt{-31}}{8}$$

No real solution.

50. $4t^2 + t + 1 = 0$

$a = 4, \quad b = 1, \quad c = 1$

$$t = \frac{-1 \pm \sqrt{1^2 - 4(4)(1)}}{2(4)}$$

$$= \frac{-1 \pm \sqrt{1-16}}{8} = \frac{-1 \pm \sqrt{-15}}{8}$$

No real solution.

51. $9x^2 + 8x = 5$

$9x^2 + 8x - 5 = 0$

$a = 9, \quad b = 8, \quad c = -5$

$$x = \frac{-8 \pm \sqrt{8^2 - 4(9)(-5)}}{2(9)}$$

$$= \frac{-8 \pm \sqrt{64+180}}{18} = \frac{-8 \pm \sqrt{244}}{18}$$

$$= \frac{-8 \pm 2\sqrt{61}}{18} = \frac{-4 \pm \sqrt{61}}{9}$$

The solution set is $\left\{\frac{-4-\sqrt{61}}{9}, \frac{-4+\sqrt{61}}{9}\right\}$.

52. $2x^2 = 1 - 2x$

$2x^2 + 2x - 1 = 0$

$a = 2, \quad b = 2, \quad c = -1$

$$x = \frac{-2 \pm \sqrt{2^2 - 4(2)(-1)}}{2(2)} = \frac{-2 \pm \sqrt{4+8}}{4}$$

$$= \frac{-2 \pm \sqrt{12}}{4} = \frac{-2 \pm 2\sqrt{3}}{4} = \frac{-1 \pm \sqrt{3}}{2}$$

The solution set is $\left\{\frac{-1-\sqrt{3}}{2}, \frac{-1+\sqrt{3}}{2}\right\}$.

53. $4x^2 = 9x$

$4x^2 - 9x = 0$

$x(4x - 9) = 0$

$x = 0 \quad \text{or} \quad 4x - 9 = 0$

$x = 0 \quad \text{or} \quad x = \frac{9}{4}$

The solution set is $\left\{0, \frac{9}{4}\right\}$.

54. $5x = 4x^2$

$0 = 4x^2 - 5x$

$0 = x(4x - 5)$

$x = 0 \quad \text{or} \quad 4x - 5 = 0$

$x = 0 \quad \text{or} \quad x = \frac{5}{4}$

The solution set is $\left\{0, \frac{5}{4}\right\}$.

55. $9t^2 - 6t + 1 = 0$

$a = 9, \quad b = -6, \quad c = 1$

$$t = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(9)(1)}}{2(9)}$$

$$= \frac{6 \pm \sqrt{36-36}}{18} = \frac{6 \pm 0}{18} = \frac{1}{3}$$

The solution set is $\left\{\frac{1}{3}\right\}$.

56. $4u^2 - 6u + 9 = 0$

$a = 4, \quad b = -6, \quad c = 9$

$$u = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(4)(9)}}{2(4)}$$

$$= \frac{6 \pm \sqrt{36-144}}{8} = \frac{6 \pm \sqrt{-108}}{8}$$

No real solution.

57. $\frac{3}{4}x^2 - \frac{1}{4}x - \frac{1}{2} = 0$

$$4\left(\frac{3}{4}x^2 - \frac{1}{4}x - \frac{1}{2}\right) = 4(0)$$

$3x^2 - x - 2 = 0$

$a = 3, \quad b = -1, \quad c = -2$

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$$x=\frac{-(-1)\pm\sqrt{(-1)^2-4(3)(-2)}}{2(3)}$$
$$=\frac{1\pm\sqrt{1+24}}{6}=\frac{1\pm\sqrt{25}}{6}=\frac{1\pm5}{6}$$
$$x=\frac{1+5}{6} \text{ or } x=\frac{1-5}{6}$$
$$x=\frac{6}{6} \text{ or } x=\frac{-4}{6}$$
$$x=1 \text{ or } x=-\frac{2}{3}$$

The solution set is $\left\{-\frac{2}{3},1\right\}$.

58. $\frac{2}{3}x^2-x-3=0$

$$3\left(\frac{2}{3}x^2-x-3\right)=3(0)$$
$$2x^2-3x-9=0$$
$$a=2,\quad b=-3,\quad c=-9$$
$$x=\frac{-(-3)\pm\sqrt{(-3)^2-4(2)(-9)}}{2(2)}$$
$$=\frac{3\pm\sqrt{9+72}}{4}=\frac{3\pm\sqrt{81}}{4}=\frac{3\pm9}{4}$$
$$x=\frac{3+9}{4} \text{ or } x=\frac{3-9}{4}$$
$$x=\frac{12}{4} \text{ or } x=\frac{-6}{4}$$
$$x=3 \text{ or } x=-\frac{3}{2}$$

The solution set is $\left\{-\frac{3}{2},3\right\}$.

59. $\frac{5}{3}x^2-x=\frac{1}{3}$

$$3\left(\frac{5}{3}x^2-x\right)=3\left(\frac{1}{3}\right)$$
$$5x^2-3x=1$$
$$5x^2-3x-1=0$$
$$a=5,\quad b=-3,\quad c=-1$$
$$x=\frac{-(-3)\pm\sqrt{(-3)^2-4(5)(-1)}}{2(5)}$$
$$=\frac{3\pm\sqrt{9+20}}{10}=\frac{3\pm\sqrt{29}}{10}$$

The solution set is $\left\{\frac{3-\sqrt{29}}{10},\frac{3+\sqrt{29}}{10}\right\}$.

60. $\frac{3}{5}x^2-x=\frac{1}{5}$

$$5\left(\frac{3}{5}x^2-x\right)=5\left(\frac{1}{5}\right)$$
$$3x^2-5x=1$$
$$3x^2-5x-1=0$$
$$a=3,\quad b=-5,\quad c=-1$$
$$x=\frac{-(-5)\pm\sqrt{(-5)^2-4(3)(-1)}}{2(3)}$$
$$=\frac{5\pm\sqrt{25+12}}{6}=\frac{5\pm\sqrt{37}}{6}$$

The solution set is $\left\{\frac{5-\sqrt{37}}{6},\frac{5+\sqrt{37}}{6}\right\}$.

61. $2x(x+2)=3$

$$2x^2+4x-3=0$$
$$a=2,\quad b=4,\quad c=-3$$
$$x=\frac{-4\pm\sqrt{4^2-4(2)(-3)}}{2(2)}=\frac{-4\pm\sqrt{16+24}}{4}$$
$$=\frac{-4\pm\sqrt{40}}{4}=\frac{-4\pm2\sqrt{10}}{4}=\frac{-2\pm\sqrt{10}}{2}$$

The solution set is $\left\{\frac{-2-\sqrt{10}}{2},\frac{-2+\sqrt{10}}{2}\right\}$.

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62. $3x(x+2)=1$

$3x^2+6x-1=0$

$a=3,\quad b=6,\quad c=-1$

$$x=\frac{-6\pm\sqrt{6^2-4(3)(-1)}}{2(3)}=\frac{-6\pm\sqrt{36+12}}{6}$$

$$=\frac{-6\pm\sqrt{48}}{6}=\frac{-6\pm4\sqrt{3}}{6}=\frac{-3\pm2\sqrt{3}}{3}$$

The solution set is $\left\{\frac{-3-2\sqrt{3}}{3},\frac{-3+2\sqrt{3}}{3}\right\}$.

63. $4+\frac{1}{x}-\frac{1}{x^2}=0$

$$x^2\left(4+\frac{1}{x}-\frac{1}{x^2}\right)=x^2(0)$$

$4x^2+x-1=0$

$a=4,\quad b=1,\quad c=-1$

$$x=\frac{-1\pm\sqrt{1^2-4(4)(-1)}}{2(4)}$$

$$=\frac{-1\pm\sqrt{1+16}}{8}=\frac{-1\pm\sqrt{17}}{8}$$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{\frac{-1-\sqrt{17}}{8},\frac{-1+\sqrt{17}}{8}\right\}$.

64. $2+\frac{8}{x}+\frac{3}{x^2}=0$

$$x^2\left(2+\frac{8}{x}+\frac{3}{x^2}\right)=x^2(0)$$

$2x^2+8x+3=0$

$a=2,\quad b=8,\quad c=3$

$$x=\frac{-(8)\pm\sqrt{(8)^2-4(2)(3)}}{2(2)}$$

$$=\frac{-8\pm\sqrt{64-24}}{4}=\frac{-8\pm\sqrt{40}}{4}$$

$$=\frac{-8\pm2\sqrt{10}}{4}=\frac{-4\pm\sqrt{10}}{2}$$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{\frac{-4-\sqrt{10}}{4},\frac{-4+\sqrt{10}}{4}\right\}$.

65. $\frac{3x}{x-2}+\frac{1}{x}=4$

$$\left(\frac{3x}{x-2}+\frac{1}{x}\right)x(x-2)=4x(x-2)$$

$3x(x)+(x-2)=4x^2-8x$

$3x^2+x-2=4x^2-8x$

$0=x^2-9x+2$

$a=1,\quad b=-9,\quad c=2$

$$x=\frac{-(-9)\pm\sqrt{(-9)^2-4(1)(2)}}{2(1)}$$

$$=\frac{9\pm\sqrt{81-8}}{2}=\frac{9\pm\sqrt{73}}{2}$$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{\frac{9-\sqrt{73}}{2},\frac{9+\sqrt{73}}{2}\right\}$.

66. $\frac{2x}{x-3}+\frac{1}{x}=4$

$$\left(\frac{2x}{x-3}+\frac{1}{x}\right)x(x-3)=4x(x-3)$$

$2x(x)+(x-3)=4x^2-12x$

$2x^2+x-3=4x^2-12x$

$0=2x^2-13x+3$

$a=2,\quad b=-13,\quad c=3$

$$x=\frac{-(-13)\pm\sqrt{(-13)^2-4(2)(3)}}{2(2)}$$

$$=\frac{13\pm\sqrt{169-24}}{4}=\frac{13\pm\sqrt{145}}{4}$$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{\frac{13-\sqrt{145}}{4},\frac{13+\sqrt{145}}{4}\right\}$.

67. $x^2-4.1x+2.2=0$

$a=1,\quad b=-4.1,\quad c=2.2$

$$x=\frac{-(-4.1)\pm\sqrt{(-4.1)^2-4(1)(2.2)}}{2(1)}$$

$$=\frac{4.1\pm\sqrt{16.81-8.8}}{2}=\frac{4.1\pm\sqrt{8.01}}{2}$$

$x\approx3.47$ or $x\approx0.63$

The solution set is $\{0.63,\ 3.47\}$.

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68. $x^2+3.9x+1.8=0$

$a=1,\quad b=3.9,\quad c=1.8$

$$x=\frac{-3.9\pm\sqrt{(3.9)^2-4(1)(1.8)}}{2(1)}$$

$$=\frac{-3.9\pm\sqrt{15.21-7.2}}{2}=\frac{-3.9\pm\sqrt{8.01}}{2}$$

$x\approx -0.53$ or $x\approx -3.37$

The solution set is $\{-3.37,-0.53\}$.

69. $x^2+\sqrt{3}x-3=0$

$a=1,\quad b=\sqrt{3},\quad c=-3$

$$x=\frac{-\sqrt{3}\pm\sqrt{\left(\sqrt{3}\right)^2-4(1)(-3)}}{2(1)}$$

$$=\frac{-\sqrt{3}\pm\sqrt{3+12}}{2}=\frac{-\sqrt{3}\pm\sqrt{15}}{2}$$

$x\approx 1.07$ or $x\approx -2.80$

The solution set is $\{-2.80,\ 1.07\}$.

70. $x^2+\sqrt{2}x-2=0$

$a=1,\quad b=\sqrt{2},\quad c=-2$

$$x=\frac{-\sqrt{2}\pm\sqrt{\left(\sqrt{2}\right)^2-4(1)(-2)}}{2(1)}$$

$$=\frac{-\sqrt{2}\pm\sqrt{2+8}}{2}=\frac{-\sqrt{2}\pm\sqrt{10}}{2}$$

$x\approx 0.87$ or $x\approx -2.29$

The solution set is $\{-2.29,\ 0.87\}$.

71. $\pi x^2-x-\pi=0$

$a=\pi,\quad b=-1,\quad c=-\pi$

$$x=\frac{-(-1)\pm\sqrt{(-1)^2-4(\pi)(-\pi)}}{2(\pi)}$$

$$=\frac{1\pm\sqrt{1+4\pi^2}}{2\pi}$$

$x\approx 1.17$ or $x\approx -0.85$

The solution set is $\{-0.85,\ 1.17\}$.

72. $\pi x^2+\pi x-2=0$

$a=\pi,\quad b=\pi,\quad c=-2$

$$x=\frac{-\pi\pm\sqrt{(\pi)^2-4(\pi)(-2)}}{2(\pi)}$$

$$=\frac{-\pi\pm\sqrt{\pi^2+8\pi}}{2\pi}$$

$x\approx 0.44$ or $x\approx -1.44$

The solution set is $\{-1.44,\ 0.44\}$.

73. $2x^2-6x+7=0$

$a=2,\quad b=-6,\quad c=7$

$b^2-4ac=(-6)^2-4(2)(7)=36-56=-20$

Since the $b^2-4ac<0$, the equation has no real solution.

74. $x^2+4x+7=0$

$a=1,\quad b=4,\quad c=7$

$b^2-4ac=(4)^2-4(1)(7)=16-28=-12$

Since the $b^2-4ac<0$, the equation has no real solution.

75. $9x^2-30x+25=0$

$a=9,\quad b=-30,\quad c=25$

$b^2-4ac=(-30)^2-4(9)(25)=900-900=0$

Since $b^2-4ac=0$, the equation has one repeated real solution.

76. $25x^2-20x+4=0$

$a=25,\quad b=-20,\quad c=4$

$b^2-4ac=(-20)^2-4(25)(4)=400-400=0$

Since $b^2-4ac=0$, the equation has one repeated real solution.

77. $3x^2+5x-8=0$

$a=3,\quad b=5,\quad c=-8$

$b^2-4ac=(5)^2-4(3)(-8)=25+96=121$

Since $b^2-4ac>0$, the equation has two unequal real solutions.

78. $2x^2-3x-7=0$

$a=2,\quad b=-3,\quad c=-7$

$b^2-4ac=(-3)^2-4(2)(-7)=9+56=65$

Since $b^2-4ac>0$, the equation has two unequal real solutions.

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79. $x^2 - 5 = 0$

$x^2 = 5$

$x = \pm\sqrt{5}$

The solution set is $\{-\sqrt{5}, \sqrt{5}\}$.

80. $x^2 - 6 = 0$

$x^2 = 6$

$x = \pm\sqrt{6}$

The solution set is $\{-\sqrt{6}, \sqrt{6}\}$.

81. $16x^2 - 8x + 1 = 0$

$(4x-1)(4x-1) = 0$

$4x - 1 = 0$

$x = \frac{1}{4}$

The solution set is $\left\{\frac{1}{4}\right\}$.

82. $9x^2 - 12x + 4 = 0$

$(3x-2)(3x-2) = 0$

$3x - 2 = 0$

$x = \frac{2}{3}$

The solution set is $\left\{\frac{2}{3}\right\}$.

83. $10x^2 - 19x - 15 = 0$

$(5x+3)(2x-5) = 0$

$5x + 3 = 0$ or $2x - 5 = 0$

$x = -\frac{3}{5}$ or $x = \frac{5}{2}$

The solution set is $\left\{-\frac{3}{5}, \frac{5}{2}\right\}$.

84. $6x^2 + 7x - 20 = 0$

$(3x-4)(2x+5) = 0$

$3x - 4 = 0$ or $2x + 5 = 0$

$x = \frac{4}{3}$ or $x = -\frac{5}{2}$

The solution set is $\left\{-\frac{5}{2}, \frac{4}{3}\right\}$.

85. $2 + z = 6z^2$

$0 = 6z^2 - z - 2$

$0 = (3z-2)(2z+1)$

$3z - 2 = 0$ or $2z + 1 = 0$

$z = \frac{2}{3}$ or $z = -\frac{1}{2}$

The solution set is $\left\{-\frac{1}{2}, \frac{2}{3}\right\}$.

86. $2 = y + 6y^2$

$0 = 6y^2 + y - 2$

$0 = (3y+2)(2y-1)$

$3y + 2 = 0$ or $2y - 1 = 0$

$y = -\frac{2}{3}$ or $y = \frac{1}{2}$

The solution set is $\left\{-\frac{2}{3}, \frac{1}{2}\right\}$.

87. $x^2 + \sqrt{2}x = \frac{1}{2}$

$x^2 + \sqrt{2}x - \frac{1}{2} = 0$

$2\left(x^2 + \sqrt{2}x - \frac{1}{2}\right) = 2(0)$

$2x^2 + 2\sqrt{2}x - 1 = 0$

$a = 2, \quad b = 2\sqrt{2}, \quad c = -1$

$$x = \frac{-(2\sqrt{2}) \pm \sqrt{(2\sqrt{2})^2 - 4(2)(-1)}}{2(2)}$$

$$= \frac{-2\sqrt{2} \pm \sqrt{8+8}}{4} = \frac{-2\sqrt{2} \pm \sqrt{16}}{4}$$

$$= \frac{-2\sqrt{2} \pm 4}{4} = \frac{-\sqrt{2} \pm 2}{2}$$

The solution set is $\left\{\frac{-\sqrt{2}-2}{2}, \frac{-\sqrt{2}+2}{2}\right\}$

88. $\frac{1}{2}x^2 = \sqrt{2}x + 1$

$\frac{1}{2}x^2 - \sqrt{2}x - 1 = 0$

$2\left(\frac{1}{2}x^2 - \sqrt{2}x - 1\right) = 2(0)$

$x^2 - 2\sqrt{2}x - 2 = 0$

$a = 1, \quad b = -2\sqrt{2}, \quad c = -2$

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$$x = \frac{-(-2\sqrt{2}) \pm \sqrt{(-2\sqrt{2})^2 - 4(1)(-2)}}{2(1)}$$
$$= \frac{2\sqrt{2} \pm \sqrt{8+8}}{2} = \frac{2\sqrt{2} \pm \sqrt{16}}{2}$$
$$= \frac{2\sqrt{2} \pm 4}{2} = \frac{\sqrt{2} \pm 2}{1}$$

The solution set is $\left\{\sqrt{2}-2, \sqrt{2}+2\right\}$.

89. $x^2 + x = 4$

$x^2 + x - 4 = 0$

$a = 1, \quad b = 1, \quad c = -4$

$$x = \frac{-(1) \pm \sqrt{(1)^2 - 4(1)(-4)}}{2(1)}$$
$$= \frac{-1 \pm \sqrt{1+16}}{2} = \frac{-1 \pm \sqrt{17}}{2}$$

The solution set is $\left\{\frac{-1-\sqrt{17}}{2}, \frac{-1+\sqrt{17}}{2}\right\}$.

90. $x^2 + x = 1$

$x^2 + x - 1 = 0$

$a = 1, \quad b = 1, \quad c = -1$

$$x = \frac{-(1) \pm \sqrt{(1)^2 - 4(1)(-1)}}{2(1)}$$
$$= \frac{-1 \pm \sqrt{1+4}}{2} = \frac{-1 \pm \sqrt{5}}{2}$$

The solution set is $\left\{\frac{-1-\sqrt{5}}{2}, \frac{-1+\sqrt{5}}{2}\right\}$.

91.
$$\frac{x}{x-2} + \frac{2}{x+1} = \frac{7x+1}{x^2-x-2}$$
$$\frac{x}{x-2} + \frac{2}{x+1} = \frac{7x+1}{(x-2)(x+1)}$$
$$\left(\frac{x}{x-2} + \frac{2}{x+1}\right)(x-2)(x+1) = \left(\frac{7x+1}{(x-2)(x+1)}\right)(x-2)(x+1)$$
$$x(x+1) + 2(x-2) = 7x+1$$
$$x^2 + x + 2x - 4 = 7x + 1$$
$$x^2 + 3x - 4 = 7x + 1$$
$$x^2 - 4x - 5 = 0$$
$$(x+1)(x-5) = 0$$
$$x+1 = 0 \quad \text{or} \quad x-5 = 0$$
$$x = -1 \quad \text{or} \quad x = 5$$

The value $x = -1$ causes a denominator to equal zero, so we disregard it. Thus, the solution set is $\{5\}$.

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92.
$$\frac{3x}{x+2}+\frac{1}{x-1}=\frac{4-7x}{x^2+x-2}$$
$$\frac{3x}{x+2}+\frac{1}{x-1}=\frac{4-7x}{(x+2)(x-1)}$$
$$\left(\frac{3x}{x+2}+\frac{1}{x-1}\right)(x+2)(x-1)=\left(\frac{4-7x}{(x+2)(x-1)}\right)(x+2)(x-1)$$
$$3x(x-1)+(x+2)=4-7x$$
$$3x^2-3x+x+2=4-7x$$
$$3x^2-2x+2=4-7x$$
$$3x^2+5x-2=0$$
$$(3x-1)(x+2)=0$$
$$3x-1=0 \quad \text{or} \quad x+2=0$$
$$x=\frac{1}{3} \quad \text{or} \quad x=-2$$

The value $x=-2$ causes a denominator to equal zero, so we disregard it. Thus, the solution set is $\left\{\frac{1}{3}\right\}$.

93. Since this is a right triangle then we can use the Pythagorean Theorem. So
$$(2x+3)^2=(2x-5)^2+(x+7)^2$$
$$4x^2+12x+9=4x^2-20x+25+x^2+14x+49$$
$$12x+9=x^2-6x+74$$
$$0=x^2-18x+65$$
$$0=(x-5)(x-13)$$
$$x-5=0 \quad \text{or} \quad x-13=0$$
$$x=5 \quad \text{or} \quad x=13$$

This means there are 2 possible that meet these requirements. Substituting x into the given sides gives:
When $x=5$: 5m, 12m, 13m
When $x=13$: 20m, 21m, 29m
Thus there are 2 solutions.

94. Since this is a right triangle then we can use the Pythagorean Theorem. So
$$(4x+5)^2=(3x+13)^2+x^2$$
$$16x^2+40x+25=9x^2+78x+169+x^2$$
$$6x^2-38x-144=0$$
$$2(3x^2-19x-72)=0$$
$$2(3x+8)(x-9)=0$$
$$3x+8=0 \quad \text{or} \quad x-9=0$$
$$x=-\frac{8}{3} \quad \text{or} \quad x=9$$

This means there are 2 possible solutions that meet these requirements. Substituting x into the given sides gives:
When $x=9$: 41m, 40m, 9m
When $x=-\frac{8}{3}$ at least one side of the triangle has a negative measurement which is impossible.
Thus there is only 1 triangle possible

95. Let w represent the width of window.
Then $l=w+2$ represents the length of the window.
Since the area is 143 square feet, we have:
$$w(w+2)=143$$
$$w^2+2w-143=0$$
$$(w+13)(w-11)=0$$
$$\cancel{w=-13} \quad \text{or} \quad w=11$$
Discard the negative solution since width cannot be negative. The width of the rectangular window is 11 feet and the length is 13 feet.

96. Let w represent the width of window.
Then $l=w+1$ represents the length of the window.
Since the area is 306 square centimeters, we have: $w(w+1)=306$
$$w^2+w-306=0$$
$$(w+18)(w-17)=0$$
$$\cancel{w=-18} \quad \text{or} \quad w=17$$
Discard the negative solution since width cannot

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be negative. The width of the rectangular window is 17 centimeters and the length is 18 centimeters.

97. Let l represent the length of the rectangle.
Let w represent the width of the rectangle.
The perimeter is 26 meters and the area is 40 square meters.

$$2l + 2w = 26$$
$$l + w = 13 \quad \text{so} \quad w = 13 - l$$
$$lw = 40$$
$$l(13 - l) = 40$$
$$13l - l^2 = 40$$
$$l^2 - 13l + 40 = 0$$
$$(l - 8)(l - 5) = 0$$
$$l = 8 \text{ or } l = 5$$
$$w = 5 \quad w = 8$$

The dimensions are 5 meters by 8 meters.

98. Let r represent the radius of the circle.
Since the field is a square with area 1250 square feet, the length of a side of the square is $\sqrt{1250} = 25\sqrt{2}$ feet. The length of the diagonal is $2r$.
Use the Pythagorean Theorem to solve for r:

$$(2r)^2 = \left(25\sqrt{2}\right)^2 + \left(25\sqrt{2}\right)^2$$
$$4r^2 = 1250 + 1250$$
$$4r^2 = 2500$$
$$r^2 = 625$$
$$r = 25$$

The shortest radius setting for the sprinkler is 25 feet.

99. Let x = length of side of original sheet in feet.
Length of box: $x - 2$ feet
Width of box: $x - 2$ feet
Height of box: 1 foot

$$V = l \cdot w \cdot h$$
$$4 = (x - 2)(x - 2)(1)$$
$$4 = x^2 - 4x + 4$$
$$0 = x^2 - 4x$$
$$0 = x(x - 4)$$
$$x = 0 \text{ or } x = 4$$

Discard $x = 0$ since that is not a feasible length for the original sheet. Therefore, the original sheet should measure 4 feet on each side.

100. Let x = width of original sheet in feet.
Length of sheet: $2x$
Length of box: $2x - 2$ feet
Width of box: $x - 2$ feet
Height of box: 1 foot

$$V = l \cdot w \cdot h$$
$$4 = (2x - 2)(x - 2)(1)$$
$$4 = 2x^2 - 6x + 4$$
$$0 = 2x^2 - 6x$$
$$0 = x^2 - 3x$$
$$0 = x(x - 3)$$
$$x = 0 \text{ or } x = 3$$

Discard $x = 0$ since that is not a feasible length for the original sheet. Therefore, the original sheet is 3 feet wide and 6 feet long.

101. a. When the ball strikes the ground, the distance from the ground will be 0. Therefore, we solve

$$96 + 80t - 16t^2 = 0$$
$$-16t^2 + 80t + 96 = 0$$
$$t^2 - 5t - 6 = 0$$
$$(t - 6)(t + 1) = 0$$
$$t = 6 \text{ or } t = -1$$

Discard the negative solution since the time of flight must be positive. The ball will strike the ground after 6 seconds.

b. When the ball passes the top of the building, it will be 96 feet from the ground. Therefore, we solve

$$96 + 80t - 16t^2 = 96$$
$$-16t^2 + 80t = 0$$
$$t^2 - 5t = 0$$
$$t(t - 5) = 0$$
$$t = 0 \text{ or } t = 5$$

The ball is at the top of the building at time $t = 0$ when it is thrown. It will pass the top of the building on the way down after 5 seconds.

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102. a. To find when the object will be 15 meters above the ground, we solve

$$-4.9t^2 + 20t = 15$$

$$-4.9t^2 + 20t - 15 = 0$$

$$a = -4.9,\ b = 20,\ c = -15$$

$$t = \frac{-20 \pm \sqrt{20^2 - 4(-4.9)(-15)}}{2(-4.9)}$$

$$= \frac{-20 \pm \sqrt{106}}{-9.8} = \frac{20 \pm \sqrt{106}}{9.8}$$

$$t \approx 0.99 \quad \text{or} \quad t \approx 3.09$$

The object will be 15 meters above the ground after about 0.99 seconds (on the way up) and about 3.09 seconds (on the way down).

b. The object will strike the ground when the distance from the ground is 0. Therefore, we solve

$$-4.9t^2 + 20t = 0$$

$$t(-4.9t + 20) = 0$$

$$t = 0 \quad \text{or} \quad -4.9t + 20 = 0$$

$$-4.9t = -20$$

$$t \approx 4.08$$

The object will strike the ground after about 4.08 seconds.

c.

$$-4.9t^2 + 20t = 100$$

$$-4.9t^2 + 20t - 100 = 0$$

$$a = -4.9,\ b = 20,\ c = -100$$

$$t = \frac{-20 \pm \sqrt{20^2 - 4(-4.9)(-100)}}{2(-4.9)}$$

$$= \frac{-20 \pm \sqrt{-1560}}{-9.8}$$

There is no real solution. The object never reaches a height of 100 meters.

103. Let x represent the number of centimeters the length and width should be reduced.
$12 - x$ = the new length, $7 - x$ = the new width.
The new volume is 90% of the old volume.

$$(12 - x)(7 - x)(3) = 0.9(12)(7)(3)$$

$$3x^2 - 57x + 252 = 226.8$$

$$3x^2 - 57x + 25.2 = 0$$

$$x^2 - 19x + 8.4 = 0$$

$$x = \frac{-(-19) \pm \sqrt{(-19)^2 - 4(1)(8.4)}}{2(1)} = \frac{19 \pm \sqrt{327.4}}{2}$$

$$x \approx 0.45 \quad \text{or} \quad x \approx 18.55$$

Since 18.55 exceeds the dimensions, it is discarded. The dimensions of the new chocolate bar are: 11.55 cm by 6.55 cm by 3 cm.

104. Let x represent the number of centimeters the length and width should be reduced.
$12 - x$ = the new length, $7 - x$ = the new width.
The new volume is 80% of the old volume.

$$(12 - x)(7 - x)(3) = 0.8(12)(7)(3)$$

$$3x^2 - 57x + 252 = 201.6$$

$$3x^2 - 57x + 50.4 = 0$$

$$x^2 - 19x + 16.8 = 0$$

$$x = \frac{-(-19) \pm \sqrt{(-19)^2 - 4(1)(16.8)}}{2(1)} = \frac{19 \pm \sqrt{293.8}}{2}$$

$$x \approx 0.93 \quad \text{or} \quad x \approx 18.07$$

Since 18.07 exceeds the dimensions, it is discarded. The dimensions of the new chocolate bar are: 11.07 cm by 6.07 cm by 3 cm.

105. Let x represent the width of the border measured in feet. The radius of the pool is 5 feet. Then $x + 5$ represents the radius of the circle, including both the pool and the border. The total area of the pool and border is

$$A_T = \pi(x + 5)^2.$$

The area of the pool is $A_P = \pi(5)^2 = 25\pi$.
The area of the border is

$$A_B = A_T - A_P = \pi(x + 5)^2 - 25\pi.$$

Since the concrete is 3 inches or 0.25 feet thick, the volume of the concrete in the border is

$$0.25A_B = 0.25\left(\pi(x + 5)^2 - 25\pi\right)$$

Solving the volume equation:

$$0.25\left(\pi(x + 5)^2 - 25\pi\right) = 27$$

$$\pi\left(x^2 + 10x + 25 - 25\right) = 108$$

$$\pi x^2 + 10\pi x - 108 = 0$$

$$x = \frac{-10\pi \pm \sqrt{(10\pi)^2 - 4(\pi)(-108)}}{2(\pi)}$$

$$= \frac{-31.42 \pm \sqrt{100\pi^2 + 432\pi}}{6.28}$$

$$x \approx 2.71 \quad \text{or} \quad x \approx -12.71$$

Discard the negative solution. The width of the border is roughly 2.71 feet.

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106. Let x represent the width of the border measured in feet. The radius of the pool is 5 feet. Then $x+5$ represents the radius of the circle, including both the pool and the border. The total area of the pool and border is $A_T = \pi(x+5)^2$.

The area of the pool is $A_P = \pi(5)^2 = 25\pi$.

The area of the border is $A_B = A_T - A_P = \pi(x+5)^2 - 25\pi$.

Since the concrete is 4 inches = $\frac{1}{3}$ foot thick, the volume of the concrete in the border is $\frac{1}{3}A_B = \frac{1}{3}\left(\pi(x+5)^2 - 25\pi\right)$

Solving the volume equation:

$$\frac{1}{3}\left(\pi(x+5)^2 - 25\pi\right) = 27$$

$$\pi\left(x^2+10x+25-25\right) = 81$$

$$\pi x^2 + 10\pi x - 81 = 0$$

$$x = \frac{-10\pi \pm \sqrt{(10\pi)^2 - 4(\pi)(-81)}}{2(\pi)}$$

$$= \frac{-31.42 \pm \sqrt{100\pi^2 + 324\pi}}{6.28}$$

$x \approx 2.13$ or $x \approx -12.13$

Discard the negative solution. The width of the border is approximately 2.13 feet.

107. Let x represent the width of the border measured in feet.

The total area is $A_T = (6+2x)(10+2x)$.

The area of the garden is $A_G = 6 \cdot 10 = 60$.

The area of the border is $A_B = A_T - A_G = (6+2x)(10+2x) - 60$.

Since the concrete is 3 inches or 0.25 feet thick, the volume of the concrete in the border is $0.25A_B = 0.25\left((6+2x)(10+2x) - 60\right)$

Solving the volume equation:

$$0.25\left((6+2x)(10+2x) - 60\right) = 27$$

$$60 + 32x + 4x^2 - 60 = 108$$

$$4x^2 + 32x - 108 = 0$$

$$x^2 + 8x - 27 = 0$$

$$x = \frac{-8 \pm \sqrt{8^2 - 4(1)(-27)}}{2(1)} = \frac{-8 \pm \sqrt{172}}{2}$$

$x \approx 2.56$ or $x \approx -10.56$

Discard the negative solution. The width of the border is approximately 2.56 feet.

108. Let x = the width and $2x$ = the length of the patio. The height is $\frac{1}{3}$ foot and the concrete available is $8(27) = 216$ cubic feet..

$$V = lwh = x(2x) \cdot \frac{1}{3} = 216$$

$$\frac{2}{3}x^2 = 216$$

$$x^2 = 324 \Rightarrow x = \pm 18$$

The dimensions of the patio are 18 feet by 36 feet.

109. Let x = the length of a 12.9-inch iPad Pro in a 16:94:3 format.

Then $\frac{9}{16}x$ = the width of the iPad. The diagonal of the 12.9-inch iPad is 9.7 inches, so by the Pythagorean theorem we have:

$$x^2 + \left(\frac{9}{16}x\right)^2 = 12.9^2$$

$$x^2 + \frac{81}{256}x^2 = 166.41$$

$$256\left(x^2 + \frac{81}{256}x^2\right) = 256(166.41)$$

$$256x^2 + 81x^2 = 42600.96$$

$$337x^2 = 42600.96 \Rightarrow x^2 = \frac{42600.96}{337}$$

$$x = \pm\sqrt{\frac{42600.96}{337}} \approx \pm 11.24$$

Since the length cannot be negative, the length of the iPad is $\sqrt{\frac{42600.96}{337}}$ inches and the width is $\frac{9}{16}\sqrt{\frac{42600.96}{337}} \approx 6.32$ inches. Thus, the area of the iPad is $\sqrt{\frac{42600.96}{337}} \cdot \frac{9}{16}\sqrt{\frac{42600.96}{337}} = 71.11$ square inches.

Let y = the length of a 12-inch 3:2 format Microsoft Surface Pro. Then $\frac{2}{3}y$ = the width of the Surface Pro. The diagonal of a 12-inch Surface Pro is 12 inches, so by the Pythagorean theorem we have:

$$y^2 + \left(\frac{2}{3}y\right)^2 = 12.2^2$$

$$y^2 + \frac{4}{9}y^2 = 151.29$$

$$9\left(y^2 + \frac{4}{9}y^2\right) = 9(151.29)$$

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$$9y^2 + 4y^2 = 1361.61$$
$$13y^2 = 1361.61$$
$$y^2 = \frac{1361.61}{13}$$
$$y = \pm\sqrt{\frac{1361.61}{13}} \approx \pm 10.23$$

Since the length cannot be negative, the length of the Surface Pro is 10.23 inches and the width is $\frac{2}{3}\sqrt{\frac{1361.61}{13}} \approx 6.82$ inches. Thus, the area of the 12.3-inch 3:2 format Surface Pro is $\sqrt{\frac{1361.61}{13}} \cdot \frac{2}{3}\sqrt{\frac{1361.61}{13}}$ ≈ 69.83 square inches.

The iPad Pro format has the larger screen since its area is larger.

110. Let x = the length of a 7.9-inch iPad Mini in a 4:3 format.

Then $\frac{3}{4}x$ = the width of the iPad. The diagonal of the 7.9-inch iPad is 7.9 inches, so by the Pythagorean theorem we have:

$$x^2 + \left(\frac{3}{4}x\right)^2 = 7.9^2$$
$$x^2 + \frac{9}{16}x^2 = 62.41$$
$$16\left(x^2 + \frac{9}{16}x^2\right) = 16(62.41)$$
$$16x^2 + 9x^2 = 998.56$$
$$25x^2 = 998.56$$
$$x^2 = 39.9424$$
$$x = \pm\sqrt{39.9424} = \pm 6.32$$

Since the length cannot be negative, the length of the iPad is 6.32 inches and the width is $\frac{3}{4}(6.32) = 4.74$ inches. Thus, the area of the iPad is $(6.32)(4.74) = 29.9568$ square inches.

Let y = the length of a 8-inch 16:10 format Amazon Fire HD 8™. Then $\frac{10}{16}y$ = the width of the Fire. The diagonal of a 8-inch Fire is 8 inches, so by the Pythagorean theorem we have:

$$y^2 + \left(\frac{10}{16}y\right)^2 = 8^2$$
$$y^2 + \frac{100}{256}y^2 = 64$$
$$256\left(y^2 + \frac{100}{256}y^2\right) = 256(64)$$
$$256y^2 + 100y^2 = 16384$$
$$356y^2 = 16384$$
$$y^2 = \frac{16384}{356}$$
$$y = \pm\sqrt{\frac{16384}{356}} \approx \pm 6.78399$$

Since the length cannot be negative, the length of the Fire is $\sqrt{\frac{16384}{356}} \approx 6.78399$ inches and the width is $\frac{10}{16}\sqrt{\frac{16384}{356}} \approx 4.240$ inches. Thus, the area of the Amazon Fire is $(6.78399)(4.240) \approx 28.76$ square inches.

The iPad Mini™ 4:3 format has the larger screen since its area is larger.

111. Let h be 1.1. Then

$$1.1 = -0.00025x^2 + 0.04x$$
$$0 = -0.00025x^2 + 0.04x - 1.1$$
$$x = \frac{-0.04 \pm \sqrt{(0.04)^2 - 4(-0.00025)(-1.1)}}{2(-0.00025)}$$
$$= 35.3 \text{ ft or } 124.7 \text{ ft}$$

124.7 ft does not make sense in the context of the problem, so the answer is 35.3 ft.

112. Since d is expressed in 1000's we will set d = 15 and solve for x using the Quadratic Formula.

$$d = -0.012x^2 + 0.828x + 15.750$$
$$25 = -0.012x^2 + 0.828x + 15.750$$
$$0 = -0.012x^2 + 0.828x - 9.25$$
$$x = \frac{-0.828 \pm \sqrt{(0.828)^2 - 4(-0.012)(-9.25)}}{2(-0.012)}$$
$$= \frac{-0.828 \pm \sqrt{.241584}}{-0.024}$$
$$x \approx 54.98 \text{ or } x \approx 14.02$$

So the nearest year when the difference was \$25,000 occurred about 14 years after 1980 or 1994. The value 55 has no meaning since it is in the future.

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113. We will set g = 2.97 and solve for h using the Quadratic Formula.

$$g = -0.0006x^2 + 0.015x + 3.04$$
$$2.97 = -0.0006x^2 + 0.015x + 3.04$$
$$0 = -0.0006x^2 + 0.015x + 0.07$$
$$x = \frac{-0.015 \pm \sqrt{(0.015)^2 - 4(-0.0006)(0.07)}}{2(-0.0006)}$$
$$= \frac{-0.015 \pm \sqrt{0.000393}}{-0.0012}$$
$$x \approx 29 \text{ or } x \approx -4.02$$

So the estimated numbers of hours worked by a student with a GPA of 2.97 is 29 hours. The value -4.02 has no meaning since it is negative.

114. Let x be the numbers of members in the fraternity and s be the share paid by each member. Then $s = \frac{1470}{x}$. If there are 7 members who cannot contribute then the share goes up by \$5. So we have the following equation:

$$s + 5 = \frac{1470}{x - 7} \text{ or } (s+5)(x-7) = 1470$$

Solving these two equations together:

$$(s+5)(x-7) = 1470 \text{ and } s = \frac{1470}{x}$$
$$\left(\frac{1470}{x} + 5\right)(x-7) = 1470$$
$$1470 - \frac{10290}{x} + 5x - 35 = 1470$$
$$5x - \frac{10290}{x} - 35 = 0$$
$$5x^2 - 35x - 10290 = 0$$

$$5x^2 - 35x - 10290 = 0$$
$$x^2 - 7x - 2058 = 0$$
$$(x+42)(x-49) = 0$$
$$x = -42 \text{ or } x = 49$$

Since x is the number of members, it must be positive so the number of members is 49.

115. Let a be the age the individual is able to start saving money. Then we need to find where the models are equal. Solving these two equations together:

$$-25a^2 + 2400a - 30700 = 160a + 7840$$
$$25a^2 - 2240a + 38540 = 0$$
$$a = \frac{2240 \pm \sqrt{(2240)^2 - 4(25)(38540)}}{2(25)}$$
$$a = \frac{2240 \pm \sqrt{1163600}}{50}$$
$$a = \frac{2240 \pm 1078.7}{50}$$
$$a = \frac{2240 + 1078.7}{50} \text{ or } a = \frac{2240 - 1078.7}{50}$$
$$a = 66.4 \text{ or } a = 23.2$$

Since x is the age to start saving, it makes sense that the answer is approximate at age 23.

116. We will set the equation equal to 10 and solve:

$$0.003x^2 - 0.034x + 8.086 = 10$$
$$0.003x^2 - 0.034x - 1.914 = 0$$
$$x = \frac{0.034 \pm \sqrt{(-0.034)^2 - 4(0.003)(-1.914)}}{2(0.003)}$$
$$x = \frac{0.034 \pm \sqrt{.024124}}{0.006}$$
$$x = \frac{0.034 \pm .15532}{0.006}$$
$$x = \frac{0.034 - 0.15532}{0.006} \text{ or } x = \frac{0.034 + 0.15532}{0.006}$$
$$x = -20.22 \text{ or } x = 31.55$$

The percentage will reach 10% approximately 32 years after 1960 which is 1992.

117.
$$\frac{1}{2}n(n+1) = 703$$
$$n(n+1) = 1406$$
$$n^2 + n - 1406 = 0$$
$$(n-37)(n+38) = 0$$
$$n = 37 \text{ or } n = -38$$

Since the number of consecutive integers cannot be negative, we discard the negative value. We must add 37 consecutive integers, beginning at 1, in order to get a sum of 703.

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118. $\frac{1}{2}n(n-3)=65$

$n(n-3)=130$

$n^2-3n-130=0$

$(n-13)(n+10)=0$

$n=13 \quad \text{or} \quad n=-10$

Since the number of sides cannot be negative, we discard the negative value. A polygon with 65 diagonals will have 13 sides.

$\frac{1}{2}n(n-3)=80$

$n(n-3)=160$

$n^2-3n-160=0$

$a=1, b=-3, c=-160$

$n=\frac{3\pm\sqrt{(-3)^2-4(1)(-160)}}{2(1)}=\frac{3\pm\sqrt{646}}{2}$

Neither solution is an integer, so there is no polygon that has 80 diagonals.

119. The roots of a quadratic equation are

$x_1=\frac{-b-\sqrt{b^2-4ac}}{2a}$ and $x_2=\frac{-b+\sqrt{b^2-4ac}}{2a}$

$x_1+x_2=\frac{-b-\sqrt{b^2-4ac}}{2a}+\frac{-b+\sqrt{b^2-4ac}}{2a}$

$=\frac{-b-\sqrt{b^2-4ac}-b+\sqrt{b^2-4ac}}{2a}$

$=\frac{-2b}{2a}$

$=-\frac{b}{a}$

120. The roots of a quadratic equation are

$x_1=\frac{-b-\sqrt{b^2-4ac}}{2a}$ and $x_2=\frac{-b+\sqrt{b^2-4ac}}{2a}$

$x_1\cdot x_2=\left(\frac{-b-\sqrt{b^2-4ac}}{2a}\right)\left(\frac{-b+\sqrt{b^2-4ac}}{2a}\right)$

$=\frac{(-b)^2-\left(\sqrt{b^2-4ac}\right)^2}{(2a)^2}=\frac{b^2-b^2+4ac}{4a^2}$

$=\frac{4ac}{4a^2}$

$=\frac{c}{a}$

121. In order to have one repeated solution, we need the discriminant to be 0.

$b^2-4ac=0$

$1^2-4(k)(k)=0$

$1-4k^2=0$

$4k^2=1$

$k^2=\frac{1}{4}$

$k=\pm\sqrt{\frac{1}{4}}$

$k=\frac{1}{2} \quad \text{or} \quad k=-\frac{1}{2}$

122. In order to have one repeated solution, we need the discriminant to be 0.

$b^2-4ac=0$

$(-k)^2-4(1)(4)=0$

$k^2-16=0$

$(k-4)(k+4)=0$

$k=4 \quad \text{or} \quad k=-4$

123. For $ax^2+bx+c=0$:

$x=\frac{-b\pm\sqrt{b^2-4ac}}{2a}$

For $ax^2-bx+c=0$:

$x=\frac{b\pm\sqrt{(-b)^2-4ac}}{2a}$

$=-\left(\frac{-b\pm\sqrt{b^2-4ac}}{2a}\right)$

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124. For $ax^2+bx+c=0$:

$$x_1=\frac{-b-\sqrt{b^2-4ac}}{2a} \text{ and } x_2=\frac{-b+\sqrt{b^2-4ac}}{2a}$$

For $cx^2+bx+a=0$:

$$x_1^*=\frac{-b-\sqrt{b^2-4(c)(a)}}{2c}=\frac{-b-\sqrt{b^2-4ac}}{2c}$$

$$=\frac{-b-\sqrt{b^2-4ac}}{2c}\cdot\frac{-b+\sqrt{b^2-4ac}}{-b+\sqrt{b^2-4ac}}$$

$$=\frac{b^2-\left(b^2-4ac\right)}{2c\left(-b+\sqrt{b^2-4ac}\right)}=\frac{4ac}{2c\left(-b+\sqrt{b^2-4ac}\right)}$$

$$=\frac{2a}{-b+\sqrt{b^2-4ac}}$$

$$=\frac{1}{x_2}$$

and

$$x_2^*=\frac{-b+\sqrt{b^2-4(c)(a)}}{2c}=\frac{-b+\sqrt{b^2-4ac}}{2c}$$

$$=\frac{-b+\sqrt{b^2-4ac}}{2c}\cdot\frac{-b-\sqrt{b^2-4ac}}{-b-\sqrt{b^2-4ac}}$$

$$=\frac{b^2-\left(b^2-4ac\right)}{2c\left(-b-\sqrt{b^2-4ac}\right)}=\frac{4ac}{2c\left(-b-\sqrt{b^2-4ac}\right)}$$

$$=\frac{2a}{-b-\sqrt{b^2-4ac}}$$

$$=\frac{1}{x_1}$$

125. If x = original width and y = original length, then $xy=1$ or $x=\frac{1}{y}$. The ratio of side lengths is $\frac{x}{y}=\frac{1}{y^2}$. Folding along the longest side results in sides of length $x=\frac{1}{y}$ and $\frac{y}{2}$ whose ratio is

$$\frac{\frac{y}{2}}{\frac{1}{y}}=\frac{y^2}{2}$$

Equating the ratios gives

$$\frac{1}{y^2}=\frac{y^2}{2}$$

$$y^4=2$$

$$y=\sqrt[4]{2} \text{ m}$$

So

$$x=\frac{1}{\sqrt[4]{2}}=\frac{\sqrt[4]{8}}{2} \text{ m.}$$

126. **a.** $x^2=9$ and $x=3$ are not equivalent because they do not have the same solution set. In the first equation we can also have $x=-3$.

b. $x=\sqrt{9}$ and $x=3$ are equivalent because $\sqrt{9}=3$.

c. $(x-1)(x-2)=(x-1)^2$ and $x-2=x-1$ are not equivalent because they do not have the same solution set.
The first equation has the solution set $\{1\}$ while the second equation has no solutions.

127. Answers will vary. Methods may include the quadratic formula, completing the square, graphing, etc.

128. Answers will vary. Knowing the discriminant allows us to know how many real solutions the equation will have.

129. Answers will vary. One possibility:
Two distinct: $x^2-3x-18=0$
One repeated: $x^2-14x+49=0$
No real: $x^2+x+4=0$

130. Answers will vary.

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Section 1.3

1. Integers: $\{-3, 0\}$

Rationals: $\left\{-3, 0, \frac{6}{5}\right\}$

2. True; the set of real numbers consists of all rational and irrational numbers.

3. $$\frac{3}{2+\sqrt{3}} = \frac{3}{2+\sqrt{3}} \cdot \frac{2-\sqrt{3}}{2-\sqrt{3}} = \frac{3\left(2-\sqrt{3}\right)}{2^2-\left(\sqrt{3}\right)^2} = \frac{3\left(2-\sqrt{3}\right)}{4-3} = 3\left(2-\sqrt{3}\right)$$

4. real; imaginary; imaginary unit

5. False; the conjugate of $2+5i$ is $2-5i$.

6. True; the set of real numbers is a subset of the set of complex numbers.

7. False; if $2-3i$ is a solution of a quadratic equation with real coefficients, then its conjugate, $2+3i$, is also a solution.

8. b

9. a

10. c

11. $(2-3i)+(6+8i) = (2+6)+(-3+8)i = 8+5i$

12. $(4+5i)+(-8+2i) = (4+(-8))+(5+2)i = -4+7i$

13. $(-3+2i)-(4-4i) = (-3-4)+(2-(-4))i = -7+6i$

14. $(3-4i)-(-3-4i) = (3-(-3))+(-4-(-4))i = 6+0i = 6$

15. $(2-5i)-(8+6i) = (2-8)+(-5-6)i = -6-11i$

16. $(-8+4i)-(2-2i) = (-8-2)+(4-(-2))i = -10+6i$

17. $3(2-6i) = 6-18i$

18. $-4(2+8i) = -8-32i$

19. $-3i(7+6i) = -21i-18i^2 = -21i-18(-1) = 18-21i$

20. $3i(-3+4i) = -9i+12i^2 = -9i+12(-1) = -12-9i$

21. $(3-4i)(2+i) = 6+3i-8i-4i^2 = 6-5i-4(-1) = 10-5i$

22. $(5+3i)(2-i) = 10-5i+6i-3i^2 = 10+i-3(-1) = 13+i$

23. $(-5-i)(-5+i) = 25-5i+5i-i^2 = 25-(-1) = 26$

24. $(-3+i)(3+i) = -9-3i+3i+i^2 = -9+(-1) = -10$

25. $$\frac{10}{3-4i} = \frac{10}{3-4i} \cdot \frac{3+4i}{3+4i} = \frac{30+40i}{9+12i-12i-16i^2} = \frac{30+40i}{9-16(-1)} = \frac{30+40i}{25} = \frac{30}{25}+\frac{40}{25}i = \frac{6}{5}+\frac{8}{5}i$$

26. $$\frac{13}{5-12i} = \frac{13}{5-12i} \cdot \frac{5+12i}{5+12i} = \frac{65+156i}{25+60i-60i-144i^2} = \frac{65+156i}{25-144(-1)} = \frac{65+156i}{169} = \frac{65}{169}+\frac{156}{169}i = \frac{5}{13}+\frac{12}{13}i$$

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27. $\dfrac{2+i}{i} = \dfrac{2+i}{i}\cdot\dfrac{-i}{-i} = \dfrac{-2i-i^2}{-i^2}$

$= \dfrac{-2i-(-1)}{-(-1)} = \dfrac{1-2i}{1} = 1-2i$

28. $\dfrac{2-i}{-2i} = \dfrac{2-i}{-2i}\cdot\dfrac{i}{i} = \dfrac{2i-i^2}{-2i^2}$

$= \dfrac{2i-(-1)}{-2(-1)} = \dfrac{1+2i}{2} = \dfrac{1}{2}+i$

29. $\dfrac{6-i}{1+i} = \dfrac{6-i}{1+i}\cdot\dfrac{1-i}{1-i} = \dfrac{6-6i-i+i^2}{1-i+i-i^2}$

$= \dfrac{6-7i+(-1)}{1-(-1)} = \dfrac{5-7i}{2} = \dfrac{5}{2}-\dfrac{7}{2}i$

30. $\dfrac{2+3i}{1-i} = \dfrac{2+3i}{1-i}\cdot\dfrac{1+i}{1+i} = \dfrac{2+2i+3i+3i^2}{1+i-i-i^2}$

$= \dfrac{2+5i+3(-1)}{1-(-1)} = \dfrac{-1+5i}{2} = -\dfrac{1}{2}+\dfrac{5}{2}i$

31. $\left(\dfrac{1}{2}+\dfrac{\sqrt{3}}{2}i\right)^2 = \dfrac{1}{4}+2\left(\dfrac{1}{2}\right)\left(\dfrac{\sqrt{3}}{2}i\right)+\dfrac{3}{4}i^2$

$= \dfrac{1}{4}+\dfrac{\sqrt{3}}{2}i+\dfrac{3}{4}(-1) = -\dfrac{1}{2}+\dfrac{\sqrt{3}}{2}i$

32. $\left(\dfrac{\sqrt{3}}{2}-\dfrac{1}{2}i\right)^2 = \dfrac{3}{4}-2\left(\dfrac{\sqrt{3}}{2}\right)\left(\dfrac{1}{2}i\right)+\dfrac{1}{4}i^2$

$= \dfrac{3}{4}-\dfrac{\sqrt{3}}{2}i+\dfrac{1}{4}(-1) = \dfrac{1}{2}-\dfrac{\sqrt{3}}{2}i$

33. $(1+i)^2 = 1+2i+i^2 = 1+2i+(-1) = 2i$

34. $(1-i)^2 = 1-2i+i^2 = 1-2i+(-1) = -2i$

35. $i^{23} = i^{22+1} = i^{22}\cdot i = \left(i^2\right)^{11}\cdot i = (-1)^{11}i = -i$

36. $i^{14} = \left(i^2\right)^7 = (-1)^7 = -1$

37. $i^{-20} = \dfrac{1}{i^{20}} = \dfrac{1}{i^{20}} = \dfrac{1}{(i^2)^{10}}$

$= \dfrac{1}{(-1)^{10}} = \dfrac{1}{1} = 1$

38. $i^{-23} = \dfrac{1}{i^{23}} = \dfrac{1}{i^{22+1}} = \dfrac{1}{i^{22}\cdot i} = \dfrac{1}{(i^2)^{11}\cdot i}$

$= \dfrac{1}{(-1)^{11}i} = \dfrac{1}{-i} = \dfrac{1}{-i}\cdot\dfrac{i}{i} = \dfrac{i}{-i^2} = \dfrac{i}{-(-1)} = i$

39. $i^6-5 = \left(i^2\right)^3-5 = (-1)^3-5 = -1-5 = -6$

40. $4+i^3 = 4+i^2\cdot i = 4+(-1)i = 4-i$

41. $6i^3-4i^5 = i^3(6-4i^2)$

$= i^2\cdot i(6-4(-1)) = -1\cdot i(10) = -10i$

42. $4i^3-2i^2+1 = 4i^2\cdot i-2i^2+1$

$= 4(-1)i-2(-1)+1$

$= -4i+2+1$

$= 3-4i$

43. $(1+i)^3 = (1+i)(1+i)(1+i) = (1+2i+i^2)(1+i)$

$= (1+2i-1)(1+i) = 2i(1+i)$

$= 2i+2i^2 = 2i+2(-1)$

$= -2+2i$

44. $(3i)^4+1 = 81i^4+1 = 81(1)+1 = 82$

45. $i^7(1+i^2) = i^7(1+(-1)) = i^7(0) = 0$

46. $2i^4(1+i^2) = 2(1)(1+(-1)) = 2(0) = 0$

47. $i^8+i^6-i^4-i^2 = \left(i^2\right)^4+\left(i^2\right)^3+\left(i^2\right)^2+i^2$

$= (-1)^4+(-1)^3+(-1)^2-1$

$= 1-1+1-1$

$= 0$

48. $i^7+i^5+i^3+i = \left(i^2\right)^3\cdot i+\left(i^2\right)^2\cdot i+i^2\cdot i+i$

$= (-1)^3\cdot i+(-1)^2\cdot i+(-1)\cdot i+i$

$= -i+i-i+i$

$= 0$

49. $\sqrt{-4} = 2i$

50. $\sqrt{-9} = 3i$

51. $\sqrt{-25} = 5i$

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52. $\sqrt{-64} = 8i$

53. $\sqrt{-12} = i\sqrt{4 \cdot 3} = 2\sqrt{3}i$

54. $\sqrt{-18} = i\sqrt{9 \cdot 2} = 3\sqrt{2}i$

55. $\sqrt{-200} = i\sqrt{100 \cdot 2} = 10\sqrt{2}i$

56. $\sqrt{-45} = i\sqrt{9 \cdot 5} = 3\sqrt{5}i$

57. $\sqrt{(3+4i)(4i-3)} = \sqrt{12i - 9 + 16i^2 - 12i}$
$= \sqrt{-9 + 16(-1)}$
$= \sqrt{-25}$
$= 5i$

58. $\sqrt{(4+3i)(3i-4)} = \sqrt{12i - 16 + 9i^2 - 12i}$
$= \sqrt{-16 + 9(-1)}$
$= \sqrt{-25}$
$= 5i$

59. $x^2 + 4 = 0$
$x^2 = -4$
$x = \pm\sqrt{-4}$
$x = \pm 2i$
The solution set is $\{-2i, 2i\}$.

60. $x^2 - 4 = 0$
$(x+2)(x-2) = 0$
$x = -2$ or $x = 2$
The solution set is $\{-2, 2\}$.

61. $x^2 - 16 = 0$
$(x+4)(x-4) = 0$
$x = -4$ or $x = 4$
The solution set is $\{-4, 4\}$.

62. $x^2 + 25 = 0$
$x^2 = -25$
$x = \pm\sqrt{-25} = \pm 5i$
The solution set is $\{-5i, 5i\}$.

63. $x^2 - 6x + 13 = 0$
$a = 1, b = -6, c = 13,$
$b^2 - 4ac = (-6)^2 - 4(1)(13) = 36 - 52 = -16$
$x = \dfrac{-(-6) \pm \sqrt{-16}}{2(1)} = \dfrac{6 \pm 4i}{2} = 3 \pm 2i$
The solution set is $\{3 - 2i, 3 + 2i\}$.

64. $x^2 + 4x + 8 = 0$
$a = 1, b = 4, c = 8$
$b^2 - 4ac = 4^2 - 4(1)(8) = 16 - 32 = -16$
$x = \dfrac{-4 \pm \sqrt{-16}}{2(1)} = \dfrac{-4 \pm 4i}{2} = -2 \pm 2i$
The solution set is $\{-2 - 2i, -2 + 2i\}$.

65. $x^2 - 6x + 10 = 0$
$a = 1, b = -6, c = 10$
$b^2 - 4ac = (-6)^2 - 4(1)(10) = 36 - 40 = -4$
$x = \dfrac{-(-6) \pm \sqrt{-4}}{2(1)} = \dfrac{6 \pm 2i}{2} = 3 \pm i$
The solution set is $\{3 - i, 3 + i\}$.

66. $x^2 - 2x + 5 = 0$
$a = 1, b = -2, c = 5$
$b^2 - 4ac = (-2)^2 - 4(1)(5) = 4 - 20 = -16$
$x = \dfrac{-(-2) \pm \sqrt{-16}}{2(1)} = \dfrac{2 \pm 4i}{2} = 1 \pm 2i$
The solution set is $\{1 - 2i, 1 + 2i\}$.

67. $25x^2 - 10x + 2 = 0$
$a = 25, b = -10, c = 2$
$b^2 - 4ac = (-10)^2 - 4(25)(2) = 100 - 200 = -100$
$x = \dfrac{-(-10) \pm \sqrt{-100}}{50} = \dfrac{10 \pm 10i}{50} = \dfrac{1}{5} \pm \dfrac{1}{5}i$
The solution set is $\left\{ \dfrac{1}{5} - \dfrac{1}{5}i, \dfrac{1}{5} + \dfrac{1}{5}i \right\}$.

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68. $10x^2+6x+1=0$

$a=10, b=6, c=1$

$b^2-4ac=6^2-4(10)(1)=36-40=-4$

$x=\dfrac{-6\pm\sqrt{-4}}{2(10)}=\dfrac{-6\pm 2i}{20}=-\dfrac{3}{10}\pm\dfrac{1}{10}i$

The solution set is $\left\{-\dfrac{3}{10}-\dfrac{1}{10}i,\ -\dfrac{3}{10}+\dfrac{1}{10}i\right\}$.

69. $5x^2+1=2x$

$5x^2-2x+1=0$

$a=5, b=-2, c=1$

$b^2-4ac=(-2)^2-4(5)(1)=4-20=-16$

$x=\dfrac{-(-2)\pm\sqrt{-16}}{2(5)}=\dfrac{2\pm 4i}{10}=\dfrac{1}{5}\pm\dfrac{2}{5}i$

The solution set is $\left\{\dfrac{1}{5}-\dfrac{2}{5}i,\ \dfrac{1}{5}+\dfrac{2}{5}i\right\}$.

70. $13x^2+1=6x$

$13x^2-6x+1=0$

$a=13, b=-6, c=1$

$b^2-4ac=(-6)^2-4(13)(1)=36-52=-16$

$x=\dfrac{-(-6)\pm\sqrt{-16}}{2(13)}=\dfrac{6\pm 4i}{26}=\dfrac{3}{13}\pm\dfrac{2}{13}i$

The solution set is $\left\{\dfrac{3}{13}-\dfrac{2}{13}i,\dfrac{3}{13}+\dfrac{2}{13}i\right\}$.

71. $x^2+x+1=0$

$a=1, b=1, c=1,$

$b^2-4ac=1^2-4(1)(1)=1-4=-3$

$x=\dfrac{-1\pm\sqrt{-3}}{2(1)}=\dfrac{-1\pm\sqrt{3}\,i}{2}=-\dfrac{1}{2}\pm\dfrac{\sqrt{3}}{2}i$

The solution set is $\left\{-\dfrac{1}{2}-\dfrac{\sqrt{3}}{2}i,\ -\dfrac{1}{2}+\dfrac{\sqrt{3}}{2}i\right\}$.

72. $x^2-x+1=0$

$a=1, b=-1, c=1$

$b^2-4ac=(-1)^2-4(1)(1)=1-4=-3$

$x=\dfrac{-(-1)\pm\sqrt{-3}}{2(1)}=\dfrac{1\pm\sqrt{3}\,i}{2}=\dfrac{1}{2}\pm\dfrac{\sqrt{3}}{2}i$

The solution set is $\left\{\dfrac{1}{2}-\dfrac{\sqrt{3}}{2}i,\ \dfrac{1}{2}+\dfrac{\sqrt{3}}{2}i\right\}$.

73. $x^3-64=0$

$(x-4)\left(x^2+4x+16\right)=0$

$x-4=0\Rightarrow x=4$

or $x^2+4x+16=0$

$a=1, b=4, c=16$

$b^2-4ac=4^2-4(1)(16)=16-64=-48$

$x=\dfrac{-4\pm\sqrt{-48}}{2(1)}=\dfrac{-4\pm 4\sqrt{3}\,i}{2}=-2\pm 2\sqrt{3}i$

The solution set is $\left\{4,-2-2\sqrt{3}i,-2+2\sqrt{3}i\right\}$.

74. $x^3+27=0$

$(x+3)\left(x^2-3x+9\right)=0$

$x+3=0\Rightarrow x=-3$

or $x^2-3x+9=0$

$a=1, b=-3, c=9$

$b^2-4ac=(-3)^2-4(1)(9)=9-36=-27$

$x=\dfrac{-(-3)\pm\sqrt{-27}}{2(1)}=\dfrac{3\pm 3\sqrt{3}\,i}{2}=\dfrac{3}{2}\pm\dfrac{3\sqrt{3}}{2}i$

The solution set is $\left\{-3,\dfrac{3}{2}-\dfrac{3\sqrt{3}}{2}i,\dfrac{3}{2}+\dfrac{3\sqrt{3}}{2}i\right\}$.

75. $x^4=16$

$x^4-16=0$

$\left(x^2-4\right)\left(x^2+4\right)=0$

$(x-2)(x+2)\left(x^2+4\right)=0$

$x-2=0$ or $x+2=0$ or $x^2+4=0$

$x=2$ or $x=-2$ or $x^2=-4$

$x=2$ or $x=-2$ or $x=\pm\sqrt{-4}=\pm 2i$

The solution set is $\{-2,2,-2i,2i\}$.

76. $x^4=1$

$x^4-1=0$

$\left(x^2-1\right)\left(x^2+1\right)=0$

$(x-1)(x+1)\left(x^2+1\right)=0$

$x-1=0$ or $x+1=0$ or $x^2+1=0$

$x=1$ or $x=-1$ or $x^2=-1$

$x=1$ or $x=-1$ or $x=\pm\sqrt{-1}=\pm i$

The solution set is $\{-1,1,-i,i\}$.

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77. $x^4 + 13x^2 + 36 = 0$

$(x^2 + 9)(x^2 + 4) = 0$

$x^2 + 9 = 0 \quad \text{or} \quad x^2 + 4 = 0$

$x^2 = -9 \quad \text{or} \quad x^2 = -4$

$x = \pm\sqrt{-9} \quad \text{or} \quad x = \pm\sqrt{-4}$

$x = \pm 3i \quad \text{or} \quad x = \pm 2i$

The solution set is $\{-3i, 3i, -2i, 2i\}$.

78. $x^4 + 3x^2 - 4 = 0$

$(x^2 - 1)(x^2 + 4) = 0$

$(x-1)(x+1)(x^2 + 4) = 0$

$x - 1 = 0 \text{ or } x + 1 = 0 \text{ or } x^2 + 4 = 0$

$x = 1 \text{ or } x = -1 \text{ or } x^2 = -4$

$x = 1 \text{ or } x = -1 \text{ or } x = \pm\sqrt{-4} = \pm 2i$

The solution set is $\{-1, 1, -2i, 2i\}$.

79. $3x^2 - 3x + 4 = 0$

$a = 3, b = -3, c = 4$

$b^2 - 4ac = (-3)^2 - 4(3)(4) = 9 - 48 = -39$

The equation has two complex solutions that are conjugates of each other.

80. $2x^2 - 4x + 1 = 0$

$a = 2, b = -4, c = 1$

$b^2 - 4ac = (-4)^2 - 4(2)(1) = 16 - 8 = 8$

The equation has two unequal real number solutions.

81. $2x^2 + 3x = 4$

$2x^2 + 3x - 4 = 0$

$a = 2, b = 3, c = -4$

$b^2 - 4ac = 3^2 - 4(2)(-4) = 9 + 32 = 41$

The equation has two unequal real solutions.

82. $x^2 + 6 = 2x$

$x^2 - 2x + 6 = 0$

$a = 1, b = -2, c = 6$

$b^2 - 4ac = (-2)^2 - 4(1)(6) = 4 - 24 = -20$

The equation has two complex solutions that are conjugates of each other.

83. $9x^2 - 12x + 4 = 0$

$a = 9, b = -12, c = 4$

$b^2 - 4ac = (-12)^2 - 4(9)(4) = 144 - 144 = 0$

The equation has a repeated real solution.

84. $4x^2 + 12x + 9 = 0$

$a = 4, b = 12, c = 9$

$b^2 - 4ac = 12^2 - 4(4)(9) = 144 - 144 = 0$

The equation has a repeated real solution.

85. The other solution is $\overline{2 + 3i} = 2 - 3i$.

86. The other solution is $\overline{4 - i} = 4 + i$.

87. $z + \overline{z} = 3 - 4i + \overline{3 - 4i} = 3 - 4i + 3 + 4i = 6$

88. $w - \overline{w} = 8 + 3i - \left(\overline{8 + 3i}\right)$

$= 8 + 3i - (8 - 3i)$

$= 8 + 3i - 8 + 3i$

$= 0 + 6i = 6i$

89. $z \cdot \overline{z} = (3 - 4i)(\overline{3 - 4i})$

$= (3 - 4i)(3 + 4i)$

$= 9 + 12i - 12i - 16i^2$

$= 9 - 16(-1) = 25$

90. $\overline{z - w} = \overline{3 - 4i - (8 + 3i)}$

$= \overline{3 - 4i - 8 - 3i}$

$= \overline{-5 - 7i}$

$= -5 + 7i$

91. $Z = \dfrac{V}{I} = \dfrac{18 + i}{3 - 4i} = \dfrac{18 + i}{3 - 4i} \cdot \dfrac{3 + 4i}{3 + 4i}$

$= \dfrac{54 + 72i + 3i + 4i^2}{9 + 12i - 12i - 16i^2} = \dfrac{54 + 75i - 4}{9 + 16}$

$= \dfrac{50 + 75i}{25} = 2 + 3i$

The impedance is $2 + 3i$ ohms.

92. $\dfrac{1}{Z} = \dfrac{1}{Z_1} + \dfrac{1}{Z_2} = \dfrac{1}{2 + i} + \dfrac{1}{4 - 3i} = \dfrac{(4 - 3i) + (2 + i)}{(2 + i)(4 - 3i)}$

$= \dfrac{6 - 2i}{8 - 6i + 4i - 3i^2} = \dfrac{6 - 2i}{8 - 2i + 3} = \dfrac{6 - 2i}{11 - 2i}$

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So, $Z = \dfrac{11-2i}{6-2i} = \dfrac{11-2i}{6-2i}\cdot\dfrac{6+2i}{6+2i}$

$= \dfrac{66+22i-12i-4i^2}{36+12i-12i-4i^2} = \dfrac{66+10i+4}{36+4}$

$= \dfrac{70+10i}{40} = \dfrac{7}{4}+\dfrac{1}{4}i$

The total impedance is $\dfrac{7}{4}+\dfrac{1}{4}i$ ohms.

93. $z+\overline{z} = (a+bi)+(\overline{a+bi})$

$= a+bi+a-bi$

$= 2a$

$z-\overline{z} = a+bi-(\overline{a+bi})$

$= a+bi-(a-bi)$

$= a+bi-a+bi$

$= 2bi$

94. $\overline{\overline{z}} = \overline{\overline{a+bi}} = \overline{a-bi} = a+bi = z$

95. $\overline{z+w} = \overline{(a+bi)+(c+di)}$

$= \overline{(a+c)+(b+d)i}$

$= (a+c)-(b+d)i$

$= (a-bi)+(c-di)$

$= \overline{a+bi}+\overline{c+di}$

$= \overline{z}+\overline{w}$

96. $\overline{z\cdot w} = \overline{(a+bi)\cdot(c+di)}$

$= \overline{ac+adi+bci+bdi^2}$

$= \overline{(ac-bd)+(ad+bc)i}$

$= (ac-bd)-(ad+bc)i$

$\overline{z}\cdot\overline{w} = \overline{a+bi}\cdot\overline{c+di}$

$= (a-bi)(c-di)$

$= ac-adi-bci+bdi^2$

$= (ac-bd)-(ad+bc)i$

97. $(a+bi)^2 = -(a-bi)^2$

$a^2+2abi+(bi)^2 = -\left(a^2-2abi+(bi)^2\right)$

$a^2+2abi+b^2i^2 = -\left(a^2-2abi+b^2i^2\right)$

$a^2+2abi-b^2 = -a^2+2abi+b^2$

$a^2-b^2 = -(a^2-b^2)$

$2(a^2-b^2) = 0$

$a^2 = b^2 \rightarrow b = \pm a$

Any complex number of the form $a+ai$ or $a-ai$ will work.

98. Let $u = \sqrt[3]{2}$ in $x^3+2=0$ so that $x^3+u^3=0$. Then, $(x+u)(x^2-ux+u^2)=0$. From the first factor we find $x = -u = -\sqrt[3]{2}$. From the second factor, use the quadratic formula to get

$x = \dfrac{-(-u)\pm\sqrt{(-u)^2-4\cdot1\cdot u^2}}{2\cdot1}$

$= \dfrac{u\pm\sqrt{-3u^2}}{2} = \dfrac{u}{2}\pm\dfrac{u\sqrt{3}}{2}i = \dfrac{\sqrt[3]{2}}{2}\pm\dfrac{\sqrt[3]{2}\sqrt{3}}{2}i$

The solution set is:

$\left\{-\sqrt[3]{2}, \dfrac{\sqrt[3]{2}}{2}\pm\dfrac{\sqrt[3]{2}\sqrt{3}}{2}i\right\}$

99. $(x+5)(y-5) = (x+y)^2$; let $u = x+5$ (so $x = u-5$ and $v = y-5$ so $y = v+5$.

Substituting gives $uv = (u+v)^2$ or

$u^2+uv+v^2 = 0$ which is quadratic in u. Using the quadratic formula gives

$x = \dfrac{-v\pm\sqrt{v^2-4\cdot1\cdot v^2}}{2\cdot1} = \dfrac{-v\pm|v|\sqrt{-3}}{2}$. Since x is a real number, u must also be a real number. This is only possible if v = 0 which then makes u = 0. Therefore, $x = 0-5 = -5$ and $y = 0+5 = 5$, so $x-y = -5-5 = -10$

100 – 102. Answers will vary.

103. Answers will vary. A complex number is the sum or difference of two numbers (real and imaginary parts of the complex number) just as a binomial is the sum or difference of two monomial terms. We multiply two binomials by using the FOIL method, an approach we can also use to multiply two complex numbers.

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104. Although the set of real numbers is a subset of the set of complex numbers, not all rules that work in the real number system can be used in the larger complex number system. The rule that allows us to write the product of two square roots as the square root of the product only works in the real number system. That is, $\sqrt{a}\cdot\sqrt{b}=\sqrt{ab}$ only when $\sqrt{a}$ and $\sqrt{b}$ are real numbers. In the complex number system we must first convert the radicals to complex form. In this case this means we need to write $\sqrt{-9}$ as $\sqrt{-1\cdot 9}=\sqrt{9}\cdot\sqrt{-1}=3i$. Then we can multiply to get $\sqrt{-9}\cdot\sqrt{-9}=3i\cdot 3i=9i^2=9(-1)=-9$.

Section 1.4

1. True

2. $\left(\sqrt[3]{x}\right)^3=x$

3. $6x^3-2x^2=2x^2(3x-1)$

4. False; you can also use the Quadratic Formula or completing the square.

5. quadratic in form

6. True

7. a

8. c

9.
$$\sqrt{2t-1}=1$$
$$\left(\sqrt{2t-1}\right)^2=1^2$$
$$2t-1=1$$
$$2t=2$$
$$t=1$$
Check: $\sqrt{2(1)-1}=\sqrt{1}=1$
The solution set is $\{1\}$.

10.
$$\sqrt{3t+4}=2$$
$$\left(\sqrt{3t+4}\right)^2=2^2$$
$$3t+4=4$$
$$3t=0$$
$$t=0$$
Check: $\sqrt{3(0)+4}=\sqrt{4}=2$
The solution set is $\{0\}$.

11. $\sqrt{3t+4}=-6$
Since the principal square root is never negative, the equation has no real solution.

12. $\sqrt{5t+3}=-2$
Since the principal square root is never negative, the equation has no real solution.

13.
$$\sqrt[3]{1-2x}-3=0$$
$$\sqrt[3]{1-2x}=3$$
$$\left(\sqrt[3]{1-2x}\right)^3=3^3$$
$$1-2x=27$$
$$-2x=26$$
$$x=-13$$
Check: $\sqrt[3]{1-2(-13)}-3=\sqrt[3]{27}-3=0$
The solution set is $\{-13\}$.

14.
$$\sqrt[3]{1-2x}-1=0$$
$$\sqrt[3]{1-2x}=1$$
$$\left(\sqrt[3]{1-2x}\right)^3=1^3$$
$$1-2x=1$$
$$-2x=0$$
$$x=0$$
Check: $\sqrt[3]{1-2(0)}-1=\sqrt[3]{1}-1=0$
The solution set is $\{0\}$.

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15. $\sqrt[5]{x^2+2x}=-1$

$\left(\sqrt[5]{x^2+2x}\right)^5=(-1)^5$

$x^2+2x=-1$

$x^2+2x+1=0$

$(x+1)^2=0$

$x+1=0$

$x=-1$

Check: $\sqrt[5]{(-1)^2+2(-1)}=\sqrt[5]{1-2}=\sqrt[5]{-1}=-1$

The solution set is $\{-1\}$.

16. $\sqrt[4]{x^2+16}=\sqrt{5}$

$\left(\sqrt[4]{x^2+16}\right)^4=\left(\sqrt{5}\right)^4$

$x^2+16=25$

$x^2=9$

$x=\pm 3$

Check -3: $\sqrt[4]{(-3)^2+16}=\sqrt[4]{9+16}=\sqrt[4]{25}=\sqrt{5}$

Check 3: $\sqrt[4]{(3)^2+16}=\sqrt[4]{9+16}=\sqrt[4]{25}=\sqrt{5}$

The solution set is $\{-3,3\}$.

17. $x=8\sqrt{x}$

$(x)^2=\left(8\sqrt{x}\right)^2$

$x^2=64x$

$x^2-64x=0$

$x(x-64)=0$

$x=0$ or $x=64$

Check 0: $0=8\sqrt{0}$, $0=0$ Check 64: $64=8\sqrt{64}$, $64=64$

The solution set is $\{0,64\}$.

18. $x=3\sqrt{x}$

$(x)^2=\left(3\sqrt{x}\right)^2$

$x^2=9x$

$x^2-9x=0$

$x(x-9)=0$

$x=0$ or $x=9$

Check 0: $0=3\sqrt{0}$, $0=0$ Check 9: $9=3\sqrt{9}$, $9=9$

The solution set is $\{0,9\}$.

19. $\sqrt{15-2x}=x$

$\left(\sqrt{15-2x}\right)^2=x^2$

$15-2x=x^2$

$x^2+2x-15=0$

$(x+5)(x-3)=0$

$x=-5$ or $x=3$

Check -5: $\sqrt{15-2(-5)}=\sqrt{25}=5\neq -5$

Check 3: $\sqrt{15-2(3)}=\sqrt{9}=3=3$

Disregard $x=-5$ as extraneous.

The solution set is $\{3\}$.

20. $\sqrt{12-x}=x$

$\left(\sqrt{12-x}\right)^2=x^2$

$12-x=x^2$

$x^2+x-12=0$

$(x+4)(x-3)=0$

$x=-4$ or $x=3$

Check -4: $\sqrt{12-(-4)}=\sqrt{16}=4\neq -4$

Check 3: $\sqrt{12-3}=\sqrt{9}=3=3$

Disregard $x=-4$ as extraneous.

The solution set is $\{3\}$.

21. $x=2\sqrt{x-1}$

$x^2=\left(2\sqrt{x-1}\right)^2$

$x^2=4(x-1)$

$x^2=4x-4$

$x^2-4x+4=0$

$(x-2)^2=0$

$x=2$

Check: $2=2\sqrt{2-1}$

$2=2$

The solution set is $\{2\}$.

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22. $x = 2\sqrt{-x-1}$

$x^2 = \left(2\sqrt{-x-1}\right)^2$

$x^2 = 4(-x-1)$

$x^2 = -4x-4$

$x^2 + 4x + 4 = 0$

$(x+2)^2 = 0$

$x = -2$

Check: $-2 = 2\sqrt{-(-2)-1}$

$-2 \neq 2$

The equation has no real solution.

23. $\sqrt{x^2 - x - 4} = x + 2$

$\left(\sqrt{x^2 - x - 4}\right)^2 = (x+2)^2$

$x^2 - x - 4 = x^2 + 4x + 4$

$-8 = 5x$

$-\frac{8}{5} = x$

Check: $\sqrt{\left(-\frac{8}{5}\right)^2 - \left(-\frac{8}{5}\right) - 4} = \left(-\frac{8}{5}\right) + 2$

$\sqrt{\frac{64}{25} + \frac{8}{5} - 4} = \frac{2}{5}$

$\sqrt{\frac{4}{25}} = \frac{2}{5}$

$\frac{2}{5} = \frac{2}{5}$

The solution set is $\left\{-\frac{8}{5}\right\}$.

24. $\sqrt{3 - x + x^2} = x - 2$

$\left(\sqrt{3 - x + x^2}\right)^2 = (x-2)^2$

$3 - x + x^2 = x^2 - 4x + 4$

$3x = 1$

$x = \frac{1}{3}$

Check: $\sqrt{3 - \left(\frac{1}{3}\right) + \left(\frac{1}{3}\right)^2} = \left(\frac{1}{3}\right) - 2$

$\sqrt{3 - \frac{1}{3} + \frac{1}{9}} = -\frac{5}{3}$

Since the principal square root is always a non-negative number; $x = \frac{1}{3}$ does not check.

Therefore this equation has no real solution.

25. $3 + \sqrt{3x+1} = x$

$\sqrt{3x+1} = x - 3$

$\left(\sqrt{3x+1}\right)^2 = (x-3)^2$

$3x + 1 = x^2 - 6x + 9$

$0 = x^2 - 9x + 8$

$0 = (x-1)(x-8)$

$x = 1$ or $x = 8$

Check 1: $3 + \sqrt{3(1)+1} = 3 + \sqrt{4} = 5 \neq 1$

Check 8: $3 + \sqrt{3(8)+1} = 3 + \sqrt{25} = 8 = 8$

Discard $x = 1$ as extraneous.

The solution set is $\{8\}$.

26. $2 + \sqrt{12 - 2x} = x$

$\sqrt{12 - 2x} = x - 2$

$\left(\sqrt{12 - 2x}\right)^2 = (x-2)^2$

$12 - 2x = x^2 - 4x + 4$

$0 = x^2 - 2x - 8$

$(x+2)(x-4) = 0$

$x = -2$ or $x = 4$

Check -2: $2 + \sqrt{12 - 2(-2)} = 2 + \sqrt{16} = 6 \neq -2$

Check 4: $2 + \sqrt{12 - 2(4)} = 2 + \sqrt{4} = 4 = 4$

Discard $x = -2$ as extraneous.

The solution set is $\{4\}$.

27. $\sqrt{3(x+10)} - 4 = x$

$\sqrt{3(x+10)} = x + 4$

$\left(\sqrt{3(x+10)}\right)^2 = (x+4)^2$

$3x + 30 = x^2 + 8x + 16$

$0 = x^2 + 5x - 14$

$0 = (x+7)(x-2)$

$x = -7$ or $x = 2$

Check -7: $\sqrt{3(-7+10)} - 4 = \sqrt{9} - 4 = -1 \neq -7$

Check 2: $\sqrt{3(2+10)} - 4 = \sqrt{36} - 4 = 2 = 2$

Discard $x = -7$ as extraneous.

The solution set is $\{2\}$.

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28. $\sqrt{1-x}-3=x+2$

$\sqrt{1-x}=x+5$

$\left(\sqrt{1-x}\right)^2=(x+5)^2$

$1-x=x^2+10x+25$

$0=x^2+11x+24$

$0=(x+3)(x+8)$

$x=-3$ or $x=-8$

Check -3: $\sqrt{1-(-3)}-3=-3+2\rightarrow -1=-1$

Check -8: $\sqrt{1-(-8)}-3=-8+2\rightarrow 0=-6$

Discard $x=-8$ as extraneous.

The solution set is {-3}.

29. $\sqrt{3x-5}-\sqrt{x+7}=2$

$\sqrt{3x-5}=2+\sqrt{x+7}$

$\left(\sqrt{3x-5}\right)^2=\left(2+\sqrt{x+7}\right)^2$

$3x-5=4+4\sqrt{x+7}+x+7$

$2x-16=4\sqrt{x+7}$

$(2x-16)^2=\left(4\sqrt{x+7}\right)^2$

$4x^2-64x+256=16(x+7)$

$4x^2-64x+256=16x+112$

$4x^2-80x+144=0$

$x^2-20x+36=0$

$(x-2)(x-18)=0$

$x=2$ or $x=18$

Check 2: $\sqrt{3(2)-5}-\sqrt{2+7}$

$=\sqrt{1}-\sqrt{9}=1-3=-2\neq 2$

Check 18: $\sqrt{3(18)-5}-\sqrt{18+7}$

$=\sqrt{49}-\sqrt{25}=7-5=2=2$

Discard $x=2$ as extraneous.

The solution set is {18}.

30. $\sqrt{3x+7}+\sqrt{x+2}=1$

$\sqrt{3x+7}=1-\sqrt{x+2}$

$\left(\sqrt{3x+7}\right)^2=\left(1-\sqrt{x+2}\right)^2$

$3x+7=1-2\sqrt{x+2}+x+2$

$2x+4=-2\sqrt{x+2}$

$-x-2=\sqrt{x+2}$

$(-x-2)^2=\left(\sqrt{x+2}\right)^2$

$x^2+4x+4=x+2$

$x^2+3x+2=0$

$(x+1)(x+2)=0$

$x=-1$ or $x=-2$

Check -1: $\sqrt{3(-1)+7}+\sqrt{-1+2}$

$=\sqrt{4}+\sqrt{1}=2+1=3\neq 1$

Check -2: $\sqrt{3(-2)+7}+\sqrt{-2+2}$

$=\sqrt{1}+\sqrt{0}=1+0=1=1$

Discard $x=-1$ as extraneous.

The solution set is $\{-2\}$.

31. $\sqrt{3x+1}-\sqrt{x-1}=2$

$\sqrt{3x+1}=2+\sqrt{x-1}$

$\left(\sqrt{3x+1}\right)^2=\left(2+\sqrt{x-1}\right)^2$

$3x+1=4+4\sqrt{x-1}+x-1$

$2x-2=4\sqrt{x-1}$

$(2x-2)^2=\left(4\sqrt{x-1}\right)^2$

$4x^2-8x+4=16(x-1)$

$x^2-2x+1=4x-4$

$x^2-6x+5=0$

$(x-1)(x-5)=0$

$x=1$ or $x=5$

Check 1: $\sqrt{3(1)+1}-\sqrt{1-1}$

$=\sqrt{4}-\sqrt{0}=2-0=2=2$

Check 5: $\sqrt{3(5)+1}-\sqrt{5-1}$

$=\sqrt{16}-\sqrt{4}=4-2=2=2$

The solution set is $\{1,5\}$.

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32. $\sqrt{2x+3}-\sqrt{x+1}=1$

$$\sqrt{2x+3}=1+\sqrt{x+1}$$
$$\left(\sqrt{2x+3}\right)^2=\left(1+\sqrt{x+1}\right)^2$$
$$2x+3=1+2\sqrt{x+1}+x+1$$
$$x+1=2\sqrt{x+1}$$
$$(x+1)^2=\left(2\sqrt{x+1}\right)^2$$
$$x^2+2x+1=4(x+1)$$
$$x^2+2x+1=4x+4$$
$$x^2-2x-3=0$$
$$(x+1)(x-3)=0$$
$$x=-1 \text{ or } x=3$$

Check -1: $\sqrt{2(-1)+3}-\sqrt{-1+1}$
$=\sqrt{1}-\sqrt{0}=1-0=1=1$

Check 3: $\sqrt{2(3)+3}-\sqrt{3+1}$
$=\sqrt{9}-\sqrt{4}=3-2=1=1$

The solution set is $\{-1,3\}$.

33. $\sqrt{3-2\sqrt{x}}=\sqrt{x}$

$$\left(\sqrt{3-2\sqrt{x}}\right)^2=\left(\sqrt{x}\right)^2$$
$$3-2\sqrt{x}=x$$
$$-2\sqrt{x}=x-3$$
$$\left(-2\sqrt{x}\right)^2=(x-3)^2$$
$$4x=x^2-6x+9$$
$$0=x^2-10x+9$$
$$0=(x-1)(x-9)$$
$$x=1 \text{ or } x=9$$

Check 1:
$\sqrt{3-2\sqrt{1}}=\sqrt{1}$
$\sqrt{3-2}=1$
$\sqrt{1}=1$
$1=1$

Check 9:
$\sqrt{3-2\sqrt{9}}=\sqrt{9}$
$\sqrt{3-2\cdot 3}=3$
$\sqrt{-3}\neq 3$

Discard $x=9$ as extraneous.
The solution set is $\{1\}$.

34. $\sqrt{10+3\sqrt{x}}=\sqrt{x}$

$$\left(\sqrt{10+3\sqrt{x}}\right)^2=\left(\sqrt{x}\right)^2$$
$$10+3\sqrt{x}=x$$
$$3\sqrt{x}=x-10$$
$$\left(3\sqrt{x}\right)^2=(x-10)^2$$
$$9x=x^2-20x+100$$
$$0=x^2-29x+100$$
$$0=(x-4)(x-25)$$
$$x=4 \text{ or } x=25$$

Check 4:
$\sqrt{10+3\sqrt{4}}=\sqrt{4}$
$\sqrt{10+3\cdot 2}=2$
$\sqrt{16}=2$
$4\neq 2$

Check 25:
$\sqrt{10+3\sqrt{25}}=\sqrt{25}$
$\sqrt{10+3\cdot 5}=5$
$\sqrt{25}=5$
$5=5$

Discard $x=4$ as extraneous.
The solution set is $\{25\}$.

35. $(3x+1)^{1/2}=4$

$$\left((3x+1)^{1/2}\right)^2=(4)^2$$
$$3x+1=16$$
$$3x=15$$
$$x=5$$

Check: $\left(3(5)+1\right)^{1/2}=16^{1/2}=4$

The solution set is $\{5\}$.

36. $(3x-5)^{1/2}=2$

$$\left((3x-5)^{1/2}\right)^2=(2)^2$$
$$3x-5=4$$
$$3x=9$$
$$x=3$$

Check: $\left(3(3)-5\right)^{1/2}=4^{1/2}=2$

The solution set is $\{3\}$.

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37. $(5x-2)^{1/3}=2$

$\left((5x-2)^{1/3}\right)^3=(2)^3$

$5x-2=8$

$5x=10$

$x=2$

Check: $(5(2)-2)^{1/3}=8^{1/3}=2$

The solution set is $\{2\}$.

38. $(2x+1)^{1/3}=-1$

$\left((2x+1)^{1/3}\right)^3=(-1)^3$

$2x+1=-1$

$2x=-2$

$x=-1$

Check: $(2(-1)+1)^{1/3}=(-1)^{1/3}=-1$

The solution set is $\{-1\}$.

39. $\left(x^2+9\right)^{1/2}=5$

$\left(\left(x^2+9\right)^{1/2}\right)^2=(5)^2$

$x^2+9=25$

$x^2=16$

$x=\pm\sqrt{16}=\pm4$

Check -4: $\left((-4)^2+9\right)^{1/2}=25^{1/2}=5$

Check 4: $\left((4)^2+9\right)^{1/2}=25^{1/2}=5$

The solution set is $\{-4,4\}$.

40. $\left(x^2-16\right)^{1/2}=9$

$\left(\left(x^2-16\right)^{1/2}\right)^2=(9)^2$

$x^2-16=81$

$x^2=97$

$x=\pm\sqrt{97}$

Check $-\sqrt{97}$: $\left(\left(-\sqrt{97}\right)^2-16\right)^{1/2}=81^{1/2}=9$

Check $\sqrt{97}$: $\left(\left(\sqrt{97}\right)^2-16\right)^{1/2}=81^{1/2}=9$

The solution set is $\left\{-\sqrt{97},\sqrt{97}\right\}$.

41. $x^{3/2}-3x^{1/2}=0$

$x^{1/2}(x-3)=0$

$x^{1/2}=0$ or $x-3=0$

$x=0$ or $x=3$

Check 0: $0^{3/2}-3\cdot0^{1/2}=0-0=0$

Check 3: $3^{3/2}-3\cdot3^{1/2}=3\sqrt{3}-3\sqrt{3}=0$

The solution set is $\{0,3\}$.

42. $x^{3/4}-9x^{1/4}=0$

$x^{1/4}\left(x^{1/2}-9\right)=0$

$x^{1/4}=0$ or $x^{1/2}=9$

$x=0$ $x=81$

Check 0: $0^{3/4}-9\cdot0^{1/4}=0-0=0$

Check 81: $81^{3/4}-9\cdot81^{1/4}=27-27=0$

The solution set is $\{0,81\}$.

43. $x^4-5x^2+4=0$

$\left(x^2-4\right)\left(x^2-1\right)=0$

$x^2-4=0$ or $x^2-1=0$

$x=\pm2$ or $x=\pm1$

The solution set is $\{-2,-1,1,2\}$.

44. $x^4-10x^2+25=0$

$\left(x^2-5\right)\left(x^2-5\right)=0$

$x^2-5=0$

$x=\pm\sqrt{5}$

The solution set is $\left\{-\sqrt{5},\sqrt{5}\right\}$.

45. $6x^4-5x^2-1=0$

$\left(6x^2+1\right)\left(x^2-1\right)=0$

$6x^2+1=0$ or $x^2-1=0$

$6x^2=-1$ or $x^2=1$

Not real or $x=\pm1$

The solution set is $\{-1,1\}$.

46. $2x^4-5x^2-12=0$

$\left(2x^2+3\right)\left(x^2-4\right)=0$

$2x^2+3=0$ or $x^2-4=0$

$2x^2=-3$ or $x^2=4$

Not real or $x=\pm2$

The solution set is $\{-2,2\}$.

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47. $x^6 + 7x^3 - 8 = 0$

$(x^3 + 8)(x^3 - 1) = 0$

$x^3 + 8 = 0$ or $x^3 - 1 = 0$

$x^3 = -8$ or $x^3 = 1$

$x = -2$ or $x = 1$

The solution set is $\{-2, 1\}$.

48. $x^6 - 7x^3 - 8 = 0$

$(x^3 - 8)(x^3 + 1) = 0$

$x^3 - 8 = 0$ or $x^3 + 1 = 0$

$x^3 = 8$ or $x^3 = -1$

$x = 2$ or $x = -1$

The solution set is $\{-1, 2\}$.

49. $(x+2)^2 + 7(x+2) + 12 = 0$

Let $u = x + 2$, so that $u^2 = (x+2)^2$.

$u^2 + 7u + 12 = 0$

$(u+3)(u+4) = 0$

$u + 3 = 0$ or $u + 4 = 0$

$u = -3$ or $u = -4$

$x + 2 = -3$ or $x + 2 = -4$

$x = -5$ or $x = -6$

The solution set is $\{-6, -5\}$.

50. $(2x+5)^2 - (2x+5) - 6 = 0$

Let $u = 2x + 5$ so that $u^2 = (2x+5)^2$.

$u^2 - u - 6 = 0$

$(u-3)(u+2) = 0$

$u - 3 = 0$ or $u + 2 = 0$

$u = 3$ or $u = -2$

$2x + 5 = 3$ or $2x + 5 = -2$

$x = -1$ or $x = -\frac{7}{2}$

The solution set is $\left\{-\frac{7}{2}, -1\right\}$.

51. $(4x-9)^2 - 10(4x-9) + 25 = 0$

Let $u = 4x - 9$ so that $u^2 = (4x-9)^2$.

$u^2 - 10u + 25 = 0$

$(u-5)^2 = 0$

$u - 5 = 0$

$u = 5$

$4x - 9 = 5$

$4x = 14$

$x = \frac{7}{2}$

The solution set is $\left\{\frac{7}{2}\right\}$.

52. $(2-x)^2 + (2-x) - 20 = 0$

Let $u = 2 - x$ so that $u^2 = (2-x)^2$.

$u^2 + u - 20 = 0$

$(u+5)(u-4) = 0$

$u + 5 = 0$ or $u - 4 = 0$

$u = -5$ or $u = 4$

$2 - x = -5$ or $2 - x = 4$

$x = 7$ or $x = -2$

The solution set is $\{-2, 7\}$.

53. $2(s+1)^2 - 5(s+1) = 3$

Let $u = s + 1$ so that $u^2 = (s+1)^2$.

$2u^2 - 5u = 3$

$2u^2 - 5u - 3 = 0$

$(2u+1)(u-3) = 0$

$2u + 1 = 0$ or $u - 3 = 0$

$u = -\frac{1}{2}$ or $u = 3$

$s + 1 = -\frac{1}{2}$ or $s + 1 = 3$

$s = -\frac{3}{2}$ or $s = 2$

The solution set is $\left\{-\frac{3}{2}, 2\right\}$.

54. $3(1-y)^2 + 5(1-y) + 2 = 0$

Let $u = 1 - y$ so that $u^2 = (1-y)^2$.

$3u^2 + 5u + 2 = 0$

$(3u+2)(u+1) = 0$

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$$3u+2=0 \quad \text{or} \quad u+1=0$$
$$u=-\frac{2}{3} \quad \text{or} \quad u=-1$$
$$1-y=-\frac{2}{3} \quad \text{or} \quad 1-y=-1$$
$$y=\frac{5}{3} \quad \text{or} \quad y=2$$

The solution set is $\left\{\frac{5}{3},2\right\}$.

55. $x-4x\sqrt{x}=0$

$$x\left(1-4\sqrt{x}\right)=0$$
$$x=0 \quad \text{or} \quad 1-4\sqrt{x}=0$$
$$1=4\sqrt{x}$$
$$\tfrac{1}{4}=\sqrt{x}$$
$$\left(\tfrac{1}{4}\right)^2=\left(\sqrt{x}\right)^2$$
$$\tfrac{1}{16}=x$$

Check:

$x=0$: $0-4(0)\sqrt{0}=0$

$0=0$

$x=\frac{1}{16}$: $\left(\frac{1}{16}\right)-4\left(\frac{1}{16}\right)\sqrt{\frac{1}{16}}=0$

$\frac{1}{16}-4\left(\frac{1}{16}\right)\left(\frac{1}{4}\right)=0$

$\frac{1}{16}-\frac{1}{16}=0$

$0=0$

The solution set is $\left\{0,\frac{1}{16}\right\}$.

56. $x+8\sqrt{x}=0$

$$8\sqrt{x}=-x$$
$$\left(8\sqrt{x}\right)^2=(-x)^2$$
$$64x=x^2$$
$$0=x^2-64x$$
$$0=x(x-64)$$
$$x=0 \text{ or } x=64$$

Check: $x=0$: $0+8\sqrt{0}=0$

$0=0$

$x=64$: $64+8\sqrt{64}=0$

$64+64\neq 0$

The solution set is $\{0\}$.

57. $x+\sqrt{x}=20$

Let $u=\sqrt{x}$ so that $u^2=x$.

$$u^2+u=20$$
$$u^2+u-20=0$$
$$(u+5)(u-4)=0$$
$$u+5=0 \quad \text{or} \quad u-4=0$$
$$u=-5 \quad \text{or} \quad u=4$$
$$\sqrt{x}=-5 \quad \text{or} \quad \sqrt{x}=4$$
$$\text{not possible} \quad \text{or} \quad x=16$$

Check: $16+\sqrt{16}=20$

$16+4=20$

The solution set is $\{16\}$.

58. $x+\sqrt{x}=6$

Let $u=\sqrt{x}$ so that $u^2=x$.

$$u^2+u=6$$
$$u^2+u-6=0$$
$$(u+3)(u-2)=0$$
$$u+3=0 \quad \text{or} \quad u-2=0$$
$$u=-3 \quad \text{or} \quad u=2$$
$$\sqrt{x}=-3 \quad \text{or} \quad \sqrt{x}=2$$
$$\text{not possible} \quad \text{or} \quad x=4$$

Check: $4+\sqrt{4}=6$

$4+2=6$

The solution set is $\{4\}$.

59. $t^{1/2}-2t^{1/4}+1=0$

Let $u=t^{1/4}$ so that $u^2=t^{1/2}$.

$$u^2-2u+1=0$$
$$(u-1)^2=0$$
$$u-1=0$$
$$u=1$$
$$t^{1/4}=1$$
$$t=1$$

Check: $1^{1/2}-2(1)^{1/4}+1=0$

$1-2+1=0$

$0=0$

The solution set is $\{1\}$.

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60. $z^{1/2}-4t^{1/4}+4=0$

Let $u=z^{1/4}$ so that $u^2=z^{1/2}$.

$u^2-4u+4=0$

$(u-2)^2=0$

$u-2=0$

$u=2$

$z^{1/4}=2$

$z=16$

Check: $16^{1/2}-4(16)^{1/4}+4=0$

$4-8+4=0$

$0=0$

The solution set is $\{16\}$.

61. $x^{1/2}-3x^{1/4}+2=0$

Let $u=x^{1/4}$ so that $u^2=x^{1/2}$.

$u^2-3u+2=0$

$(u-2)(u-1)=0$

$u=2$ or $u=1$

$x^{1/4}=2$ or $x^{1/4}=1$

$x=16$ or $x=1$

Check:

$x=16$: $16^{1/2}-3(16)^{1/4}+2=0$

$4-6+2=0$

$0=0$

$x=1$: $1^{1/2}-3(1)^{1/4}+2=0$

$1-3+2=0$

$0=0$

The solution set is $\{1,16\}$.

62. $4x^{1/2}-9x^{1/4}+4=0$

Let $u=x^{1/4}$ so that $u^2=x^{1/2}$.

$4u^2-9u+4=0$

$$u=\frac{-(-9)\pm\sqrt{(-9)^2-4(4)(4)}}{2(4)}=\frac{9\pm\sqrt{17}}{8}$$

$$x^{1/4}=\frac{9\pm\sqrt{17}}{8}$$

$$x=\left(\frac{9\pm\sqrt{17}}{8}\right)^4$$

Check $x=\left(\frac{9+\sqrt{17}}{8}\right)^4$:

$$4\left(\left(\frac{9+\sqrt{17}}{8}\right)^4\right)^{1/2}-9\left(\left(\frac{9+\sqrt{17}}{8}\right)^4\right)^{1/4}+4=0$$

$$4\left(\frac{9+\sqrt{17}}{8}\right)^2-9\left(\frac{9+\sqrt{17}}{8}\right)+4=0$$

$$4\frac{\left(9+\sqrt{17}\right)^2}{64}-9\left(\frac{9+\sqrt{17}}{8}\right)+4=0$$

$$64\left(4\frac{\left(9+\sqrt{17}\right)^2}{64}-9\left(\frac{9+\sqrt{17}}{8}\right)+4\right)=(0)(64)$$

$$4\left(9+\sqrt{17}\right)^2-72\left(9+\sqrt{17}\right)+256=0$$

$$4\left(81+18\sqrt{17}+17\right)-72\left(9+\sqrt{17}\right)+256=0$$

$$324+72\sqrt{17}+68-648-72\sqrt{17}+256=0$$

$$0=0$$

Check $x=\left(\frac{9-\sqrt{17}}{8}\right)^4$:

$$4\left(\left(\frac{9-\sqrt{17}}{8}\right)^4\right)^{1/2}-9\left(\left(\frac{9-\sqrt{17}}{8}\right)^4\right)^{1/4}+4=0$$

$$4\left(\frac{9-\sqrt{17}}{8}\right)^2-9\left(\frac{9-\sqrt{17}}{8}\right)+4=0$$

$$4\left(81-18\sqrt{17}+17\right)-72\left(9-\sqrt{17}\right)+256=0$$

$$324-72\sqrt{17}+68-648+72\sqrt{17}+256=0$$

$$0=0$$

The solution set is $\left\{\left(\frac{9-\sqrt{17}}{8}\right)^4,\left(\frac{9+\sqrt{17}}{8}\right)^4\right\}$.

63. $\sqrt[4]{5x^2-6}=x$

$\left(\sqrt[4]{5x^2-6}\right)^4=x^4$

$5x^2-6=x^4$

$0=x^4-5x^2+6$

Let $u=x^2$ so that $u^2=x^4$.

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$0 = u^2 - 5u + 6$

$0 = (u-3)(u-2)$

$u = 3 \quad \text{or} \quad u = 2$

$x^2 = 3 \quad \text{or} \quad x^2 = 2$

$x = \pm\sqrt{3} \quad \text{or} \quad x = \pm\sqrt{2}$

Check:

$x = -\sqrt{3}$: $\sqrt[4]{5\left(-\sqrt{3}\right)^2 - 6} = -\sqrt{3}$

$\sqrt[4]{15-6} = -\sqrt{3}$

$\sqrt[4]{9} \neq -\sqrt{3}$

$x = \sqrt{3}$: $\sqrt[4]{5\left(\sqrt{3}\right)^2 - 6} = \sqrt{3}$

$\sqrt[4]{15-6} = \sqrt{3}$

$\sqrt[4]{9} = \sqrt{3}$

$\sqrt{3} = \sqrt{3}$

$x = -\sqrt{2}$: $\sqrt[4]{5\left(-\sqrt{2}\right)^2 - 6} = -\sqrt{2}$

$\sqrt[4]{10-6} = -\sqrt{2}$

$\sqrt[4]{4} \neq -\sqrt{2}$

$x = \sqrt{2}$: $\sqrt[4]{5\left(\sqrt{2}\right)^2 - 6} = \sqrt{2}$

$\sqrt[4]{10-6} = \sqrt{2}$

$\sqrt[4]{4} = \sqrt{2}$

$\sqrt{2} = \sqrt{2}$

The solution set is $\left\{\sqrt{2}, \sqrt{3}\right\}$.

64. $\sqrt[4]{4-5x^2} = x$

$\left(\sqrt[4]{4-5x^2}\right)^4 = x^4$

$4 - 5x^2 = x^4$

$0 = x^4 + 5x^2 - 4$

Let $u = x^2$ so that $u^2 = x^4$.

$0 = u^2 + 5u - 4$

$u = \dfrac{-5 \pm \sqrt{5^2 - 4(1)(-4)}}{2} = \dfrac{-5 \pm \sqrt{41}}{2}$

$x^2 = \dfrac{-5 \pm \sqrt{41}}{2}$

$x = \pm\sqrt{\dfrac{-5 \pm \sqrt{41}}{2}}$

Since $-5 - \sqrt{41} < 0$, $x = \pm\sqrt{\dfrac{-5-\sqrt{41}}{2}}$ is not real.

Since x is a fourth root, $x = -\sqrt{\dfrac{-5+\sqrt{41}}{2}}$ is also not real. Therefore, we have only one possible solution to check: $x = \sqrt{\dfrac{-5+\sqrt{41}}{2}}$:

Check $x = \sqrt{\dfrac{-5+\sqrt{41}}{2}}$:

$$\sqrt[4]{4 - 5\left(\pm\sqrt{\frac{-5+\sqrt{41}}{2}}\right)^2} = \sqrt{\frac{-5+\sqrt{41}}{2}}$$

$$\sqrt[4]{4 - 5\left(\frac{-5+\sqrt{41}}{2}\right)} = \sqrt{\frac{-5+\sqrt{41}}{2}}$$

$$\sqrt[4]{\frac{8 - 5\left(-5+\sqrt{41}\right)}{2}} = \sqrt{\frac{-5+\sqrt{41}}{2}}$$

$$\sqrt[4]{\frac{33 - 5\sqrt{41}}{2}} = \sqrt{\frac{-5+\sqrt{41}}{2}}$$

$$\sqrt[4]{\frac{66 - 10\sqrt{41}}{4}} = \sqrt{\frac{-5+\sqrt{41}}{2}}$$

$$\sqrt[4]{\frac{25 - 10\sqrt{41} + 41}{4}} = \sqrt{\frac{-5+\sqrt{41}}{2}}$$

$$\sqrt[4]{\frac{\left(-5+\sqrt{41}\right)^2}{4}} = \sqrt{\frac{-5+\sqrt{41}}{2}}$$

$$\sqrt{\frac{-5+\sqrt{41}}{2}} = \sqrt{\frac{-5+\sqrt{41}}{2}}$$

The solution set is $\left\{\sqrt{\dfrac{-5+\sqrt{41}}{2}}\right\}$.

65. $x^2 + 3x + \sqrt{x^2+3x} = 6$

Let $u = \sqrt{x^2+3x}$ so that $u^2 = x^2 + 3x$.

$u^2 + u = 6$

$u^2 + u - 6 = 0$

$(u+3)(u-2) = 0$

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$$u=-3 \quad \text{or} \quad u=2$$
$$\sqrt{x^2+3x}=-3 \quad \text{or} \quad \sqrt{x^2+3x}=2$$
$$\text{Not possible} \quad \text{or} \quad x^2+3x=4$$
$$x^2+3x-4=0$$
$$(x+4)(x-1)=0$$
$$x=-4 \text{ or } x=1$$

Check $x=-4$:

$$(-4)^2+3(-4)+\sqrt{(-4)^2+3(-4)}=6$$
$$16-12+\sqrt{16-12}=6$$
$$16-12+\sqrt{4}=6$$
$$6=6$$

Check $x=1$:

$$(1)^2+3(1)+\sqrt{(1)^2+3(1)}=6$$
$$1+3+\sqrt{1+3}=6$$
$$4+\sqrt{4}=6$$
$$6=6$$

The solution set is $\{-4,\ 1\}$.

66. $x^2-3x-\sqrt{x^2-3x}=2$

Let $u=\sqrt{x^2-3x}$ so that $u^2=x^2-3x$.

$$u^2-u=2$$
$$u^2-u-2=0$$
$$(u+1)(u-2)=0$$
$$u=-1 \quad \text{or} \quad u=2$$
$$\sqrt{x^2-3x}=-1 \quad \text{or} \quad \sqrt{x^2-3x}=2$$
$$\text{Not possible} \quad \text{or} \quad x^2-3x=4$$
$$x^2-3x-4=0$$
$$(x-4)(x+1)=0$$
$$x=4 \text{ or } x=-1$$

Check $x=4$:

$$(4)^2-3(4)-\sqrt{(4)^2-3(4)}=16-12-\sqrt{4}$$
$$=4-2=2$$

Check $x=-1$:

$$(-1)^2-3(-1)-\sqrt{(-1)^2-3(-1)}=1+3-\sqrt{4}$$
$$=4-2=2$$

The solution set is $\{-1,\ 4\}$.

67. $\dfrac{1}{(x+1)^2}=\dfrac{1}{x+1}+2$

Let $u=\dfrac{1}{x+1}$ so that $u^2=\left(\dfrac{1}{x+1}\right)^2$.

$$u^2=u+2$$
$$u^2-u-2=0$$
$$(u+1)(u-2)=0$$
$$u=-1 \quad \text{or} \quad u=2$$
$$\frac{1}{x+1}=-1 \quad \text{or} \quad \frac{1}{x+1}=2$$
$$1=-x-1 \quad \text{or} \quad 1=2x+2$$
$$x=-2 \quad \text{or} \quad -2x=1$$
$$x=-\frac{1}{2}$$

Check:

$x=-2$: $\dfrac{1}{(-2+1)^2}=\dfrac{1}{-2+1}+2$

$$1=-1+2$$
$$1=1$$

$x=-\dfrac{1}{2}$: $\dfrac{1}{\left(-\frac{1}{2}+1\right)^2}=\dfrac{1}{\left(-\frac{1}{2}+1\right)}+2$

$$4=2+2$$
$$4=4$$

The solution set is $\left\{-2,-\frac{1}{2}\right\}$.

68. $\dfrac{1}{(x-1)^2}+\dfrac{1}{x-1}=12$

Let $u=\dfrac{1}{x-1}$ so that $u^2=\left(\dfrac{1}{x-1}\right)^2$.

$$u^2+u=12$$
$$u^2+u-12=0$$
$$(u+4)(u-3)=0$$
$$u=-4 \quad \text{or} \quad u=3$$
$$\frac{1}{x-1}=-4 \quad \text{or} \quad \frac{1}{x-1}=3$$
$$1=-4x+4 \quad \text{or} \quad 1=3x-3$$
$$4x=3 \quad \text{or} \quad 4=3x$$
$$x=\frac{3}{4} \quad \text{or} \quad x=\frac{4}{3}$$

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Check:

$$x=\frac{3}{4}:\ \frac{1}{\left(\frac{3}{4}-1\right)^2}+\frac{1}{\left(\frac{3}{4}-1\right)}=12$$

$$\frac{1}{\left(\frac{1}{16}\right)}+\frac{1}{\left(-\frac{1}{4}\right)}=12$$

$$16-4=12$$

$$12=12$$

$$x=\frac{4}{3}:\ \frac{1}{\left(\frac{4}{3}-1\right)^2}+\frac{1}{\left(\frac{4}{3}-1\right)}=12$$

$$\frac{1}{\left(\frac{1}{9}\right)}+\frac{1}{\left(\frac{1}{3}\right)}=12$$

$$9+3=12$$

$$12=12$$

The solution set is $\left\{\frac{3}{4},\frac{4}{3}\right\}$.

69. $3x^{-2}-7x^{-1}-6=0$

Let $u=x^{-1}$ so that $u^2=x^{-2}$.

$$3u^2-7u-6=0$$

$$(3u+2)(u-3)=0$$

$$u=-\frac{2}{3} \quad \text{or} \quad u=3$$

$$x^{-1}=-\frac{2}{3} \quad \text{or} \quad x^{-1}=3$$

$$\left(x^{-1}\right)^{-1}=\left(-\frac{2}{3}\right)^{-1} \quad \text{or} \quad \left(x^{-1}\right)^{-1}=(3)^{-1}$$

$$x=-\frac{3}{2} \quad \text{or} \quad x=\frac{1}{3}$$

Check:

$$x=-\frac{3}{2}:\ 3\left(-\frac{3}{2}\right)^{-2}-7\left(-\frac{3}{2}\right)^{-1}-6=0$$

$$3\left(\frac{4}{9}\right)-7\left(-\frac{2}{3}\right)-6=0$$

$$\frac{4}{3}+\frac{14}{3}-6=0$$

$$0=0$$

$$x=\frac{1}{3}:\ 3\left(\frac{1}{3}\right)^{-2}-7\left(\frac{1}{3}\right)^{-1}-6=0$$

$$3(9)-7(3)-6=0$$

$$27-21-6=0$$

$$0=0$$

The solution set is $\left\{-\frac{3}{2},\frac{1}{3}\right\}$.

70. $2x^{-2}-3x^{-1}-4=0$

Let $u=x^{-1}$ so that $u^2=x^{-2}$.

$$2u^2-3u-4=0$$

$$u=\frac{-(-3)\pm\sqrt{(-3)^2-4(2)(-4)}}{2(2)}=\frac{3\pm\sqrt{41}}{4}$$

$$u=\frac{3+\sqrt{41}}{4} \quad \text{or} \quad u=\frac{3-\sqrt{41}}{4}$$

$$x^{-1}=\frac{3+\sqrt{41}}{4} \quad \text{or} \quad x^{-1}=\frac{3-\sqrt{41}}{4}$$

$$\left(x^{-1}\right)^{-1}=\left(\frac{3+\sqrt{41}}{4}\right)^{-1} \quad \text{or} \quad \left(x^{-1}\right)^{-1}=\left(\frac{3-\sqrt{41}}{4}\right)^{-1}$$

$$x=\frac{4}{3+\sqrt{41}}\left(\frac{3-\sqrt{41}}{3-\sqrt{41}}\right) \quad \text{or} \quad x=\frac{4}{3-\sqrt{41}}\left(\frac{3+\sqrt{41}}{3+\sqrt{41}}\right)$$

$$=\frac{12-4\sqrt{41}}{-32} \qquad =\frac{12+4\sqrt{41}}{-32}$$

$$=\frac{-3+\sqrt{41}}{8} \qquad =\frac{-3-\sqrt{41}}{8}$$

Check $x=\frac{-3+\sqrt{41}}{8}$:

$$2\left(\frac{-3+\sqrt{41}}{8}\right)^{-2}-3\left(\frac{-3+\sqrt{41}}{8}\right)^{-1}-4=0$$

$$2\left(\frac{64}{\left(-3+\sqrt{41}\right)^2}\right)-3\left(\frac{8}{-3+\sqrt{41}}\right)-4=0$$

$$2(64)-3(8)\left(-3+\sqrt{41}\right)-4\left(-3+\sqrt{41}\right)^2=0$$

$$128+72-24\sqrt{41}-4\left(9-6\sqrt{41}+41\right)=0$$

$$128+72-24\sqrt{41}-36+24\sqrt{41}-164=0$$

$$0=0$$

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Check $x=\dfrac{-3-\sqrt{41}}{8}$:

$$2\left(\frac{-3-\sqrt{41}}{8}\right)^{-2}-3\left(\frac{-3-\sqrt{41}}{8}\right)^{-1}-4=0$$

$$2\left(\frac{64}{\left(-3-\sqrt{41}\right)^2}\right)-3\left(\frac{8}{-3-\sqrt{41}}\right)-4=0$$

$$2(64)-3(8)\left(-3-\sqrt{41}\right)-4\left(-3-\sqrt{41}\right)^2=0$$

$$128+72+24\sqrt{41}-4\left(9+6\sqrt{41}+41\right)=0$$

$$128+72+24\sqrt{41}-36-24\sqrt{41}-164=0$$

$$0=0$$

The solution set is $\left\{\dfrac{-3-\sqrt{41}}{8},\dfrac{-3+\sqrt{41}}{8}\right\}$.

71. $2x^{2/3}-5x^{1/3}-3=0$

Let $u=x^{1/3}$ so that $u^2=x^{2/3}$.

$$2u^2-5u-3=0$$

$$(2u+1)(u-3)=0$$

$$u=-\frac{1}{2} \quad \text{or} \quad u=3$$

$$x^{1/3}=-\frac{1}{2} \quad \text{or} \quad x^{1/3}=3$$

$$\left(x^{1/3}\right)^3=\left(-\frac{1}{2}\right)^3 \quad \text{or} \quad \left(x^{1/3}\right)^3=(3)^3$$

$$x=-\frac{1}{8} \quad \text{or} \quad x=27$$

Check $x=-\dfrac{1}{8}$: $2\left(-\dfrac{1}{8}\right)^{2/3}-5\left(-\dfrac{1}{8}\right)^{1/3}-3=0$

$$2\left(\frac{1}{4}\right)-5\left(-\frac{1}{2}\right)-3=0$$

$$\frac{1}{2}+\frac{5}{2}-3=0$$

$$3-3=0$$

$$0=0$$

Check $x=27$: $2(27)^{2/3}-5(27)^{1/3}-3=0$

$$2(9)-5(3)-3=0$$

$$18-15-3=0$$

$$3-3=0$$

$$0=0$$

The solution set is $\left\{-\dfrac{1}{8},27\right\}$.

72. $3x^{4/3}+5x^{2/3}-2=0$

Let $u=x^{2/3}$ so that $u^2=x^{4/3}$.

$$3u^2+5u-2=0$$

$$(3u-1)(u+2)=0$$

$$u=\frac{1}{3} \quad \text{or} \quad u=-2$$

$$x^{2/3}=\frac{1}{3} \quad \text{or} \quad x^{2/3}=-2$$

$$\left(x^{2/3}\right)^3=\left(\frac{1}{3}\right)^3 \quad \text{or} \quad \left(x^{2/3}\right)^3=(-2)^3$$

$$x^2=\frac{1}{27} \quad \text{or} \quad x^2=-8$$

$$x=\pm\sqrt{\frac{1}{27}} \quad \text{not real}$$

Check: $3\left(\pm\sqrt{\dfrac{1}{27}}\right)^{4/3}+5\left(\pm\sqrt{\dfrac{1}{27}}\right)^{2/3}-2=0$

$$3\left(\frac{1}{27}\right)^{2/3}+5\left(\pm\frac{1}{27}\right)^{1/3}-2=0$$

$$3\left(\frac{1}{3}\right)^2+5\left(\frac{1}{3}\right)-2=0$$

$$3\left(\frac{1}{9}\right)+\frac{5}{3}-2=0$$

$$\frac{1}{3}+\frac{5}{3}-2=0$$

$$2-2=0$$

$$0=0$$

Note: $\pm\sqrt{\dfrac{1}{27}}=\pm\sqrt{\dfrac{3}{81}}=\pm\dfrac{\sqrt{3}}{9}$

The solution set is $\left\{-\dfrac{\sqrt{3}}{9},\dfrac{\sqrt{3}}{9}\right\}$.

73. $\left(\dfrac{v}{v+2}\right)^2+\dfrac{3v}{v+2}=10$

$$\left(\frac{v}{v+2}\right)^2+3\left(\frac{v}{v+2}\right)=10$$

Let $u=\dfrac{v}{v+2}$ so that $u^2=\left(\dfrac{v}{v+2}\right)^2$.

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$$u^2+3u=10$$
$$u^2+3u-10=0$$
$$(u+5)(u-2)=0$$
$$u=-5 \quad \text{or} \quad u=2$$
$$\frac{v}{v+2}=-5 \quad \text{or} \quad \frac{v}{v+2}=2$$
$$v=-5v-10 \quad \text{or} \quad v=2v+4$$
$$v=-\frac{5}{3} \quad \text{or} \quad v=-4$$

Check $v=-\frac{5}{3}$: $\left(\frac{-\frac{5}{3}}{-\frac{5}{3}+2}\right)^2+\frac{3\left(-\frac{5}{3}\right)}{\left(-\frac{5}{3}\right)+2}=10$

$$\frac{\left(\frac{25}{9}\right)}{\left(\frac{1}{9}\right)}+\frac{\left(-\frac{15}{3}\right)}{\left(\frac{1}{3}\right)}=10$$
$$25-15=10$$
$$10=10$$

Check $v=-4$: $\left(\frac{-4}{-4+2}\right)^2+\frac{3(-4)}{(-4)+2}=10$

$$\frac{16}{4}+\frac{-12}{-2}=10$$
$$4+6=10$$
$$10=10$$

The solution set is $\left\{-4,-\frac{5}{3}\right\}$.

74. $\left(\frac{y}{y-1}\right)^2=6\left(\frac{y}{y-1}\right)+16$

Let $u=\frac{y}{y-1}$ so that $u^2=\left(\frac{y}{y-1}\right)^2$.

$$u^2=6u+16$$
$$u^2-6u-16=0$$
$$(u+2)(u-8)=0$$
$$u=-2 \quad \text{or} \quad u=8$$
$$\frac{y}{y-1}=-2 \quad \text{or} \quad \frac{y}{y-1}=8$$
$$y=-2y+2 \quad \text{or} \quad y=8y-8$$
$$3y=2 \quad \text{or} \quad -7y=-8$$
$$y=\frac{2}{3} \quad \text{or} \quad y=\frac{8}{7}$$

Check $y=\frac{2}{3}$: $\left(\frac{\frac{2}{3}}{\frac{2}{3}-1}\right)^2=6\left(\frac{\frac{2}{3}}{\frac{2}{3}-1}\right)+16$

$$\frac{\frac{4}{9}}{\frac{1}{9}}=6\cdot\frac{\frac{2}{3}}{\left(-\frac{1}{3}\right)}+16$$
$$4=6(-2)+16$$
$$4=4$$

Check $y=\frac{8}{7}$: $\left(\frac{\frac{8}{7}}{\frac{8}{7}-1}\right)^2=6\left(\frac{\frac{8}{7}}{\frac{8}{7}-1}\right)+16$

$$\frac{\left(\frac{64}{49}\right)}{\left(\frac{1}{49}\right)}=6\left(\frac{\left(\frac{8}{7}\right)}{\left(\frac{1}{7}\right)}\right)+16$$
$$64=48+16$$
$$64=64$$

The solution set is $\left\{\frac{2}{3},\frac{8}{7}\right\}$.

75.
$$x^3-9x=0$$
$$x\left(x^2-9\right)=0$$
$$x(x-3)(x+3)=0$$
$$x=0 \quad \text{or} \quad x-3=0 \quad x+3=0$$
$$x=3 \qquad x=-3$$

The solution set is $\{-3,0,3\}$.

76.
$$x^4-x^2=0$$
$$x^2\left(x^2-1\right)=0$$
$$x^2(x-1)(x+1)=0$$
$$x^2=0 \quad \text{or} \quad x-1=0 \quad \text{or} \quad x+1=0$$
$$x=0 \qquad x=1 \qquad x=-1$$

The solution set is $\{-1,0,1\}$.

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77. $4x^3 = 3x^2$

$4x^3 - 3x^2 = 0$

$x^2(4x-3) = 0$

$x^2 = 0$ or $4x-3=0$

$x = 0$ $\quad 4x = 3$

$x = \frac{3}{4}$

The solution set is $\left\{0, \frac{3}{4}\right\}$.

78. $x^5 = 4x^3$

$x^5 - 4x^3 = 0$

$x^3(x^2-4) = 0$

$x^3(x-2)(x+2) = 0$

$x^3 = 0$ or $x-2=0$ or $x+2=0$

$x = 0$ $\quad x = 2$ $\quad x = -2$

The solution set is $\{-2, 0, 2\}$.

79. $x^3 + x^2 - 20x = 0$

$x(x^2 + x - 20) = 0$

$x(x+5)(x-4) = 0$

$x = 0$ or $x+5=0$ or $x-4=0$

$x = -5$ $\quad x = 4$

The solution set is $\{-5, 0, 4\}$.

80. $x^3 + 6x^2 - 7x = 0$

$x(x^2 + 6x - 7) = 0$

$x(x+7)(x-1) = 0$

$x = 0$ or $x+7=0$ or $x-1=0$

$x = -7$ $\quad x = 1$

The solution set is $\{-7, 0, 1\}$.

81. $x^3 + x^2 - x - 1 = 0$

$x^2(x+1) - 1(x+1) = 0$

$(x+1)(x^2-1) = 0$

$(x+1)(x-1)(x+1) = 0$

$x+1=0$ or $x-1=0$

$x = -1$ $\quad x = 1$

The solution set is $\{-1, 1\}$.

82. $x^3 + 4x^2 - x - 4 = 0$

$x^2(x+4) - 1(x+4) = 0$

$(x+4)(x^2-1) = 0$

$(x+4)(x-1)(x+1) = 0$

$x+4=0$ or $x-1=0$ or $x+1=0$

$x = -4$ $\quad x = 1$ $\quad x = -1$

The solution set is $\{-4, -1, 1\}$.

83. $x^3 - 3x^2 - 16x + 48 = 0$

$x^2(x-3) - 16(x-3) = 0$

$(x-3)(x^2-16) = 0$

$(x-3)(x-4)(x+4) = 0$

$x-3=0$ or $x-4=0$ or $x+4=0$

$x = 3$ $\quad x = 4$ $\quad x = -4$

The solution set is $\{-4, 3, 4\}$.

84. $x^3 - 3x^2 - x + 3 = 0$

$x^2(x-3) - 1(x-3) = 0$

$(x-3)(x^2-1) = 0$

$(x-3)(x-1)(x+1) = 0$

$x-3=0$ or $x-1=0$ or $x+1=0$

$x = 3$ $\quad x = 1$ $\quad x = -1$

The solution set is $\{-1, 1, 3\}$.

85. $2x^3 + 4 = x^2 + 8x$

$2x^3 - x^2 - 8x + 4 = 0$

$x^2(2x-1) - 4(2x-1) = 0$

$(2x-1)(x^2-4) = 0$

$(2x-1)(x-2)(x+2) = 0$

$2x-1=0$ or $x-2=0$ or $x+2=0$

$2x = 1$ $\quad x = 2$ $\quad x = -2$

$x = \frac{1}{2}$

The solution set is $\left\{-2, \frac{1}{2}, 2\right\}$.

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86. $3x^3+4x^2=27x+36$

$3x^3+4x^2-27x-36=0$

$x^2(3x+4)-9(3x+4)=0$

$(3x+4)(x^2-9)=0$

$(3x+4)(x-3)(x+3)=0$

$3x+4=0$ or $x-3=0$ or $x+3=0$

$3x=-4$ $x=3$ $x=-3$

$x=-\frac{4}{3}$

The solution set is $\left\{-3,-\frac{4}{3},3\right\}$.

87. $3x^3+12x=7x^2+28$

$3x^3-7x^2+12x-28=0$

$x^2(3x-7)+4(3x-7)=0$

$(3x-7)(x^2+4)=0$

$3x-7=0$ or $x^2+4=0$

$3x=7$ $x^2=-4$

$x=\frac{7}{3}$ no real solutions

The solution set is $\left\{\frac{7}{3}\right\}$.

88. $3x^3+12x=5x^2+20$

$3x^3-5x^2+12x-20=0$

$x^2(3x-5)+4(3x-5)=0$

$(3x-5)(x^2+4)=0$

$3x-5=0$ or $x^2+4=0$

$3x=5$ $x^2=-4$

$x=\frac{5}{3}$ no real solutions

The solution set is $\left\{\frac{5}{3}\right\}$.

89. $x(x^2-3x)^{1/3}+2(x^2-3x)^{4/3}=0$

$(x^2-3x)^{1/3}\left[x+2(x^2-3x)\right]=0$

$(x^2-3x)^{1/3}(x+2x^2-6x)=0$

$(x^2-3x)^{1/3}(2x^2-5x)=0$

$(x^2-3x)^{1/3}=0$ or $2x^2-5x=0$

$x^2-3x=0$ or $2x^2-5x=0$

$x(x-3)=0$ or $x(2x-5)=0$

$x=0$ or $x=3$ or $x=0$ or $x=\frac{5}{2}$

The solution set is $\left\{0,\frac{5}{2},3\right\}$.

90. $3x(x^2+2x)^{1/2}-2(x^2+2x)^{3/2}=0$

$(x^2+2x)^{1/2}\left[3x-2(x^2+2x)\right]=0$

$(x^2+2x)^{1/2}(3x-2x^2-4x)=0$

$(x^2+2x)^{1/2}(-2x^2-x)=0$

$(x^2+2x)^{1/2}=0$ or $-2x^2-x=0$

$x^2+2x=0$ or $2x^2+x=0$

$x(x+2)=0$ or $x(2x+1)=0$

$x=0$ or $x=-2$ or $x=0$ or $x=-\frac{1}{2}$

Check $x=0$:

$3\cdot0(0^2+2\cdot0)^{1/2}-2(0^2+2\cdot0)^{3/2}=0$

$3\cdot0(0)^{1/2}-2(0)^{3/2}=0$

$0=0$

Check $x=-2$:

$3(-2)((-2)^2+2(-2))^{1/2}-2((-2)^2+2(-2))^{3/2}=0$

$3(-2)(4-4)^{1/2}-2(4-4)^{3/2}=0$

$3(-2)(0)^{1/2}-2(0)^{3/2}=0$

$3(-2)(0)-2(0)=0$

$0=0$

Check $x=-\frac{1}{2}$:

$3\left(-\frac{1}{2}\right)\left(\left(-\frac{1}{2}\right)^2+2\left(-\frac{1}{2}\right)\right)^{1/2}-2\left(\left(-\frac{1}{2}\right)^2+2\left(-\frac{1}{2}\right)\right)^{3/2}=0$

$3\left(-\frac{1}{2}\right)\left(\frac{1}{4}-1\right)^{1/2}-2\left(\frac{1}{4}-1\right)^{3/2}=0$

$3\left(-\frac{1}{2}\right)\left(-\frac{3}{4}\right)^{1/2}-2\left(-\frac{3}{4}\right)^{3/2}=0$

Not real

The solution set is $\{-2,0\}$.

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91. $x-4x^{1/2}+2=0$

Let $u=x^{1/2}$ so that $u^2=x^2$.

$u^2-4u+2=0$

$$u=\frac{-(-4)\pm\sqrt{(-4)^2-4(1)(2)}}{2}$$

$$=\frac{4\pm\sqrt{8}}{2}=\frac{4\pm2\sqrt{2}}{2}=2\pm\sqrt{2}$$

$u=2+\sqrt{2}$ or $u=2-\sqrt{2}$

$x^{1/2}=2+\sqrt{2}$ or $x^{1/2}=2-\sqrt{2}$

$\left(x^{1/2}\right)^2=\left(2+\sqrt{2}\right)^2$ or $\left(x^{1/2}\right)^2=\left(2-\sqrt{2}\right)^2$

$x=\left(2+\sqrt{2}\right)^2$ or $x=\left(2-\sqrt{2}\right)^2$

Check $x=\left(2+\sqrt{2}\right)^2$:

$\left(2+\sqrt{2}\right)^2-4\left(2+\sqrt{2}\right)+2=0$

$4+4\sqrt{2}+2-8-4\sqrt{2}+2=0$

$0=0$

Check $x=\left(2-\sqrt{2}\right)^2$:

$\left(2-\sqrt{2}\right)^2-4\left(2-\sqrt{2}\right)+2=0$

$4-4\sqrt{2}+2-8+4\sqrt{2}+2=0$

$0=0$

The solution set is

$\left\{\left(2-\sqrt{2}\right)^2,\ \left(2+\sqrt{2}\right)^2\right\}\approx\{0.34,\ 11.66\}$.

92. $x^{2/3}+4x^{1/3}+2=0$

Let $u=x^{1/3}$ so that $u^2=x^{2/3}$.

$u^2+4u+2=0$

$$u=\frac{-4\pm\sqrt{4^2-4(1)(2)}}{2(1)}$$

$$=\frac{-4\pm\sqrt{8}}{2}=\frac{-4\pm2\sqrt{2}}{2}=-2\pm\sqrt{2}$$

$u=-2+\sqrt{2}$ or $u=-2-\sqrt{2}$

$x^{1/3}=-2+\sqrt{2}$ or $x^{1/3}=-2-\sqrt{2}$

$x=\left(-2+\sqrt{2}\right)^3$ or $x=\left(-2-\sqrt{2}\right)^3$

Check $x=\left(-2+\sqrt{2}\right)^3$:

$\left(\left(-2+\sqrt{2}\right)^3\right)^{2/3}+4\left(\left(-2+\sqrt{2}\right)^3\right)^{1/3}+2=0$

$\left(-2+\sqrt{2}\right)^2+4\left(-2+\sqrt{2}\right)+2=0$

$4-4\sqrt{2}+2-8+4\sqrt{2}+2=0$

$0=0$

Check $x=\left(-2-\sqrt{2}\right)^3$:

$\left(\left(-2-\sqrt{2}\right)^3\right)^{2/3}+4\left(\left(-2-\sqrt{2}\right)^3\right)^{1/3}+2=0$

$\left(-2-\sqrt{2}\right)^2+4\left(-2-\sqrt{2}\right)+2=0$

$4+4\sqrt{2}+2-8-4\sqrt{2}+2=0$

$0=0$

The solution set is

$\left\{\left(-2-\sqrt{2}\right)^3,\ \left(-2+\sqrt{2}\right)^3\right\}\approx\{-39.80,\ -0.20\}$.

93. $x^4+\sqrt{3}x^2-3=0$

Let $u=x^2$ so that $u^2=x^4$.

$u^2+\sqrt{3}u-3=0$

$$u=\frac{-\sqrt{3}\pm\sqrt{\left(\sqrt{3}\right)^2-4(1)(-3)}}{2(1)}=\frac{-\sqrt{3}\pm\sqrt{15}}{2}$$

$u=\dfrac{-\sqrt{3}+\sqrt{15}}{2}$ or $u=\dfrac{-\sqrt{3}-\sqrt{15}}{2}$

$x^2=\dfrac{-\sqrt{3}+\sqrt{15}}{2}$ or $x^2=\dfrac{-\sqrt{3}-\sqrt{15}}{2}$

$x=\pm\sqrt{\dfrac{-\sqrt{3}+\sqrt{15}}{2}}$ or $x=\pm\sqrt{\dfrac{-\sqrt{3}-\sqrt{15}}{2}}$

Not real

Check $x=\sqrt{\dfrac{-\sqrt{3}+\sqrt{15}}{2}}$:

$$\left(\sqrt{\frac{-\sqrt{3}+\sqrt{15}}{2}}\right)^4+\sqrt{3}\left(\sqrt{\frac{-\sqrt{3}+\sqrt{15}}{2}}\right)^2-3=0$$

$$\left(\frac{-\sqrt{3}+\sqrt{15}}{2}\right)^2+\sqrt{3}\left(\frac{-\sqrt{3}+\sqrt{15}}{2}\right)-3=0$$

$$\frac{3-2\sqrt{3}\sqrt{15}+15}{4}+\frac{\sqrt{3}\left(-\sqrt{3}\right)+\sqrt{3}\sqrt{15}}{2}-3=0$$

$$\frac{18-2\sqrt{45}}{4}+\frac{-3+\sqrt{45}}{2}-3=0$$

$$\frac{9-\sqrt{45}}{2}+\frac{-3+\sqrt{45}}{2}-3=0$$

$$\frac{9-\sqrt{45}-3+\sqrt{45}}{2}-3=0$$

$3-3=0$

$0=0$

Check $x=-\sqrt{\dfrac{-\sqrt{3}+\sqrt{15}}{2}}$:

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$$\left(-\sqrt{\frac{-\sqrt{3}+\sqrt{15}}{2}}\right)^4+\sqrt{3}\left(-\sqrt{\frac{-\sqrt{3}+\sqrt{15}}{2}}\right)^2-3=0$$
$$\left(\frac{-\sqrt{3}+\sqrt{15}}{2}\right)^2+\sqrt{3}\left(\frac{-\sqrt{3}+\sqrt{15}}{2}\right)-3=0$$
$$\frac{3-2\sqrt{3}\sqrt{15}+15}{4}+\frac{\sqrt{3}\left(-\sqrt{3}\right)+\sqrt{3}\sqrt{15}}{2}-3=0$$
$$\frac{18-2\sqrt{45}}{4}+\frac{-3+\sqrt{45}}{2}-3=0$$
$$\frac{9-\sqrt{45}}{2}+\frac{-3+\sqrt{45}}{2}-3=0$$
$$\frac{9-\sqrt{45}-3+\sqrt{45}}{2}-3=0$$
$$3-3=0$$
$$0=0$$

The solution set is

$$\left\{-\sqrt{\frac{-\sqrt{3}+\sqrt{15}}{2}},\ \sqrt{\frac{-\sqrt{3}+\sqrt{15}}{2}}\right\}\approx\{-1.03,\ 1.03\}.$$

94. $x^4+\sqrt{2}x^2-2=0$

Let $u=x^2$ so that $u^2=x^4$.

$$u^2+\sqrt{2}u-2=0$$
$$u=\frac{-\sqrt{2}\pm\sqrt{\left(\sqrt{2}\right)^2-4(1)(-2)}}{2(1)}=\frac{-\sqrt{2}\pm\sqrt{10}}{2}$$
$$u=\frac{-\sqrt{2}+\sqrt{10}}{2}\quad\text{or}\quad u=\frac{-\sqrt{2}-\sqrt{10}}{2}$$
$$x^2=\frac{-\sqrt{2}+\sqrt{10}}{2}\quad\text{or}\quad x^2=\frac{-\sqrt{2}-\sqrt{10}}{2}$$
$$x=\pm\sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}}\quad\text{or}\quad x=\pm\sqrt{\frac{-\sqrt{2}-\sqrt{10}}{2}}$$
Not real

Check $x=\sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}}$:

$$\left(\sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}}\right)^4+\sqrt{2}\left(\sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}}\right)^2-2=0$$
$$\left(\frac{-\sqrt{2}+\sqrt{10}}{2}\right)^2+\sqrt{2}\left(\frac{-\sqrt{2}+\sqrt{10}}{2}\right)-2=0$$
$$\frac{12-2\sqrt{20}}{4}+\frac{-2+\sqrt{20}}{2}-2=0$$
$$\frac{6-\sqrt{20}-2+\sqrt{20}}{2}-2=0$$
$$2-2=0$$
$$0=0$$

Check $x=-\sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}}$:

$$\left(-\sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}}\right)^4+\sqrt{2}\left(-\sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}}\right)^2-2=0$$
$$\left(\frac{-\sqrt{2}+\sqrt{10}}{2}\right)^2+\sqrt{2}\left(\frac{-\sqrt{2}+\sqrt{10}}{2}\right)-2=0$$
$$\frac{12-2\sqrt{20}}{4}+\frac{-2+\sqrt{20}}{2}-2=0$$
$$\frac{6-\sqrt{20}-2+\sqrt{20}}{2}-2=0$$
$$2-2=0$$
$$0=0$$

The solution set is

$$\left\{-\sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}},\ \sqrt{\frac{-\sqrt{2}+\sqrt{10}}{2}}\right\}\approx\{-0.93,\ 0.93\}.$$

95. $\pi(1+t)^2=\pi+1+t$

Let $u=1+t$ so that $u^2=(1+t)^2$.

$$\pi u^2=\pi+u$$
$$\pi u^2-u-\pi=0$$
$$u=\frac{-(-1)\pm\sqrt{(-1)^2-4(\pi)(-\pi)}}{2(\pi)}=\frac{1\pm\sqrt{1+4\pi^2}}{2\pi}$$
$$1+t=\frac{1\pm\sqrt{1+4\pi^2}}{2\pi}$$
$$t=-1+\frac{1\pm\sqrt{1+4\pi^2}}{2\pi}$$

Check $t=-1+\frac{1+\sqrt{1+4\pi^2}}{2\pi}$:

$$\pi\left(\frac{1+\sqrt{1+4\pi^2}}{2\pi}\right)^2=\pi+\frac{1+\sqrt{1+4\pi^2}}{2\pi}$$
$$\pi\left(\frac{1+2\sqrt{1+4\pi^2}+1+4\pi^2}{4\pi^2}\right)=\pi+\frac{1+\sqrt{1+4\pi^2}}{2\pi}$$
$$\frac{2+2\sqrt{1+4\pi^2}+4\pi^2}{4\pi}=\frac{2\pi^2+1+\sqrt{1+4\pi^2}}{2\pi}$$
$$\frac{1+\sqrt{1+4\pi^2}+2\pi^2}{2\pi}=\frac{2\pi^2+1+\sqrt{1+4\pi^2}}{2\pi}$$

Check $t=-1+\frac{1-\sqrt{1+4\pi^2}}{2\pi}$:

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$$\pi\left(\frac{1-\sqrt{1+4\pi^2}}{2\pi}\right)^2 = \pi + \frac{1-\sqrt{1+4\pi^2}}{2\pi}$$

$$\pi\left(\frac{1-2\sqrt{1+4\pi^2}+1+4\pi^2}{4\pi^2}\right) = \pi + \frac{1-\sqrt{1+4\pi^2}}{2\pi}$$

$$\frac{2-2\sqrt{1+4\pi^2}+4\pi^2}{4\pi} = \frac{2\pi^2+1-\sqrt{1+4\pi^2}}{2\pi}$$

$$\frac{1-\sqrt{1+4\pi^2}+2\pi^2}{2\pi} = \frac{2\pi^2+1-\sqrt{1+4\pi^2}}{2\pi}$$

The solution set is

$$\left\{-1+\frac{1-\sqrt{1+4\pi^2}}{2\pi}, -1+\frac{1+\sqrt{1+4\pi^2}}{2\pi}\right\}$$

$$\approx \{-1.85,\ 0.17\}.$$

96. $\pi(1+r)^2 = 2+\pi(1+r)$

Let $u = 1+r$ so that $u^2 = (1+r)^2$.

$$\pi u^2 = 2+\pi u$$

$$\pi u^2 - \pi u - 2 = 0$$

$$u = \frac{-(-\pi) \pm \sqrt{(-\pi)^2 + 4(\pi)(-2)}}{2(\pi)}$$

$$= \frac{\pi \pm \sqrt{\pi^2 - 8\pi}}{2\pi}$$

$$1+r = \frac{\pi \pm \sqrt{\pi^2+8\pi}}{2\pi}$$

$$r = -1 + \frac{\pi \pm \sqrt{\pi^2+8\pi}}{2\pi}$$

Check $r = -1+\frac{\pi+\sqrt{\pi^2+8\pi}}{2\pi}$:

$$\pi\left(\frac{\pi+\sqrt{\pi^2+8\pi}}{2\pi}\right)^2 = 2+\pi\left(\frac{\pi+\sqrt{\pi^2+8\pi}}{2\pi}\right)$$

$$\pi\left(\frac{\pi^2+2\pi\sqrt{\pi^2+8\pi}+\pi^2+8\pi}{4\pi^2}\right) = 2+\pi\left(\frac{\pi+\sqrt{\pi^2+8\pi}}{2\pi}\right)$$

$$\frac{2\pi^2+2\pi\sqrt{\pi^2+8\pi}+8\pi}{4\pi} = 2+\frac{\pi+\sqrt{\pi^2+8\pi}}{2}$$

$$\frac{\pi+\sqrt{\pi^2+8\pi}+4}{2} = \frac{4+\pi+\sqrt{\pi^2+8\pi}}{2}$$

Check $r = -1+\frac{\pi-\sqrt{\pi^2+8\pi}}{2\pi}$:

$$\pi\left(\frac{\pi-\sqrt{\pi^2+8\pi}}{2\pi}\right)^2 = 2+\pi\left(\frac{\pi-\sqrt{\pi^2+8\pi}}{2\pi}\right)$$

$$\pi\left(\frac{\pi^2-2\pi\sqrt{\pi^2+8\pi}+\pi^2+8\pi}{4\pi^2}\right) = 2+\pi\left(\frac{\pi-\sqrt{\pi^2+8\pi}}{2\pi}\right)$$

$$\frac{2\pi^2-2\pi\sqrt{\pi^2+8\pi}+8\pi}{4\pi} = 2+\frac{\pi-\sqrt{\pi^2+8\pi}}{2}$$

$$\frac{\pi-\sqrt{\pi^2+8\pi}+4}{2} = \frac{4+\pi-\sqrt{\pi^2+8\pi}}{2}$$

The solution set is

$$\left\{-1+\frac{\pi-\sqrt{\pi^2+8\pi}}{2\pi},\ -1+\frac{\pi+\sqrt{\pi^2+8\pi}}{2\pi}\right\}$$

$$\approx \{-1.44,\ 0.44\}.$$

97. $3x^2+7x-20=0$

$$(3x-5)(x+4)=0$$

$3x-5=0$ or $x+4=0$

$3x=5$ $\qquad$ $x=-4$

$x=\frac{5}{3}$

The solution set is $\left\{-4, \frac{5}{3}\right\}$.

98. $2x^2-13x+21=0$

$$(2x-7)(x-3)=0$$

$2x-7=0$ or $x-3=0$

$2x=7$ $\qquad$ $x=3$

$x=\frac{7}{2}$

The solution set is $\left\{\frac{7}{2}, 3\right\}$.

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99. $5a^3 - 45a = -2a^2 + 18$

$5a^3 + 2a^2 - 45a - 18 = 0$

$a^2(5a+2) - 9(5a+2) = 0$

$(a^2 - 9)(5a+2) = 0$

$(a-3)(a+3)(5a+2) = 0$

$a-3=0$ or $a+3=0$ or $5a+2=0$

$a=3$ $\quad a=-3$ $\quad 5a=-2$

$a=-\frac{2}{5}$

The solution set is $\left\{-3, -\frac{2}{5}, 3\right\}$.

100. $3z^3 - 12z = -5z^2 + 20$

$3z^3 + 5z^2 - 12z - 20 = 0$

$z^2(3z+5) - 4(3z+5) = 0$

$(z^2 - 4)(3z+5) = 0$

$(z-2)(z+2)(3z+5) = 0$

$z-2=0$ or $z+2=0$ $\quad 3z+5=0$

$z=2$ $\quad z=-2$ $\quad 3z=-5$

$z=-\frac{5}{3}$

The solution set is $\left\{-2, -\frac{5}{3}, 2\right\}$.

101. $4(w-3) = w+3$

$4w - 12 = w + 3$

$3w = 15$

$w = 5$

The solution set is $\{5\}$.

102. $6(k+3) - 2k = 12$

$6k + 18 - 2k = 12$

$4k = -6$

$k = -\frac{3}{2}$

The solution set is $\left\{-\frac{3}{2}\right\}$.

103. $\left(\frac{v}{v+1}\right)^2 + \frac{2v}{v+1} = 8$

Let $u = \frac{v}{v+1}$. Rewrite the equation:

$u^2 + 2u = 8$

$u^2 + 2u - 8 = 0$

$(u-2)(u+4) = 0$

$u = 2$ or $u = -4$

Go back in terms of v and solve:

$\frac{v}{v+1} = 2$ or $\frac{v}{v+1} = -4$

$v = 2v + 2$ $\quad v = -4v - 4$

$-v = 2$ $\quad 5v = -4$

$v = -2$ $\quad v = -\frac{4}{5}$

The solution set is $\left\{-2, -\frac{4}{5}\right\}$.

104. $\left(\frac{y}{y-1}\right)^2 - \frac{6y}{y-1} = 7$

Let $u = \frac{y}{y-1}$. Rewrite the equation:

$u^2 - 6u = 7$

$u^2 - 6u - 7 = 0$

$(u-7)(u+1) = 0$

$u = 7$ or $u = -1$

Go back in terms of y and solve:

$\frac{y}{y-1} = 7$ or $\frac{y}{y-1} = -1$

$y = 7y - 7$ $\quad y = -y + 1$

$-6y = -7$ $\quad 2y = 1$

$y = \frac{7}{6}$ $\quad y = \frac{1}{2}$

The solution set is $\left\{\frac{1}{2}, \frac{7}{6}\right\}$.

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105. $\sqrt{2x+5}-x=1$

$\sqrt{2x+5}=x+1$

$\left(\sqrt{2x+5}\right)^2=(x+1)^2$

$2x+5=x^2+2x+1$

$x^2-4=0$

$(x-2)(x+2)=0$

$x=2$ or $x=-2$

Check:

$\sqrt{2(-2)+5}-(-2)=1$ $\quad\sqrt{1}+2=1$ $\quad 3\neq 1$

$\sqrt{2(2)+5}-(2)=1$ $\quad\sqrt{9}-2=1$ $\quad 1=1$ T

The solution set is $\{2\}$.

106. $\sqrt{3x+1}-2x=-6$

$\sqrt{3x+1}=2x-6$

$\left(\sqrt{3x+1}\right)^2=(2x-6)^2$

$3x+1=4x^2-24x+36$

$4x^2-27x+35=0$

$(4x-7)(x-5)=0$

$4x-7=0$ or $x-5=0$

$4x=7$ $\quad x=5$

$x=\frac{7}{4}$

Check:

$\sqrt{3\left(\frac{7}{4}\right)+1}-2\left(\frac{7}{4}\right)=-6$ $\quad\frac{5}{2}-\frac{7}{2}=-6$ $\quad -1\neq -6$

$\sqrt{3(5)+1}-2(5)=-6$ $\quad 4-10=-6$ $\quad -6=-6$ T

The solution set is $\{5\}$.

107. $3m^2+6m=-1$

$3m^2+6m+1=0$

$a=3,\ b=6,\ c=1$

$m=\frac{-6\pm\sqrt{6^2-4(3)(1)}}{2(3)}=\frac{-6\pm\sqrt{24}}{6}$

$=\frac{-6\pm 2\sqrt{6}}{6}=\frac{-3\pm\sqrt{6}}{3}$

The solution set is $\left\{\frac{-3-\sqrt{6}}{3},\frac{-3+\sqrt{6}}{3}\right\}$.

108. $4y^2-8y=3$

$4y^2-8y-3=0$

$a=4,\ b=-8,\ c=-3$

$y=\frac{-(-8)\pm\sqrt{(-8)^2-4(4)(-3)}}{2(4)}$

$=\frac{8\pm\sqrt{112}}{8}=\frac{8\pm 4\sqrt{7}}{8}=\frac{2\pm\sqrt{7}}{2}$

The solution set is $\left\{\frac{2-\sqrt{7}}{2},\frac{2+\sqrt{7}}{2}\right\}$.

109. $\sqrt[4]{5x^2-6}=x$

$5x^2-6=x^4$

$x^4-5x^2+6=0$

$\left(x^2-2\right)\left(x^2-3\right)=0$

$x^2-2=0$ or $x^2-3=0$

$x^2=2$ $\quad x^2=3$

$x=\pm\sqrt{2}$ $\quad x=\pm\sqrt{3}$

Check:

$\sqrt[4]{5(\sqrt{2})^2-6}=\sqrt[4]{5(2)-6}$

$=\sqrt[4]{4}=\sqrt{2}$

$\sqrt[4]{5(-\sqrt{2})^2-6}=\sqrt[4]{5(2)-6}$

$=\sqrt[4]{4}=\sqrt{2}\neq-\sqrt{2}$

$\sqrt[4]{5(\sqrt{3})^2-6}=\sqrt[4]{5(3)-6}$

$=\sqrt[4]{9}=\sqrt{3}$

$\sqrt[4]{5(-\sqrt{3})^2-6}=\sqrt[4]{5(3)-6}$

$=\sqrt[4]{9}=\sqrt{3}\neq-\sqrt{3}$

The solution set is $\left\{\sqrt{2},\sqrt{3}\right\}$.

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110. $\sqrt[4]{4-3x^2} = x$

$4-3x^2 = x^4$

$x^4 + 3x^2 - 4 = 0$

$(x^2-1)(x^2+4) = 0$

$x^2 - 1 = 0$ or $x^2 + 4 = 0$

$x^2 = 1$ $\quad$ $x^2 = -4$

$x = \pm 1$ $\quad$ no real solution

Check:

$\sqrt[4]{4-3(1)^2} = \sqrt[4]{4-3}$ $\quad$ $\sqrt[4]{4-3(-1)^2} = \sqrt[4]{4-3}$

$= \sqrt[4]{1} = 1$ $\quad$ $= \sqrt[4]{1} = 1 \neq -1$

The solution set is $\{1\}$.

111. $k^2 - k = 12$

$k^2 - k - 12 = 0$

$(k-4)(k+3) = 0$

$k = 4$ or $k = -3$

$\frac{x+3}{x-3} = 4$ or $\frac{x+3}{x-3} = -3$

$x + 3 = 4x - 12$ or $x + 3 = -3x + 9$

$3x = 15$ or $4x = 6$

$x = 5$ or $x = \frac{6}{4} = \frac{3}{2}$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{\frac{3}{2}, 5\right\}$.

112. $k^2 - 3k = 28$

$k^2 - 3k - 28 = 0$

$(k+4)(k-7) = 0$

$k = -4$ or $k = 7$

$\frac{x+3}{x-4} = -4$ or $\frac{x+3}{x-4} = 7$

$x + 3 = -4x + 16$ or $x + 3 = 7x - 28$

$5x = 13$ or $-6x = -31$

$x = \frac{13}{5} = 2.6$ or $x = \frac{31}{6} \approx 5.17$

Neither of these values causes a denominator to equal zero, so the solution set is $\left\{\frac{13}{5}, \frac{31}{6}\right\}$.

113. Solve the equation $\frac{\sqrt{s}}{4} + \frac{s}{1100} = 4$.

$\frac{s}{1100} + \frac{\sqrt{s}}{4} - 4 = 0$

$(1100)\left(\frac{s}{1100} + \frac{\sqrt{s}}{4} - 4\right) = (0)(1100)$

$s + 275\sqrt{s} - 4400 = 0$

Let $u = \sqrt{s}$, so that $u^2 = s$.

$u^2 + 275u - 4400 = 0$

$u = \frac{-275 \pm \sqrt{275^2 - 4(1)(-4400)}}{2}$

$= \frac{-275 \pm \sqrt{93,225}}{2}$

$u \approx 15.1638$ or $u \approx -290.1638$

Since $u = \sqrt{s}$, it must be positive, so

$s = u^2 \approx (15.1638)^2 \approx 229.94$

The distance to the water's surface is approximately 229.94 feet.

114. $T = \sqrt[4]{\frac{LH^2}{25}}$

Let $T = 4$ and $H = 10$, and solve for L.

$4 = \sqrt[4]{\frac{L(10)^2}{25}}$

$4 = \sqrt[4]{4L}$

$(4)^4 = \left(\sqrt[4]{4L}\right)^4$

$256 = 4L$

$64 = L$

The crushing load is 64 tons.

115. $T = 2\pi\sqrt{\frac{l}{32}}$

Let $T = 16.5$ and solve for l.

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$$16.5 = 2\pi\sqrt{\frac{l}{32}}$$
$$\frac{16.5}{2\pi} = \sqrt{\frac{l}{32}}$$
$$\left(\frac{16.5}{2\pi}\right)^2 = \left(\sqrt{\frac{l}{32}}\right)^2$$
$$\left(\frac{16.5}{2\pi}\right)^2 = \frac{l}{32}$$
$$l = 32\left(\frac{16.5}{2\pi}\right)^2 \approx 220.7$$

The length was approximately 220.7 feet.

116.
$$\sqrt{3x+5} - \sqrt{x-2} = \sqrt{x+3}$$
$$\left(\sqrt{3x+5} - \sqrt{x-2}\right)^2 = \left(\sqrt{x+3}\right)^2$$
$$3x+5-2\sqrt{(3x+5)(x-2)} + (x-2) = x+3$$
$$4x+3-2\sqrt{(3x+5)(x-2)} = x+3$$
$$2\sqrt{3x^2-x-10} = 3x$$
$$4\left(3x^2-x-10\right) = 9x^2$$
$$3x^2-4x-40 = 0$$
$$x = \frac{4 \pm \sqrt{(-4)^2 - 4(3)(-40)}}{6}$$
$$= \frac{4 \pm \sqrt{496}}{6} = \frac{4 \pm 4\sqrt{31}}{6}$$
$$= \frac{4 \pm 4\sqrt{31}}{6}$$
$$= \frac{2 \pm 2\sqrt{31}}{3}$$

Since x > 2, the negative solution is extraneous.

The solution set is $\left\{\frac{2+2\sqrt{31}}{3}\right\}$.

117.
$$\sqrt[4]{\sqrt[3]{\sqrt{x-7}-10}+18} = 2$$
$$\left(\sqrt[4]{\sqrt[3]{\sqrt{x-7}-10}+18}\right)^4 = (2)^4$$
$$\sqrt[3]{\sqrt{x-7}-10}+18 = 16$$
$$\left(\sqrt[3]{\sqrt{x-7}-10}\right)^3 = (-2)^3$$
$$\sqrt{x-7}-10 = -8$$
$$\left(\sqrt{x-7}\right)^2 = (2)^2$$
$$x-7 = 4$$
$$x = 11$$

The solution set is $\{11\}$

118.
$$12x^{7/5} + 3x^{2/5} = 13x^{9/10}$$
$$12x^{14/10} + 3x^{4/10} - 13x^{9/10} = 0$$
$$x^{4/10}\left(12x - 13x^{1/2} + 3\right) = 0$$
$$x^{4/10} = 0 \Rightarrow x = 0$$

To solve $12x - 13x^{1/2} + 3 = 0$, let $u = x^{1/2}$

Then $12u^2 - 13u + 3 = 0$

$$(4u-3)(3u-1) = 0$$
$$u = x^{1/2} = \frac{3}{4} \text{ or } x^{1/2} = \frac{1}{3}$$
$$x = \frac{9}{16} \qquad x = \frac{1}{9}$$

The solution set is $\left\{0, \frac{9}{16}, \frac{1}{9}\right\}$

119.
$$z^6 + 28z^3 + 27 = 0$$
$$(z^3+27)(z^3+1) = 0$$
$$(z+3)(z^2-3z+9)(z+1)(z^2-z+1) = 0$$
$$z+3 = 0 \quad \text{or} \quad z+1 = 0$$
$$z = -3 \quad \text{or} \quad z = -1$$

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$a=1, b=-3, c=9$

$$x=\frac{-(-3)\pm\sqrt{(-3)^2-4(1)(9)}}{2}$$

$$=\frac{3\pm\sqrt{-27}}{2}=\frac{3\pm 3\sqrt{3}i}{2}$$

Also,

$a=1, b=-1, c=1$

$$x=\frac{-(-1)\pm\sqrt{(-1)^2-4(1)1}}{2}$$

$$=\frac{1\pm\sqrt{-3}}{2}=\frac{1\pm\sqrt{3}i}{2}$$

The solution set is $\left\{-3,-1,\frac{1\pm\sqrt{3}i}{2},\frac{3\pm 3\sqrt{3}i}{2}\right\}$.

120. Answers will vary. One example: $\sqrt{x+1}=-1$.

121. Answers will vary. One example: $x-\sqrt{x}-2=0$.

122. Answers will vary.

123. Jane did not check her solutions and included the extraneous solution, $x=-1$.

$\sqrt{2x+3}-x=0$

$\sqrt{2x+3}=x$

$\left(\sqrt{2x+3}\right)^2=x^2$

$2x+3=x^2$

$x^2-2x-3=0$

$(x-3)(x+1)=0$

$x=3$ or $x=-1$

Check:

$\sqrt{2(3)+3}-3=0$ | $\sqrt{2(-1)+3}-(-1)=0$

$\sqrt{9}-3=0$ | $\sqrt{1}+1=0$

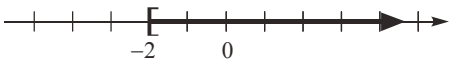
$3-3=0$ | $1+1=0$

$0=0$ T | $2\neq 0$

The solution set is $\{3\}$.

Section 1.5

1. $x\geq -2$



2. False.

3. closed interval

4. multiplication properties (for inequalities)

5. True. This follows from the addition property for inequalities.

6. True. This follows from the addition property for inequalities.

7. True;. This follows from the multiplication property for inequalities.

8. False. Since both sides of the inequality are being divided by a negative number, the sense, or direction, of the inequality must be reversed. That is, $\frac{a}{c}>\frac{b}{c}$.

9. True

10. False; either or both endpoints could be any real number.

11. d

12. c

13. Interval: $[0,2]$
Inequality: $0\leq x\leq 2$

14. Interval: $(-1,2)$
Inequality: $-1<x<2$

15. Interval: $[2,\infty)$
Inequality: $x\geq 2$

16. Interval: $(-\infty,0]$
Inequality: $x\leq 0$

17. Interval: $[0,3)$
Inequality: $0\leq x<3$

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18. Interval: $(-1,1]$
Inequality: $-1 < x \le 1$

19. **a.**
$$3 < 5$$
$$3+3 < 5+3$$
$$6 < 8$$

b.
$$3 < 5$$
$$3-5 < 5-5$$
$$-2 < 0$$

c.
$$3 < 5$$
$$3(3) < 3(5)$$
$$9 < 15$$

d.
$$3 < 5$$
$$-2(3) > -2(5)$$
$$-6 > -10$$

20. **a.**
$$2 > 1$$
$$2+3 > 1+3$$
$$5 > 4$$

b.
$$2 > 1$$
$$2-5 > 1-5$$
$$-3 > -4$$

c.
$$2 > 1$$
$$3(2) > 3(1)$$
$$6 > 3$$

d.
$$2 > 1$$
$$-2(2) < -2(1)$$
$$-4 < -2$$

21. **a.**
$$4 > -3$$
$$4+3 > -3+3$$
$$7 > 0$$

b.
$$4 > -3$$
$$4-5 > -3-5$$
$$-1 > -8$$

c.
$$4 > -3$$
$$3(4) > 3(-3)$$
$$12 > -9$$

d.
$$4 > -3$$
$$-2(4) < -2(-3)$$
$$-8 < 6$$

22. **a.**
$$-3 > -5$$
$$-3+3 > -5+3$$
$$0 > -2$$

b.
$$-3 > -5$$
$$-3-5 > -5-5$$
$$-8 > -10$$

c.
$$-3 > -5$$
$$3(-3) > 3(-5)$$
$$-9 > -15$$

d.
$$-3 > -5$$
$$-2(-3) < -2(-5)$$
$$6 < 10$$

23. **a.**
$$2x+1 < 2$$
$$2x+1+3 < 2+3$$
$$2x+4 < 5$$

b.
$$2x+1 < 2$$
$$2x+1-5 < 2-5$$
$$2x-4 < -3$$

c.
$$2x+1 < 2$$
$$3(2x+1) < 3(2)$$
$$6x+3 < 6$$

d.
$$2x+1 < 2$$
$$-2(2x+1) > -2(2)$$
$$-4x-2 > -4$$

24. **a.**
$$1-2x > 5$$
$$1-2x+3 > 5+3$$
$$4-2x > 8$$

b.
$$1-2x > 5$$
$$1-2x-5 > 5-5$$
$$-4-2x > 0$$

c.
$$1-2x > 5$$
$$3(1-2x) > 3(5)$$
$$3-6x > 15$$

d.
$$1-2x > 5$$
$$-2(1-2x) < -2(5)$$
$$-2+4x < -10$$

25. $[0, 4]$



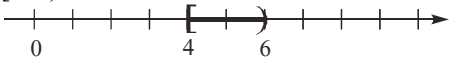
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26. $(-1, 5)$



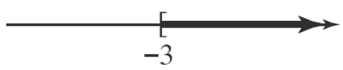
27. $[4, 6)$



28. $(-2, 0)$



29. $[-3, \infty)$



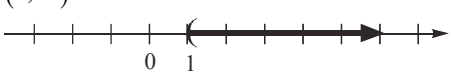
30. $(-\infty, 5]$



31. $(-\infty, -4)$



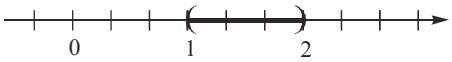
32. $(1, \infty)$



33. $2 \le x \le 5$



34. $1 < x < 2$



35. $-4 < x \le 3$



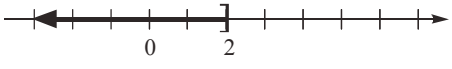
36. $0 \le x < 1$



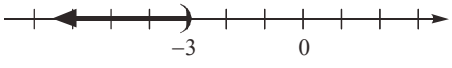
37. $x \ge 4$



38. $x \le 2$



39. $x < -3$



40. $x > -8$



41. If $x < 5$, then $x - 5 < 0$.

42. If $x < -4$, then $x + 4 < 0$.

43. If $x > -4$, then $x + 4 > 0$.

44. If $x > 6$, then $x - 6 > 0$.

45. If $x \ge -4$, then $3x \ge -12$.

46. If $x \le 3$, then $2x \le 6$.

47. If $x > 6$, then $-2x < -12$.

48. If $x > -2$, then $-4x < 8$.

49. If $x \ge 5$, then $-4x \le -20$.

50. If $x \le -4$, then $-3x \ge 12$.

51. If $8x > 40$, then $x > 5$.

52. If $3x \le 12$, then $x \le 4$.

53. If $-\frac{1}{2}x \le 3$, then $x \ge -6$.

54. If $-\frac{1}{4}x > 1$, then $x < -4$.

55. If $0 < 5 < x$, then $0 < \frac{1}{x} < \frac{1}{5}$

56. $0 < -4 < x$, then $\frac{1}{-4} \le \frac{1}{x} < 0$

57. $-5 < x < 0$, then $\frac{1}{x} < \frac{1}{-5} < 0$

58. $0 < x < 10$, then $0 < \frac{1}{10} \le \frac{1}{x}$

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59. $x+1<5$

$x+1-1<5-1$

$x<4$

$\{x \mid x<4\}$ or $(-\infty, 4)$



60. $x-6<1$

$x-6+6<1+6$

$x<7$

The solution set is $\{x \mid x<7\}$ or $(-\infty, 7)$.

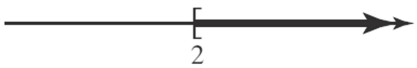


61. $3-5x \le -7$

$-5x \le -10$

$x \ge 2$

The solution set is $\{x \mid x \ge 2\}$ or $[2, \infty)$.

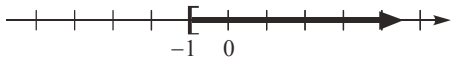


62. $2-3x \le 5$

$-3x \le 3$

$x \ge -1$

The solution set is $\{x \mid x \ge -1\}$ or $[-1, \infty)$.

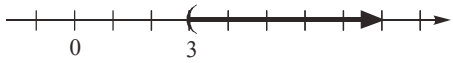


63. $3x-7>2$

$3x>9$

$x>3$

The solution set is $\{x \mid x>3\}$ or $(3, \infty)$.

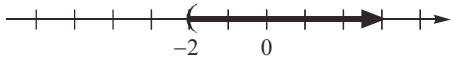


64. $2x+5>1$

$2x>-4$

$x>-2$

The solution set is $\{x \mid x>-2\}$ or $(-2, \infty)$.

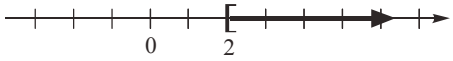


65. $3x-1 \ge 3+x$

$2x \ge 4$

$x \ge 2$

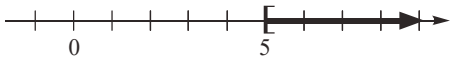
The solution set is $\{x \mid x \ge 2\}$ or $[2, \infty)$.



66. $2x-2 \ge 3+x$

$x \ge 5$

The solution set is $\{x \mid x \ge 5\}$ or $[5, \infty)$.



67. $-2(x+3)<8$

$-2x-6<8$

$-2x<14$

$x>-7$

The solution set is $\{x \mid x>-7\}$ or $(-7, \infty)$.



68. $-3(1-x)<12$

$-3+3x<12$

$3x<15$

$x<5$

The solution set is $\{x \mid x<5\}$ or $(-\infty, 5)$.



69. $4-3(1-x) \le 3$

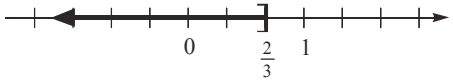
$4-3+3x \le 3$

$3x+1 \le 3$

$3x \le 2$

$x \le \frac{2}{3}$

The solution set is $\left\{x \mid x \le \frac{2}{3}\right\}$ or $\left(-\infty, \frac{2}{3}\right]$.



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70. $8-4(2-x) \le -2x$

$8-8+4x \le -2x$

$4x \le -2x$

$6x \le 0$

$x \le 0$

The solution set is $\{x \mid x \le 0\}$ or $(-\infty, 0]$.



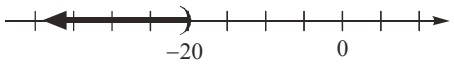
71. $\frac{1}{2}(x-4) > x+8$

$\frac{1}{2}x-2 > x+8$

$-\frac{1}{2}x > 10$

$x < -20$

The solution set is $\{x \mid x < -20\}$ or $(-\infty, -20)$.



72. $3x+4 > \frac{1}{3}(x-2)$

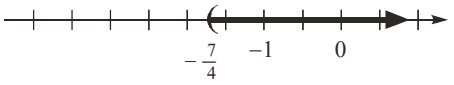
$3x+4 > \frac{1}{3}x-\frac{2}{3}$

$9x+12 > x-2$

$8x > -14$

$x > -\frac{7}{4}$

The solution set is $\left\{x \mid x > -\frac{7}{4}\right\}$ or $\left(-\frac{7}{4}, \infty\right)$.



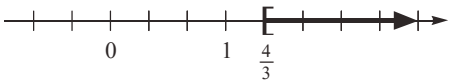
73. $\frac{x}{2} \ge 1-\frac{x}{4}$

$2x \ge 4-x$

$3x \ge 4$

$x \ge \frac{4}{3}$

The solution set is $\left\{x \mid x \ge \frac{4}{3}\right\}$ or $\left[\frac{4}{3}, \infty\right)$.

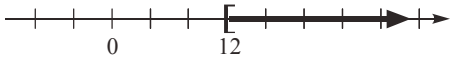


74. $\frac{x}{3} \ge 2+\frac{x}{6}$

$2x \ge 12+x$

$x \ge 12$

The solution set is $\{x \mid x \ge 12\}$ or $[12, \infty)$.



75. $0 < 3x-7 \le 5$

$7 < 3x \le 12$

$\frac{7}{3} < x \le 4$

The solution set is $\left\{x \mid \frac{7}{3} < x \le 4\right\}$ or $\left(\frac{7}{3}, 4\right]$.

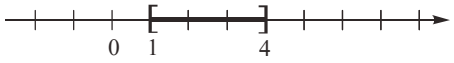


76. $4 \le 2x+2 \le 10$

$2 \le 2x \le 8$

$1 \le x \le 4$

The solution set is $\{x \mid 1 \le x \le 4\}$ or $[1, 4]$.

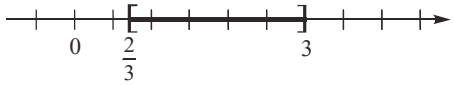


77. $-5 \le 4-3x \le 2$

$-9 \le -3x \le -2$

$3 \ge x \ge \frac{2}{3}$

The solution set is $\left\{x \mid \frac{2}{3} \le x \le 3\right\}$ or $\left[\frac{2}{3}, 3\right]$.



78. $-3 \le 3-2x \le 9$

$-6 \le -2x \le 6$

$3 \ge x \ge -3$

The solution set is $\{x \mid -3 \le x \le 3\}$ or $[-3, 3]$.



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79. $-3 < \dfrac{2x-1}{4} < 0$

$-12 < 2x - 1 < 0$

$-11 < 2x < 1$

$-\dfrac{11}{2} < x < \dfrac{1}{2}$

The solution set is $\left\{x \middle| -\dfrac{11}{2} < x < \dfrac{1}{2}\right\}$ or $\left(-\dfrac{11}{2}, \dfrac{1}{2}\right)$.



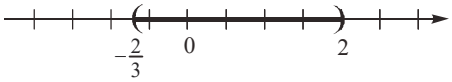
80. $0 < \dfrac{3x+2}{2} < 4$

$0 < 3x + 2 < 8$

$-2 < 3x < 6$

$-\dfrac{2}{3} < x < 2$

The solution set is $\left\{x \middle| -\dfrac{2}{3} < x < 2\right\}$ or $\left(-\dfrac{2}{3}, 2\right)$.



81. $1 < 1 - \dfrac{1}{2}x < 4$

$0 < -\dfrac{1}{2}x < 3$

$0 > x > -6$ or $-6 < x < 0$

The solution set is $\{x \mid -6 < x < 0\}$ or $(-6, 0)$.



82. $0 < 1 - \dfrac{1}{3}x < 1$

$-1 < -\dfrac{1}{3}x < 0$

$3 > x > 0$ or $0 < x < 3$

The solution set is $\{x \mid 0 < x < 3\}$ or $(0, 3)$.



83. $(x+2)(x-3) > (x-1)(x+1)$

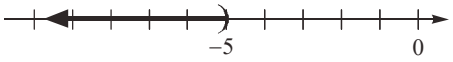
$x^2 - x - 6 > x^2 - 1$

$-x - 6 > -1$

$-x > 5$

$x < -5$

The solution set is $\{x \mid x < -5\}$ or $(-\infty, -5)$.



84. $(x-1)(x+1) > (x-3)(x+4)$

$x^2 - 1 > x^2 + x - 12$

$-1 > x - 12$

$-x > -11$

$x < 11$

The solution set is $\{x \mid x < 11\}$ or $(-\infty, 11)$.



85. $x(4x+3) \le (2x+1)^2$

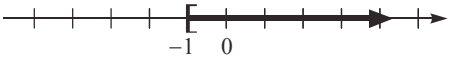
$4x^2 + 3x \le 4x^2 + 4x + 1$

$3x \le 4x + 1$

$-x \le 1$

$x \ge -1$

The solution set is $\{x \mid x \ge -1\}$ or $[-1, \infty)$.



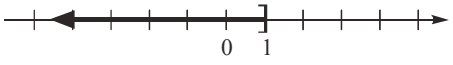
86. $x(9x-5) \le (3x-1)^2$

$9x^2 - 5x \le 9x^2 - 6x + 1$

$-5x \le -6x + 1$

$x \le 1$

The solution set is $\{x \mid x \le 1\}$ or $(-\infty, 1]$.



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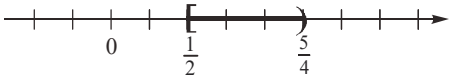
87. $\frac{1}{2} \le \frac{x+1}{3} < \frac{3}{4}$

$6 \le 4x+4 < 9$

$2 \le 4x < 5$

$\frac{1}{2} \le x < \frac{5}{4}$

The solution set is $\left\{x \middle| \frac{1}{2} \le x < \frac{5}{4}\right\}$ or $\left[\frac{1}{2}, \frac{5}{4}\right)$.



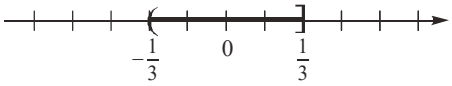
88. $\frac{1}{3} < \frac{x+1}{2} \le \frac{2}{3}$

$2 < 3x+3 \le 4$

$-1 < 3x \le 1$

$-\frac{1}{3} < x \le \frac{1}{3}$

The solution set is $\left\{x \middle| -\frac{1}{3} < x \le \frac{1}{3}\right\}$ or $\left(-\frac{1}{3}, \frac{1}{3}\right]$.



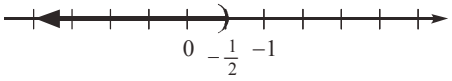
89. $(4x+2)^{-1} < 0$

$\frac{1}{4x+2} < 0$

$4x+2 < 0$

$x < -\frac{1}{2}$

The solution set is $\left\{x \middle| x < -\frac{1}{2}\right\}$ or $\left(-\infty, -\frac{1}{2}\right)$.



90. $(2x-1)^{-1} > 0$

$\frac{1}{2x-1} > 0$

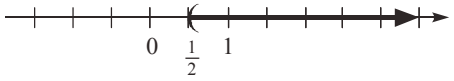
Since $\frac{1}{2x-1} > 0$, this means $2x-1 > 0$.

Therefore,

$2x-1 > 0$

$x > \frac{1}{2}$

The solution set is $\left\{x \middle| x > \frac{1}{2}\right\}$ or $\left(\frac{1}{2}, \infty\right)$.



91. $(1-4x)^{-1} \ge 7$

$\frac{1}{1-4x} - 7 \ge 0$

$\frac{1-7(1-4x)}{1-4x} \ge 0$

$\frac{-6+28x}{1-4x} \ge 0$

The zeros and values where the expression is undefined are $x = \frac{3}{14}$ and $x = \frac{1}{4}$

Interval	$(-\infty, \frac{3}{14})$	$(\frac{3}{14}, \frac{1}{4})$	$(\frac{1}{4}, \infty)$
Number Chosen	0	$\frac{22}{100}$	1
Value of f	-6	$\frac{4}{3}$	$-\frac{22}{3}$
Conclusion	*Negative*	*Positive*	*Negative*

We want to know where $f(x) \ge 0$, so the solution set is $\left\{x \middle| x \ge \frac{3}{14} \text{ or } x < \frac{1}{4}\right\}$ or, using interval notation, $[\frac{3}{14}, \frac{1}{4})$. Note that $\frac{1}{4}$ is not in the solution set because $\frac{1}{4}$ is not in the domain of f.

The solution set is $\left[\frac{3}{14}, \frac{1}{4}\right)$.



92. $2(3x+5)^{-1} \le -3$

$\frac{2}{(3x+5)} + 3 \le 0$

$\frac{2+3(3x+5)}{2(3x+5)} \le 0$

$\frac{17+9x}{(3x+5)} \le 0$

The zeros and values where the expression is undefined are $x = -\frac{17}{9}$ and $x = -\frac{5}{3}$

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Interval	$(-\infty, -\frac{17}{9})$	$(-\frac{17}{9}, -\frac{5}{3})$	$(-\frac{5}{3}, \infty)$
Number Chosen	-2	-1.7	0
Value of f	1	-17	$\frac{17}{5}$
Conclusion	*Positive*	*Negative*	*Positive*

We want to know where $f(x) \le 0$, so the solution set is $\left\{ x \middle| \, x \ge -\frac{17}{9} \text{ or } x < -\frac{5}{3} \right\}$ or, using interval notation, $[-\frac{17}{9}, -\frac{5}{3})$. Note that $-\frac{5}{3}$ is not in the solution set because $\frac{2}{7}$ is not in the domain of f.

The solution set is $\left[-\frac{17}{9}, -\frac{5}{3}\right)$.



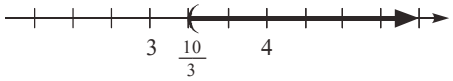
93. $0 < \frac{2}{x} < \frac{3}{5}$

$0 < \frac{2}{x}$ and $\frac{2}{x} < \frac{3}{5}$

Since $\frac{2}{x} > 0$, this means that $x > 0$. Therefore,

$$\frac{2}{x} < \frac{3}{5}$$
$$5x\left(\frac{2}{x}\right) < 5x\left(\frac{3}{5}\right)$$
$$10 < 3x$$
$$\frac{10}{3} < x$$

The solution set is $\left\{ x \middle| \, x > \frac{10}{3} \right\}$ or $\left(\frac{10}{3}, \infty\right)$.



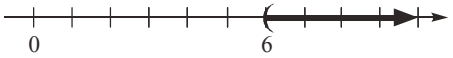
94. $0 < \frac{4}{x} < \frac{2}{3}$

$0 < \frac{4}{x}$ and $\frac{4}{x} < \frac{2}{3}$

Since $\frac{4}{x} > 0$, this means that $x > 0$. Therefore,

$$\frac{4}{x} < \frac{2}{3}$$
$$3x\left(\frac{4}{x}\right) < 3x\left(\frac{2}{3}\right)$$
$$12 < 2x$$
$$6 < x$$

The solution set is $\left\{ x \middle| \, x > 6 \right\}$ or $(6, \infty)$.



95. $0 < (2x-4)^{-1} < \frac{1}{2}$

$$0 < \frac{1}{2x-4} < \frac{1}{2}$$

$0 < \frac{1}{2x-4}$ and $\frac{1}{2x-4} < \frac{1}{2}$

Since $\frac{1}{2x-4} > 0$, this means that $2x-4 > 0$.

Therefore,

$$\frac{1}{2x-4} < \frac{1}{2}$$
$$\frac{1}{2(x-2)} < \frac{1}{2}$$
$$2(x-2)\left(\frac{1}{2(x-2)}\right) < 2(x-2)\left(\frac{1}{2}\right)$$
$$1 < x-2$$
$$3 < x$$

The solution set is $\left\{ x \middle| \, x > 3 \right\}$ or $(3, \infty)$.



96. $0 < (3x+6)^{-1} < \frac{1}{3}$

$$0 < \frac{1}{3x+6} < \frac{1}{3}$$

$0 < \frac{1}{3x+6}$ and $\frac{1}{3x+6} < \frac{1}{3}$

Since $\frac{1}{3x+6} > 0$, this means that $3x+6 > 0$.

Therefore,

$$\frac{1}{3x+6} < \frac{1}{3}$$
$$\frac{1}{3(x+2)} < \frac{1}{3}$$
$$3(x+2)\left(\frac{1}{3(x+2)}\right) < 3(x+2)\left(\frac{1}{3}\right)$$
$$1 < x+2$$
$$-1 < x$$

The solution set is $\left\{ x \middle| \, x > -1 \right\}$ or $(-1, \infty)$.



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97. If $-1 < x < 1$, then
$-1+4 < x+4 < 1+4$
$3 < x+4 < 5$
So, $a = 3$ and $b = 5$.

98. If $-3 < x < 2$, then
$-3-6 < x-6 < 2-6$
$-9 < x-6 < -4$
So, $a = -9$ and $b = -4$.

99. If $2 < x < 3$, then
$-4(2) < -4(x) < -4(3)$
$-12 < -4x < -8$
So, $a = -12$ and $b = -8$.

100. If $-4 < x < 0$, then
$\frac{1}{2}(-4) < \frac{1}{2}(x) < \frac{1}{2}(0)$
$-2 < \frac{1}{2}x < 0$
So, $a = -2$ and $b = 0$.

101. If $0 < x < 4$, then
$2(0) < 2(x) < 2(4)$
$0 < 2x < 8$
$0+3 < 2x+3 < 8+3$
$3 < 2x+3 < 11$
So, $a = 3$ and $b = 11$.

102. If $-3 < x < 3$, then
$-2(-3) > -2(x) > -2(3)$
$6 > -2x > -6$
$6+1 > -2x+1 > -6+1$
$7 > 1-2x > -5$
$-5 < 1-2x < 7$
So, $a = -5$ and $b = 7$.

103. If $-3 < x < 0$, then
$-3+4 < x+4 < 0+4$
$1 < x+4 < 4$
$1 > \frac{1}{x+4} > \frac{1}{4}$
$\frac{1}{4} < \frac{1}{x+4} < 1$
So, $a = \frac{1}{4}$ and $b = 1$.

104. If $2 < x < 4$, then
$2-6 < x-6 < 4-6$
$-4 < x-6 < -2$
$-\frac{1}{4} > \frac{1}{x-6} > -\frac{1}{2}$
$-\frac{1}{2} < \frac{1}{x-6} < -\frac{1}{4}$
So, $a = -\frac{1}{2}$ and $b = -\frac{1}{4}$.

105. If $6 < 3x < 12$, then
$\frac{6}{3} < \frac{3x}{3} < \frac{12}{3}$
$2 < x < 4$
$2^2 < x^2 < 4^2$
$4 < x^2 < 16$
So, $a = 4$ and $b = 16$.

106. If $0 < 2x < 6$, then
$\frac{0}{2} < \frac{2x}{2} < \frac{6}{2}$
$0 < x < 3$
$0^2 < x^2 < 3^2$
$0 < x^2 < 9$
So, $a = 0$ and $b = 9$.

107. $\sqrt{3x+6}$
We need $3x+6 \geq 0$
$3x \geq -6$
$x \geq -2$
To the domain is $\{x | x \geq -2\}$ or $[-2, \infty)$.

108. $\sqrt{8+2x}$
We need $8+2x \geq 0$
$2x \geq -8$
$x \geq -4$
To the domain is $\{x | x \geq -4\}$ or $[-4, \infty)$.

109. 21 < young adult's age < 30

110. 40 ≤ middle-aged < 60

111. **a.** Let x = age at death.
$x - 30 \geq 52.2$
$x \geq 82.2$
Therefore, the average life expectancy for a 30-year-old male in 2018 will be greater than or equal to 82.2 years.

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b. Let x = age at death.
$x - 30 \ge 55.8$
$x \ge 85.8$
Therefore, the average life expectancy for a 30-year-old female in 2018 will be greater than or equal to 85.8 years.

c. By the given information, a female can expect to live $85.8 - 82.2 = 3.6$ years longer.

112. $V = 20T$
$80^\circ \le T \le 120^\circ$
$80^\circ \le \frac{V}{20} \le 120^\circ$
$1600 \le V \le 2400$
The volume ranges from 1600 to 2400 cubic centimeters, inclusive.

113. Let P represent the selling price and C represent the commission.
Calculating the commission:
$C = 45,000 + 0.25(P - 900,000)$
$= 45,000 + 0.25P - 225,000$
$= 0.25P - 180,000$
Calculate the commission range, given the price range:
$900,000 \le P \le 1,100,000$
$0.25(900,000) \le 0.25P \le 0.25(1,100,000)$
$225,000 \le 0.25P \le 275,000$
$225,000 - 180,000 \le 0.25P - 180,000 \le 275,000 - 180,000$
$45,000 \le C \le 95,000$
The agent's commission ranges from \$45,000 to \$95,000, inclusive.
$\frac{45,000}{900,000} = 0.05 = 5\%$ to $\frac{95,000}{1,100,000} = 0.086 = 8.6\%$, inclusive.
As a percent of selling price, the commission ranges from 5% to 8.6%, inclusive.

114. Let C represent the commission.
Calculate the commission range:
$25 + 0.4(200) \le C \le 25 + 0.4(3000)$
$105 \le C \le 1225$
The commissions are at least \$105 and at most \$1225.

115. Let W = weekly wages and T = tax withheld.
Calculating the withholding tax range, given the range of weekly wages:
$900 \le W \le 1100$
$900 - 815 \le W - 815 \le 1100 - 815$
$85 \le W - 815 \le 285$
$0.22(85) \le 0.22(W - 815) \le 0.22(285)$
$18.70 \le 0.22(W - 815) \le 62.7$
$18.70 + 85.62 \le 0.22(W - 815) + 85.62 \le 62.7 + 85.62$
$104.32 \le T \le 148.32$

The amount withheld varies from \$104.32 to \$148.32, inclusive.

116. Let x represent the length of time Sue should exercise on the seventh day.
$200 \le 40 + 45 + 0 + 50 + 25 + 35 + x \le 300$
$200 \le 195 + x \le 300$
$5 \le x \le 105$
Sue will stay within the ACSM guidelines by exercising from 5 to 105 minutes.

117. Let K represent the monthly usage in kilowatt-hours and let C represent the monthly customer bill.
Calculating the bill: $C = 0.1006K + 25$
Calculating the range of kilowatt-hours, given the range of bills:
$140.69 \le C \le 231.23$
$140.69 \le 25 + 0.1006W \le 231.23$
$115.69 \le 0.1006K \le 206.23$
$1150 \le K \le 2050$
The usage varies from 1150.00 kilowatt-hours to 2050.00 kilowatt-hours, inclusive.

118. Let W represent the amount of sewer/water used (in thousands of gallons). Let C represent the customer charge (in dollars).
Calculating the charge:
$C = 23.55 + 0.40W$
Calculating the range of water usage, given the range of charges:
$30.35 \le C \le 36.75$
$30.35 \le 23.55 + 0.40W \le 36.75$
$6.8 \le 0.40K \le 13.2$
$17 \le K \le 33$
The range of water usage ranged from 17,000 to 33,000 gallons.

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119. You have already consumed 22 grams of fat. Let C represent the number of cookies. Then we have the following equation:

$$22 + 5C \le 47$$
$$5C \le 25$$
$$C \le 5$$

You may eat up to 5 cookies and keep the total fat content of your meal not more than 47g.

120. You have already consumed 145 grams of sodium. Let H represent the number of hamburgers. Then we have the following equation:

$$145 + 380H \le 1285$$
$$380C \le 1140$$
$$C \le 3$$

You may eat up to 3 hamburgers and keep the total sodium content of your meal not more than 1285g.

121. a. Let T represent the score on the last test and G represent the course grade.
Calculating the course grade and solving for the last test:

$$G = \frac{68 + 82 + 87 + 89 + T}{5}$$
$$G = \frac{326 + T}{5}$$
$$5G = 326 + T$$
$$T = 5G - 326$$

Calculating the range of scores on the last test, given the grade range:

$$80 \le G < 90$$
$$400 \le 5G < 450$$
$$74 \le 5G - 326 < 124$$
$$74 \le T < 124$$

To get a grade of B, you need at least a 74 on the fifth test.

b. Let T represent the score on the last test and G represent the course grade.
Calculating the course grade and solving for the last test:

$$G = \frac{68 + 82 + 87 + 89 + 2T}{6}$$
$$G = \frac{326 + 2T}{6}$$
$$G = \frac{163 + T}{3}$$
$$T = 3G - 163$$

Calculating the range of scores on the last test, given the grade range:

$$80 \le G < 90$$
$$240 \le 3G < 270$$
$$77 \le 3G - 163 < 107$$
$$77 \le T < 107$$

To get a grade of B, you need at least a 77 on the fifth test.

122. Let T represent the test scores of the people in the top 2.5%.

$$T > 1.96(12) + 100 = 123.52$$

People in the top 2.5% will have test scores greater than 123.52. That is, $T > 123.52$ or $(123.52, \infty)$.

123. Since $a < b$,

$$\frac{a}{2} < \frac{b}{2} \quad \text{and} \quad \frac{a}{2} < \frac{b}{2}$$
$$\frac{a}{2} + \frac{a}{2} < \frac{a}{2} + \frac{b}{2} \quad \text{and} \quad \frac{a}{2} + \frac{b}{2} < \frac{b}{2} + \frac{b}{2}$$
$$a < \frac{a+b}{2} \quad \text{and} \quad \frac{a+b}{2} < b$$

So, $a < \frac{a+b}{2} < b$.

124. From problem 123, $a < \frac{a+b}{2} < b$, so

$$d\left(a, \frac{a+b}{2}\right) = \frac{a+b}{2} - a = \frac{a+b-2a}{2} = \frac{b-a}{2} \quad \text{and}$$
$$d\left(b, \frac{a+b}{2}\right) = b - \frac{a+b}{2} = \frac{2b-a-b}{2} = \frac{b-a}{2}.$$

Therefore, $\frac{a+b}{2}$ is equidistant from a and b.

125. If $0 < a < b$, then

$$ab > a^2 > 0 \quad \text{and} \quad b^2 > ab > 0$$
$$\left(\sqrt{ab}\right)^2 > a^2 \quad \text{and} \quad b^2 > \left(\sqrt{ab}\right)^2$$
$$\sqrt{ab} > a \quad \text{and} \quad b > \sqrt{ab}$$

Therefore, $a < \sqrt{ab} < b$.

126. Show that $\sqrt{ab} < \frac{a+b}{2}$.

$$\frac{a+b}{2} - \sqrt{ab} = \frac{1}{2}\left(a - 2\sqrt{ab} + b\right)$$
$$= \frac{1}{2}\left(\sqrt{a} - \sqrt{b}\right)^2 > 0, \text{ since } a \ne b.$$

Therefore, $\sqrt{ab} < \frac{a+b}{2}$.

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127. For $0 < a < b$, $\dfrac{1}{h} = \dfrac{1}{2}\left(\dfrac{1}{a} + \dfrac{1}{b}\right)$

$$h \cdot \frac{1}{h} = \frac{1}{2}\left(\frac{b+a}{ab}\right) \cdot h$$

$$1 = \frac{1}{2}\left(\frac{b+a}{ab}\right) \cdot h$$

$$h = \frac{2ab}{a+b}$$

$$h - a = \frac{2ab}{a+b} - a = \frac{2ab - a(a+b)}{a+b}$$

$$= \frac{2ab - a^2 - ab}{a+b} = \frac{ab - a^2}{a+b}$$

$$= \frac{a(b-a)}{a+b} > 0$$

Therefore, $h > a$.

$$b - h = b - \frac{2ab}{a+b} = \frac{b(a+b) - 2ab}{a+b}$$

$$= \frac{ab + b^2 - 2ab}{a+b} = \frac{b^2 - ab}{a+b}$$

$$= \frac{b(b-a)}{a+b} > 0$$

Therefore, $h < b$, and we have $a < h < b$.

128. Show that $h = \dfrac{(\text{geometric mean})^2}{\text{arithmetic mean}} = \dfrac{\left(\sqrt{ab}\right)^2}{\left(\frac{1}{2}(a+b)\right)}$

$$\frac{1}{h} = \frac{1}{2}\left(\frac{1}{a} + \frac{1}{b}\right)$$

$$\frac{2}{h} = \frac{1}{a} + \frac{1}{b} = \frac{b+a}{ab}$$

$$\frac{h}{2} = \frac{ab}{a+b}$$

$$h = 2 \cdot \frac{ab}{a+b} = \frac{\left(\sqrt{ab}\right)^2}{\left(\frac{1}{2}(a+b)\right)}$$

129. $x - 4 < 2x - 3 \le \dfrac{x+5}{3}$

$$3x - 12 < 6x - 9 \le x + 5$$

$3x - 12 < 6x - 9$ and $6x - 9 \le x + 5$

$-3 < 3x$ $\qquad$ $5x \le 14$

$-1 < x$ $\qquad$ $x \le \dfrac{14}{4}$

This is equivalent to $-1 < x \le \dfrac{14}{5}$. The solution set, in interval notation, is $\left(-1, \dfrac{14}{5}\right]$.

130. The largest value of $2x^2 - 3$ occurs at the largest value for $|x|$.

$2 \le 5 - x \le 9$

$-3 \le -x \le 4$

$-4 \le x \le 3$

$3 \ge x \ge -4$ or $-4 \le x \le 3$

The largest value for $2x^2 - 3$ is

$2(-4)^2 - 3 = 32 - 3 = 29$.

131. Answers will vary

132. Answers will vary. One possibility:

No solution: $4x + 6 \le 2(x - 5) + 2x$

One solution: $3x + 5 \le 2(x + 3) + 1 \le 3(x + 2) - 1$

133. Since $x^2 \ge 0$, we have

$x^2 + 1 \ge 0 + 1$

$x^2 + 1 \ge 1$

Therefore, the expression $x^2 + 1$ can never be less than -5.

134. Answers will vary.

Section 1.6

1. $|-2| = 2$
2. True
3. $\{-5, 5\}$
4. $\{x \mid -5 < x < 5\}$
5. True
6. True
7. d
8. a

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9. $|3x| = 15$

$3x = 15$ or $3x = -15$

$x = 5$ or $x = -5$

The solution set is $\{-5, 5\}$.

10. $|3x| = 12$

$3x = 12$ or $3x = -12$

$x = 4$ or $x = -4$

The solution set is $\{-4, 4\}$.

11. $|2x + 3| = 5$

$2x + 3 = 5$ or $2x + 3 = -5$

$2x = 2$ or $2x = -8$

$x = 1$ or $x = -4$

The solution set is $\{-4, 1\}$.

12. $|3x - 1| = 2$

$3x - 1 = 2$ or $3x - 1 = -2$

$3x = 3$ or $3x = -1$

$x = 1$ or $x = -\frac{1}{3}$

The solution set is $\left\{-\frac{1}{3}, 1\right\}$.

13. $|1 - 4t| + 8 = 13$

$|1 - 4t| = 5$

$1 - 4t = 5$ or $1 - 4t = -5$

$-4t = 4$ or $-4t = -6$

$t = -1$ or $t = \frac{3}{2}$

The solution set is $\left\{-1, \frac{3}{2}\right\}$.

14. $|1 - 2z| + 6 = 9$

$|1 - 2z| = 3$

$1 - 2z = 3$ or $1 - 2z = -3$

$-2z = 2$ or $-2z = -4$

$z = -1$ or $z = 2$

The solution set is $\{-1, 2\}$.

15. $|-2x| = |8|$

$|-2x| = 8$

$-2x = 8$ or $-2x = -8$

$x = -4$ or $x = 4$

The solution set is $\{-4, 4\}$.

16. $|-x| = |1|$

$|-x| = 1$

$-x = 1$ or $-x = -1$

The solution set is $\{-1, 1\}$.

17. $|-2|x = 4$

$2x = 4$

$x = 2$

The solution set is $\{2\}$.

18. $|3|x = 9$

$3x = 9$

$x = 3$

The solution set is $\{3\}$.

19. $\frac{8}{7}|x| = 3$

$|x| = \frac{21}{8}$

$x = \frac{21}{8}$ or $x = -\frac{21}{8}$

The solution set is $\left\{-\frac{21}{8}, \frac{21}{8}\right\}$.

20. $\frac{3}{4}|x| = 9$

$|x| = 12$

$x = 12$ or $x = -12$

The solution set is $\{-12, 12\}$.

21. $\left|\frac{x}{3} + \frac{2}{5}\right| = 2$

$\frac{x}{3} + \frac{2}{5} = 2$ or $\frac{x}{3} + \frac{2}{5} = -2$

$5x + 6 = 30$ or $5x + 6 = -30$

$5x = 24$ or $5x = -36$

$x = \frac{24}{5}$ or $x = -\frac{36}{5}$

The solution set is $\left\{-\frac{36}{5}, \frac{24}{5}\right\}$.

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22. $\left|\frac{x}{2}-\frac{1}{3}\right|=1$

$\frac{x}{2}-\frac{1}{3}=1 \quad \text{or} \quad \frac{x}{2}-\frac{1}{3}=-1$

$3x-2=6 \quad \text{or} \quad 3x-2=-6$

$3x=8 \quad \text{or} \quad 3x=-4$

$x=\frac{8}{3} \quad \text{or} \quad x=-\frac{4}{3}$

The solution set is $\left\{-\frac{4}{3}, \frac{8}{3}\right\}$.

23. $|u-2|=-\frac{1}{2}$

No solution, since absolute value always yields a non-negative number.

24. $|2-v|=-1$

No solution, since absolute value always yields a non-negative number.

25. $5-|4x|=4$

$-|4x|=-1$

$|4x|=1$

$4x=1 \text{ or } 4x=-1$

$x=\frac{1}{4} \text{ or } x=-\frac{1}{4}$

The solution set is $\left\{-\frac{1}{4}, \frac{1}{4}\right\}$.

26. $5-\left|\frac{1}{2}x\right|=3$

$-\left|\frac{1}{2}x\right|=-2$

$\left|\frac{1}{2}x\right|=2$

$\frac{1}{2}x=2 \text{ or } \frac{1}{2}x=-2$

$x=4 \quad \text{or} \quad x=-4$

The solution set is $\{-4,4\}$.

27. $|x^2-9|=0$

$x^2-9=0$

$x^2=9$

$x=\pm 3$

The solution set is $\{-3,3\}$.

28. $|x^2-16|=0$

$x^2-16=0$

$x^2=16$

$x=\pm 4$

The solution set is $\{-4,4\}$.

29. $|x^2-2x|=3$

$x^2-2x=3 \quad \text{or} \quad x^2-2x=-3$

$x^2-2x-3=0 \quad \text{or} \quad x^2-2x+3=0$

$(x-3)(x+1)=0 \text{ or } x=\frac{2\pm\sqrt{4-12}}{2}$

$x=3 \text{ or } x=-1 \text{ or } x=\frac{2\pm\sqrt{-8}}{2}$ no real sol.

The solution set is $\{-1,3\}$.

30. $|x^2+x|=12$

$x^2+x=12 \quad \text{or} \quad x^2+x=-12$

$x^2+x-12=0 \quad \text{or} \quad x^2+x+12=0$

$(x-3)(x+4)=0 \text{ or } x=\frac{-1\pm\sqrt{1-48}}{2}$

$x=3 \text{ or } x=-4 \text{ or } x=\frac{1\pm\sqrt{-47}}{2}$ no real sol.

The solution set is $\{-4,3\}$.

31. $|x^2+x-1|=1$

$x^2+x-1=1 \quad \text{or} \quad x^2+x-1=-1$

$x^2+x-2=0 \quad \text{or} \quad x^2+x=0$

$(x-1)(x+2)=0 \quad \text{or} \quad x(x+1)=0$

$x=1, x=-2 \quad \text{or} \quad x=0, x=-1$

The solution set is $\{-2,-1,0,1\}$.

32. $|x^2+3x-2|=2$

$x^2+3x-2=2 \quad \text{or} \quad x^2+3x-2=-2$

$x^2+3x=4 \quad \text{or} \quad x^2+3x=0$

$x^2+3x-4=0 \text{ or } x(x+3)=0$

$(x+4)(x-1)=0 \quad \text{or} \quad x=0, x=-3$

$x=-4, x=1$

The solution set is $\{-4,-3,0,1\}$.

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33. $\left|\dfrac{5x-3}{3x-5}\right| = 2$

$\dfrac{5x-3}{3x-5} = 2$ or $\dfrac{5x-3}{3x-5} = -2$

$5x-3 = 2(3x-5)$ or $5x-3 = -2(3x-5)$

$5x-3 = 6x-10$ or $5x-3 = -6x+10$

$-x = -7$ or $11x = 13$

$x = 7$ or $x = \dfrac{13}{11}$

Neither of these values cause the denominator to equal zero, so the solution set is $\left\{\dfrac{13}{11}, 7\right\}$.

34. $\left|\dfrac{2x+1}{3x+4}\right| = 1$

$\dfrac{2x+1}{3x+4} = 1$ or $\dfrac{2x+1}{3x+4} = -1$

$2x+1 = 1(3x+4)$ or $2x+1 = -1(3x+4)$

$2x+1 = 3x+4$ or $2x+1 = -3x-4$

$-x = 3$ or $5x = -5$

$x = -3$ or $x = -1$

Neither of these values cause the denominator to equal zero, so the solution set is $\{-3,-1\}$.

35. $\left|x^2+3x\right| = \left|x^2-2x\right|$

$x^2+3x = x^2-2x$ or $x^2+3x = -\left(x^2-2x\right)$

$3x = -2x$ or $x^2+3x = -x^2+2x$

$5x = 0$ or $2x^2+x = 0$

$x = 0$ or $x(2x+1) = 0$

$x = 0$ or $x = 0$ or $x = -\dfrac{1}{2}$

The solution set is $\left\{-\dfrac{1}{2}, 0\right\}$.

36. $\left|x^2-2x\right| = \left|x^2+6x\right|$

$x^2-2x = x^2+6x$ or $x^2-2x = -\left(x^2+6x\right)$

$-2x = 6x$ or $x^2-2x = -x^2-6x$

$-8x = 0$ or $2x^2+4x = 0$

$x = 0$ or $2x(x+2) = 0$

$x = 0$ or $x = 0$ or $x = -2$

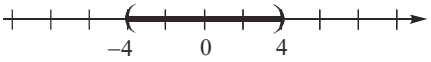
The solution set is $\{-2, 0\}$.

37. $|2x| < 8$

$-8 < 2x < 8$

$-4 < x < 4$

$\{x \mid -4 < x < 4\}$ or $(-4,4)$

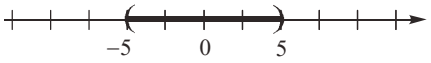


38. $|3x| < 15$

$-15 < 3x < 15$

$-5 < x < 5$

$\{x \mid -5 < x < 5\}$ or $(-5,5)$

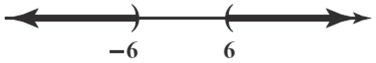


39. $|7x| > 42$

$7x < -42$ or $7x > 42$

$x < -6$ or $x > 6$

$\{x \mid x < -6 \text{ or } x > 6\}$ or $(-\infty,-6) \cup (6,\infty)$

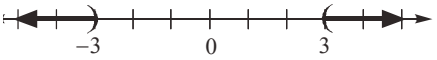


40. $|2x| > 6$

$2x < -6$ or $2x > 6$

$x < -3$ or $x > 3$

$\{x \mid x < -3 \text{ or } x > 3\}$ or $(-\infty,-3) \cup (3,\infty)$



41. $|x-2|+2 < 3$

$|x-2| < 1$

$-1 < x-2 < 1$

$1 < x < 3$

$\{x \mid 1 < x < 3\}$ or $(1,3)$



42. $|x+4|+3 < 5$

$|x+4| < 2$

$-2 < x+4 < 2$

$-6 < x < -2$

$\{x \mid -6 < x < -2\}$ or $(-6,-2)$



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43. $|3t-2| \le 4$

$-4 \le 3t-2 \le 4$

$-2 \le 3t \le 6$

$-\frac{2}{3} \le t \le 2$

$\left\{t \middle| -\frac{2}{3} \le t \le 2\right\}$ or $\left[-\frac{2}{3}, 2\right]$



44. $|2u+5| \le 7$

$-7 \le 2u+5 \le 7$

$-12 \le 2u \le 2$

$-6 \le u \le 1$

$\{u|-6 \le u \le 1\}$ or $[-6, 1]$



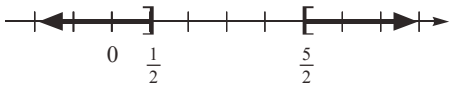
44. $|2x-3| \ge 2$

$2x-3 \le -2$ or $2x-3 \ge 2$

$2x \le 1$ or $2x \ge 5$

$x \le \frac{1}{2}$ or $x \ge \frac{5}{2}$

$\left\{x \middle| x \le \frac{1}{2} \text{ or } x \ge \frac{5}{2}\right\}$ or $\left(-\infty, \frac{1}{2}\right] \cup \left[\frac{5}{2}, \infty\right)$



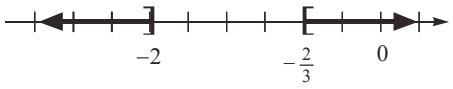
46. $|3x+4| \ge 2$

$3x+4 \le -2$ or $3x+4 \ge 2$

$3x \le -6$ or $3x \ge -2$

$x \le -2$ or $x \ge -\frac{2}{3}$

$\left\{x \middle| x \le -2 \text{ or } x \ge -\frac{2}{3}\right\}$ or $(-\infty, -2] \cup \left[-\frac{2}{3}, \infty\right)$



47. $|1-4x|-7 < -2$

$|1-4x| < 5$

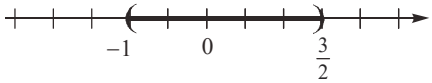
$-5 < 1-4x < 5$

$-6 < -4x < 4$

$\frac{-6}{-4} > x > \frac{4}{-4}$

$\frac{3}{2} > x > -1$ or $-1 < x < \frac{3}{2}$

$\left\{x \middle| -1 < x < \frac{3}{2}\right\}$ or $\left(-1, \frac{3}{2}\right)$



48. $|1-2x|-4 < -1$

$|1-2x| < 3$

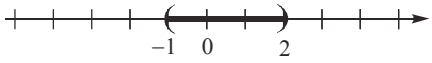
$-3 < 1-2x < 3$

$-4 < -2x < 2$

$\frac{-4}{-2} > x > \frac{2}{-2}$

$2 > x > -1$ or $-1 < x < 2$

$\{x|-1 < x < 2\}$ or $(-1,2)$



49. $|5-2x| > -7$

$5-2x < -7$ or $5-2x > 7$

$-2x < -12$ or $-2x > 2$

$x > 6$ or $x < -1$

$\{x|x < -1 \text{ or } x > 6\}$ or $(-\infty, -1) \cup (6, \infty)$



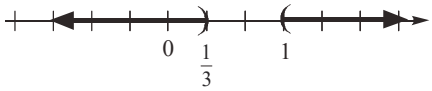
50. $|2-3x| > 1$

$2-3x < -1$ or $2-3x > 1$

$-3x < -3$ or $-3x > -1$

$x > 1$ or $x < \frac{1}{3}$

$\left\{x \middle| x < \frac{1}{3} \text{ or } x > 1\right\}$ or $\left(-\infty, \frac{1}{3}\right) \cup (1, \infty)$



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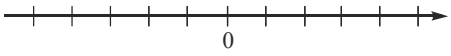
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51. $|-4x|+|-5|\le 1$

$|-4x|+5\le 1$

$|-4x|\le -4$

This is impossible since absolute value always yields a non-negative number. The inequality has no solution.



52. $|-x|-|4|\le 2$

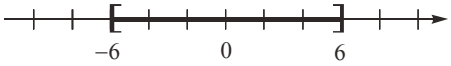
$|-x|-4\le 2$

$|-x|\le 6$

$-6\le -x\le 6$

$6\ge x\ge -6$

$\{x\,|\,-6\le x\le 6\}$ or $[-6,6]$



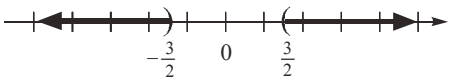
53. $|-2x|>|-3|$

$|2x|>3$

$2x<-3$ or $2x>3$

$x<-\frac{3}{2}$ or $x>\frac{3}{2}$

$\left\{x\,\middle|\,x<-\frac{3}{2}\text{ or }x>\frac{3}{2}\right\}$ or $\left(-\infty,-\frac{3}{2}\right)\cup\left(\frac{3}{2},\infty\right)$



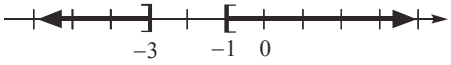
54. $|-x-2|\ge 1$

$-x-2\le -1$ or $-x-2\ge 1$

$-x\le 1$ or $-x\ge 3$

$x\ge -1$ or $x\le -3$

$\{x\,|\,x\le -3\text{ or }x\ge -1\}$ or $(-\infty,-3]\cup[-1,\infty)$



55. $-3|2x-5|\ge -21$

$|2x-5|\le 7$

$-7\le 2x-5\le 7$

$-2\le 2x\le 12$

$-1\le x\le 6$

$\{x\,|\,-1\le x\le 6\}$ or $[-1,6]$



56. $-|1-2x|\ge -3$

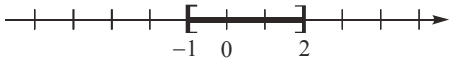
$|1-2x|\le 3$

$-3\le 1-2x\le 3$

$-4\le -2x\le 2$

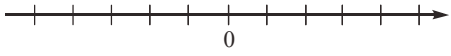
$2\ge x\ge -1$

$\{x\,|\,-1\le x\le 2\}$ or $[-1,2]$



57. $|9x|<-5$

This is impossible since absolute value always yields a non-negative number. No solution.



58. $|3x|\ge 0$

Absolute value yields a non-negative number, so this inequality is true for all real numbers, $(-\infty,\infty)$.



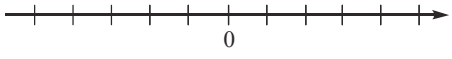
59. $|5x|\ge -1$

Absolute value yields a non-negative number, so this inequality is true for all real numbers, $(-\infty,\infty)$.



60. $|6x|<-2$

This is impossible since absolute value always yields a non-negative number. No solution.



61. $\left|\frac{2x+3}{3}-\frac{1}{2}\right|<1$

$-1<\frac{2x+3}{3}-\frac{1}{2}<1$

$6(-1)<6\left(\frac{2x+3}{3}-\frac{1}{2}\right)<6(1)$

$-6<2(2x+3)-3<6$

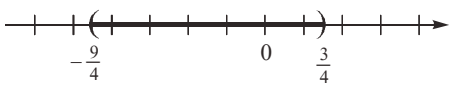
$-6<4x+6-3<6$

$-6<4x+3<6$

$-9<4x<3$

$-\frac{9}{4}<x<\frac{3}{4}$

$\left\{x\,\middle|\,-\frac{9}{4}<x<\frac{3}{4}\right\}$ or $\left(-\frac{9}{4},\frac{3}{4}\right)$



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62. $3-|x+1|<\frac{1}{2}$

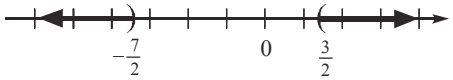
$-|x+1|<-\frac{5}{2}$

$|x+1|>\frac{5}{2}$

$x+1<-\frac{5}{2}$ or $x+1>\frac{5}{2}$

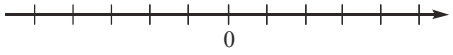
$x<-\frac{7}{2}$ or $x>\frac{3}{2}$

$\left\{x\middle|x<-\frac{7}{2} \text{ or } x>\frac{3}{2}\right\}$ or $\left(-\infty,-\frac{7}{2}\right)\cup\left(\frac{3}{2},\infty\right)$



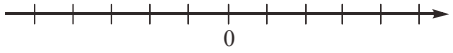
63. $|8-4x|\le -13$

This is impossible since absolute value always yields a non-negative number. No solution.



64. $|7x+4|\le -9$

This is impossible since absolute value always yields a non-negative number. No solution.



65. $\left|\frac{7-2x}{3}\right|\le 0$

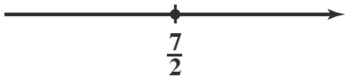
Since the absolute value cannot be negative, the only possible solution would be:

$\frac{7-2x}{3}=0$

$7-2x=0$

$-2x=-7$

$x=\frac{7}{2}$



66. $-\left|\frac{4x-15}{6}\right|\ge 0$

$\left|\frac{4x-15}{6}\right|\le 0$

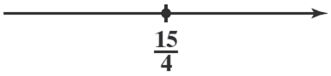
Since the absolute value cannot be negative, the only possible solution would be:

$\frac{4x-15}{6}=0$

$4x-15=0$

$4x=15$

$x=\frac{15}{4}$



67. $\left|\frac{3x-7}{5}\right|>4$

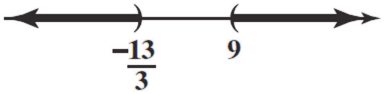
$\frac{3x-7}{5}<-4$ or $\frac{3x-7}{5}>4$

$3x-7<-20$ or $3x-7>20$

$3x<13$ or $3x>27$

$x<\frac{13}{3}$ or $x>9$

$\left\{x\middle|x<\frac{13}{3} \text{ or } x>9\right\}$ or $\left(-\infty,\frac{13}{3}\right)\cup(9,\infty)$



68. $\left|\frac{5-2x}{9}\right|\ge 8$

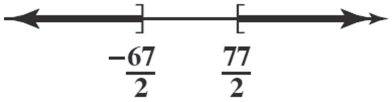
$\frac{5-2x}{9}\le -8$ or $\frac{5-2x}{9}\ge 8$

$5-2x\le -72$ or $5-2x\ge 72$

$-2x\le -77$ or $-2x\ge 67$

$x\ge\frac{77}{2}$ or $x\le -\frac{67}{2}$

$\left\{x\middle|x\le -\frac{67}{2} \text{ or } x\ge\frac{77}{2}\right\}$ or $\left(-\infty,-\frac{67}{2}\right)\cup\left(\frac{77}{2},\infty\right)$



69. $5+|x-1|>\frac{1}{2}$

$|x-1|>-\frac{9}{2}$

Absolute value yields a non-negative number, so this inequality is true for all real numbers, $(-\infty,\infty)$.

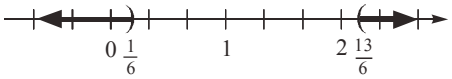


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70. $\left|\frac{2x-3}{2}+\frac{1}{3}\right|>1$

$$\frac{2x-3}{2}+\frac{1}{3}<-1 \quad \text{or} \quad \frac{2x-3}{2}+\frac{1}{3}>1$$
$$6\left(\frac{2x-3}{2}+\frac{1}{3}\right)<6(-1) \text{ or } 6\left(\frac{2x-3}{2}+\frac{1}{3}\right)>6(1)$$
$$3(2x-3)+2<-6 \quad \text{or} \quad 3(2x-3)+2>6$$
$$6x-9+2<-6 \quad \text{or} \quad 6x-9+2>6$$
$$6x-7<-6 \quad \text{or} \quad 6x-7>6$$
$$6x<1 \quad \text{or} \quad 6x>13$$
$$x<\frac{1}{6} \quad \text{or} \quad x>\frac{13}{6}$$
$$\left\{x\middle|x<\frac{1}{6} \text{ or } x>\frac{13}{6}\right\} \text{ or } \left(-\infty,\frac{1}{6}\right)\cup\left(\frac{13}{6},\infty\right)$$



71. A temperature x that differs from $98.6°$ F by at least $1.5°$F .

$$|x-98.6°|\geq 1.5°$$
$$x-98.6°\leq -1.5° \text{ or } x-98.6°\geq 1.5°$$
$$x\leq 97.1° \text{ or } x\geq 100.1°$$

The temperatures that are considered unhealthy are those that are less than 97.1˚F or greater than 100.1˚F, inclusive.

72. The length L must be within 0.0025 of 5.375 inches..

$$|L-5.375|\leq 0.0025$$
$$-0.0025\leq L-5.375\leq 0.0025$$
$$5.3725\leq L\leq 5.3775$$

The lengths must be between 5.3725 and 5.3775 inches, inclusive.

73. The percentage must be within 3.9 percentage points of 64 percent. The inequality that represents this would be:

$$|x-64|\leq 3.9$$
$$-3.9\leq x-64\leq 3.9$$
$$60.1\leq x\leq 67.9$$

The actual percentage is likely to fall between 60.1% and 67.9% inclusive.

74. The speed x varies from 707 mph by up to 55 mph.

a. $|x-707|\leq 55$

b.
$$-55\leq x-707\leq 55$$
$$-55\leq x-707\leq 55$$
$$652\leq x\leq 762$$

The speed of sound is between 652 and 762 miles per hour, depending on conditions.

75. x differs from 3 by less than $\frac{1}{2}$.

$$|x-3|<\frac{1}{2}$$
$$-\frac{1}{2}<x-3<\frac{1}{2}$$
$$\frac{5}{2}<x<\frac{7}{2}$$
$$\left\{x\middle|\frac{5}{2}<x<\frac{7}{2}\right\}$$

76. x differs from -4 by less than 1

$$|x-(-4)|<1$$
$$|x+4|<1$$
$$-1<x+4<1$$
$$-5<x<-3$$
$$\{x|-5<x<-3\}$$

77. x differs from -3 by more than 2.

$$|x-(-3)|>2$$
$$|x+3|>2$$
$$x+3<-2 \text{ or } x+3>2$$
$$x<-5 \text{ or } x>-1$$
$$\{x\,|\,x<-5 \text{ or } x>-1\}$$

78. x differs from 2 by more than 3.

$$|x-2|>3$$
$$x-2<-3 \text{ or } x-2>3$$
$$x<-1 \text{ or } x>5$$
$$\{x\,|\,x<-1 \text{ or } x>5\}$$

79. $|x-1|<3$

$$-3<x-1<3$$
$$-3+5<(x-1)+5<3+5$$
$$2<x+4<8$$
$$a=2,\ b=8$$

80. $|x+2|<5$

$$-5<x+2<5$$
$$-5-4<(x+2)-4<5-4$$
$$-9<x-2<1$$
$$a=-9,\ b=1$$

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81. $|x+4| \le 2$

$-2 \le x+4 \le 2$

$-6 \le x \le -2$

$-12 \le 2x \le -4$

$-15 \le 2x-3 \le -7$

$a=-15,\ b=-7$

82. $|x-3| \le 1$

$-1 \le x-3 \le 1$

$2 \le x \le 4$

$6 \le 3x \le 12$

$7 \le 3x+1 \le 13$

$a=7,\ b=13$

83. $|x-2| \le 7$

$-7 \le x-2 \le 7$

$-5 \le x \le 9$

$-15 \le x-10 \le -1$

$-\frac{1}{15} \ge \frac{1}{x-10} \ge -1$

$-1 \le \frac{1}{x-10} \le -\frac{1}{15}$

$a=-1,\ b=-\frac{1}{15}$

84. $|x+1| \le 3$

$-3 \le x+1 \le 3$

$-4 \le x \le 2$

$1 \le x+5 \le 7$

$1 \ge \frac{1}{x+5} \ge \frac{1}{7}$

$\frac{1}{7} \le \frac{1}{x+5} \le 1$

$a=\frac{1}{7},\ b=1$

85. Given that $a>0,\ b>0,$ and $\sqrt{a}<\sqrt{b}$, show that $a<b.$

Note that $b-a=\left(\sqrt{b}+\sqrt{a}\right)\left(\sqrt{b}-\sqrt{a}\right)$.

Since $\sqrt{a}<\sqrt{b}$ means $\sqrt{b}-\sqrt{a}>0$, we have $b-a=\left(\sqrt{b}+\sqrt{a}\right)\left(\sqrt{b}-\sqrt{a}\right)>0$.

Therefore, $b-a>0$ which means $a<b.$

86. Show that $a \le |a|$.

We know $0 \le |a|$. So if $a<0$, then we have $a<0 \le |a|$ which means $a \le |a|$.. Now, if $a \ge 0,$ then $|a|=a$. So $a \le |a|$.

87. Prove $|a+b| \le |a|+|b|$.

Note that $|a+b|^2=|a+b|\cdot|a+b|$.

Case 1: If $a+b \ge 0,$ then $|a+b|=a+b,$ so

$$\begin{aligned}|a+b|\cdot|a+b| &= (a+b)(a+b)\\ &= a^2+2ab+b^2\\ &\le |a|^2+2|a|\cdot|b|+|b|^2\\ &= \left(|a|+|b|\right)^2 \quad \text{by problem 86}\end{aligned}$$

Thus, $\left(|a+b|\right)^2 \le \left(|a|+|b|\right)^2$

$|a+b| \le |a|+|b|.$

Case 2: If $a+b<0,$ then $|a+b|=-(a+b),$ so

$$\begin{aligned}|a+b|\cdot|a+b| &= \left(-(a+b)\right)\left(-(a+b)\right)\\ &= (a+b)(a+b)\\ &= a^2+2ab+b^2\\ &\le |a|^2+2|a|\cdot|b|+|b|^2\\ &= \left(|a|+|b|\right)^2 \quad \text{by problem 86}\end{aligned}$$

Thus, $\left(|a+b|\right)^2 \le \left(|a|+|b|\right)^2$

$|a+b| \le |a|+|b|$

88. Prove $|a-b| \ge |a|-|b|$.

$|a|=|(a-b)+b| \le |a-b|+|b|$ by the Triangle Inequality, so $|a| \le |a-b|+|b|$ which means $|a|-|b| \le |a-b|$. Therefore, $|a-b| \ge |a|-|b|$.

89. Given that $a>0,$

$$x^2<a$$

$$x^2-a<0$$

$$\left(x+\sqrt{a}\right)\left(x-\sqrt{a}\right)<0$$

If $x<-\sqrt{a}$, then $x+\sqrt{a}<0$ and $x-\sqrt{a}<-2\sqrt{a}<0$. Therefore, $\left(x+\sqrt{a}\right)\left(x-\sqrt{a}\right)>0$, which is a contradiction.

If $-\sqrt{a}<x<\sqrt{a}$, then $0<x+\sqrt{a}<2\sqrt{a}$ and $-2\sqrt{a}<x-\sqrt{a}<0$.

Therefore, $\left(x+\sqrt{a}\right)\left(x-\sqrt{a}\right)<0$.

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If $x > \sqrt{a}$, then $x + \sqrt{a} > 2\sqrt{a} > 0$ and $x - \sqrt{a} > 0$. Therefore, $\left(x + \sqrt{a}\right)\left(x - \sqrt{a}\right) > 0$, which is a contradiction. So the solution set for $x^2 < a$ is $\left\{x \middle| -\sqrt{a} < x < \sqrt{a}\right\}$.

90. Given that $a > 0$,

$$x^2 > a$$
$$x^2 - a > 0$$
$$\left(x + \sqrt{a}\right)\left(x - \sqrt{a}\right) > 0$$

If $x < -\sqrt{a}$, then $x + \sqrt{a} < 0$ and $x - \sqrt{a} < -2\sqrt{a} < 0$.
Therefore, $\left(x + \sqrt{a}\right)\left(x - \sqrt{a}\right) > 0$.

If $-\sqrt{a} < x < \sqrt{a}$, then $0 < x + \sqrt{a} < 2\sqrt{a}$ and $-2\sqrt{a} < x - \sqrt{a} < 0$ ..Therefore, $\left(x + \sqrt{a}\right)\left(x - \sqrt{a}\right) < 0$, which is a contradiction.

If $x > \sqrt{a}$, then $x + \sqrt{a} > 2\sqrt{a} > 0$ and $x - \sqrt{a} > 0$. Therefore, $\left(x + \sqrt{a}\right)\left(x - \sqrt{a}\right) > 0$.

So the solution set for $x^2 > a$ is $\left\{x \middle| x < -\sqrt{a} \text{ or } x > \sqrt{a}\right\}$.

91. $x^2 < 1$
$-\sqrt{1} < x < \sqrt{1}$
$-1 < x < 1$
The solution set is $\left\{x \middle| -1 < x < 1\right\}$.

92. $x^2 < 4$
$-\sqrt{4} < x < \sqrt{4}$
$-2 < x < 2$
The solution set is $\left\{x \middle| -2 < x < 2\right\}$.

93. $x^2 \geq 9$
$x \leq -\sqrt{9}$ or $x \geq \sqrt{9}$
$x \leq -3$ or $x \geq 3$
The solution set is $\left\{x \middle| x \leq -3 \text{ or } x \geq 3\right\}$.

94. $x^2 \geq 1$
$x \leq -\sqrt{1}$ or $x \geq \sqrt{1}$
$x \leq -1$ or $x \geq 1$
The solution set is $\left\{x \middle| x \leq -1 \text{ or } x \geq 1\right\}$.

95. $x^2 \leq 16$
$-\sqrt{16} \leq x \leq \sqrt{16}$
$-4 \leq x \leq 4$
The solution set is $\left\{x \middle| -4 \leq x \leq 4\right\}$.

96. $x^2 \leq 9$
$-\sqrt{9} \leq x \leq \sqrt{9}$
$-3 \leq x \leq 3$
The solution set is $\left\{x \middle| -3 \leq x \leq 3\right\}$.

97. $x^2 > 4$
$x < -\sqrt{4}$ or $x > \sqrt{4}$
$x < -2$ or $x > 2$
The solution set is $\left\{x \middle| x < -2 \text{ or } x > 2\right\}$.

98. $x^2 \geq 16$
$x \leq -\sqrt{16}$ or $x \geq \sqrt{16}$
$x \leq -4$ or $x \geq 4$
The solution set is $\left\{x \middle| x < -4 \text{ or } x > 4\right\}$.

99. $\left|3x - \left|2x + 1\right|\right| = 4$
$3x - \left|2x + 1\right| = 4$ or $3x - \left|2x + 1\right| = -4$
$3x - \left|2x + 1\right| = 4$
$3x - 4 = \left|2x + 1\right|$
$2x + 1 = 3x - 4$ or $2x + 1 = -\left(3x - 4\right)$
$-x = -5$ or $2x + 1 = -3x + 4$
$x = 5$ or $5x = 3$
$x = 5$ or $x = \frac{3}{5}$

or

$3x - \left|2x + 1\right| = -4$
$3x + 4 = \left|2x + 1\right|$
$2x + 1 = 3x + 4$ or $2x + 1 = -\left(3x + 4\right)$
$-x = 3$ or $2x + 1 = -3x - 4$
$x = -3$ or $5x = -5$
$x = -3$ or $x = -1$

The values $\frac{3}{5}$ and -3 are extraneous.
The solution set is $\left\{-1, 5\right\}$.

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100. $|x+|3x-2||=2$

$x+|3x-2|=2 \quad \text{or} \quad x+|3x-2|=-2$

$x+|3x-2|=2$

$|3x-2|=2-x$

$3x-2=2-x \quad \text{or} \quad 3x-2=-(2-x)$

$4x=4 \quad \text{or} \quad 3x-2=-2+x$

$x=1 \quad \text{or} \quad 2x=0$

$x=1 \quad \text{or} \quad x=0$

or

$x+|3x-2|=-2$

$|3x-2|=-2-x$

$3x-2=-2-x \quad \text{or} \quad 3x-2=-(-2-x)$

$4x=0 \quad \text{or} \quad 3x-2=2+x$

$x=0 \quad \text{or} \quad 2x=4$

$x=0 \quad \text{or} \quad x=2$

The value 2 is extraneous. The solution set is $\{0,\ 1\}$.

101. $|2x-5|=x+13 \quad \text{or} \quad 2x-5=-(x+13)$

$2x-5=x+13 \qquad 2x-5=-x-13$

$x=18 \qquad 3x=-8$

$x=-\frac{8}{3}$

$4-3y=-2 \qquad 4-3y=2$

$-3y=-6 \quad \text{or} \quad -3y=-2$

$y=2 \qquad y=\frac{2}{3}$

The value of $\frac{y}{x}$ is largest using $x = 18$ and $y = 2$, so $\frac{y}{x}=\frac{2}{18}=\frac{1}{9}$.

102. Since $|x|\geq 0$ for all real numbers, then $\frac{|x|}{1+|x|}\geq 0$ and $1+\frac{|x|}{1+|x|}\geq 1$. This means

$1\leq 1+\frac{|x|}{1+|x|}\leq \frac{3}{2}$

$0\leq \frac{1+|x|-1}{1+|x|}\leq \frac{1}{2}$

$-1\leq \frac{-1}{1+|x|}\leq -\frac{1}{2}$

$1\geq \frac{-1}{1+|x|}\geq \frac{1}{2}$

$1\leq 1+|x|\leq 2$

$0\leq |x|\leq 1$

Therefore $-1\leq x\leq 1$. The solution set in interval notation is $[-1,1]$.

103 – 105. Answers will vary.

Section 1.7

1. mathematical modeling

2. interest

3. uniform motion

4. False; the amount charged for the use of principal is the interest.

5. True; this is the uniform motion formula.

6. **a**

7. b

8. c

9. Let A represent the area of the circle and r the radius. The area of a circle is the product of π times the square of the radius: $A=\pi r^2$

10. Let C represent the circumference of a circle and r the radius. The circumference of a circle is the product of π times twice the radius: $C=2\pi r$

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11. Let A represent the area of the square and s the length of a side. The area of the square is the square of the length of a side: $A = s^2$

12. Let P represent the perimeter of a square and s the length of a side. The perimeter of a square is four times the length of a side: $P = 4s$

13. Let F represent the force, m the mass, and a the acceleration. Force equals the product of the mass times the acceleration: $F = ma$

14. Let P represent the pressure, F the force, and A the area. Pressure is the force per unit area: $P = \dfrac{F}{A}$

15. Let W represent the work, F the force, and d the distance. Work equals force times distance: $W = Fd$

16. Let K represent the kinetic energy, m the mass, and v the velocity. Kinetic energy is one-half the product of the mass and the square of the velocity: $K = \dfrac{1}{2}mv^2$

17. $C =$ total variable cost in dollars, $x =$ number of dishwashers manufactured: $C = 150x$

18. $R =$ total revenue in dollars, $x =$ number of dishwashers sold: $R = 250x$

19. Let x represent the amount of money invested in bonds. Then $50,000 - x$ represents the amount of money invested in CD's. Since the total interest is to be \$6,000, we have:

$$0.15x + 0.07(50,000 - x) = 6,000$$
$$(100)(0.15x + 0.07(50,000 - x)) = (6,000)(100)$$
$$15x + 7(50,000 - x) = 600,000$$
$$15x + 350,000 - 7x = 600,000$$
$$8x + 350,000 = 600,000$$
$$8x = 250,000$$
$$x = 31,250$$

\$31,250 should be invested in bonds at 15% and \$18,750 should be invested in CD's at 7%.

20. Let x represent the amount of money invested in bonds. Then $50,000 - x$ represents the amount of money invested in CD's. Since the total interest is to be \$7,000, we have:

$$0.15x + 0.07(50,000 - x) = 7,000$$
$$(100)(0.15x + 0.07(50,000 - x)) = (7,000)(100)$$
$$15x + 7(50,000 - x) = 700,000$$
$$15x + 350,000 - 7x = 700,000$$
$$8x + 350,000 = 700,000$$
$$8x = 350,000$$
$$x = 43,750$$

\$43,750 should be invested in bonds at 15% and \$6,250 should be invested in CD's at 7%.

21. Let x represent the amount of money loaned at 8%. Then $12,000 - x$ represents the amount of money loaned at 18%. Since the total interest is to be \$1,000, we have:

$$0.08x + 0.18(12,000 - x) = 1,000$$
$$(100)(0.08x + 0.18(12,000 - x)) = (1,000)(100)$$
$$8x + 18(12,000 - x) = 100,000$$
$$8x + 216,000 - 18x = 100,000$$
$$-10x + 216,000 = 100,000$$
$$-10x = -116,000$$
$$x = 11,600$$

\$11,600 is loaned at 8% and \$400 is at 18%.

22. Let x represent the amount of money loaned at 16%. Then $1,000,000 - x$ represents the amount of money loaned at 19%. Since the total interest is to be \$1,000,000(0.18), we have:

$$0.16x + 0.19(1,000,000 - x) = 1,000,000(0.18)$$
$$0.16x + 190,000 - 0.19x = 180,000$$
$$-0.03x + 190,000 = 180,000$$
$$-0.03x = -10,000$$
$$x = \frac{-10,000}{-0.03}$$
$$x = \$333,333.33$$

Wendy can lend \$333,333.33 at 16%.

23. Let x represent the number of pounds of Earl Gray tea. Then $100 - x$ represents the number of pounds of Orange Pekoe tea.

$$6x + 4(100 - x) = 5.50(100)$$
$$6x + 400 - 4x = 550$$
$$2x + 400 = 550$$
$$2x = 150$$
$$x = 75$$

75 pounds of Earl Gray tea must be blended with 25 pounds of Orange Pekoe.

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24. Let x represent the number of pounds of the first kind of coffee. Then $100-x$ represents the number of pounds of the second kind of coffee.

$$2.75x+5(100-x)=4.10(100)$$
$$2.75x+500-5x=410$$
$$-2.25x+500=410$$
$$-2.25x=-90$$
$$x=40$$

40 pounds of the first kind of coffee must be blended with 60 pounds of the second kind of coffee.

25. Let x represent the number of pounds of cashews. Then $x+60$ represents the number of pounds in the mixture.

$$9x+4.50(60)=7.75(x+60)$$
$$9x+270=7.75x+465$$
$$1.25x=195$$
$$x=156$$

156 pounds of cashews must be added to the 60 pounds of almonds.

26. Let x represent the number of caramels in the box. Then $30-x$ represents the number of cremes in the box.

$$\text{Revenue}-\text{Cost}=\text{Profit}$$
$$12.50-\left(0.25x+0.45(30-x)\right)=3.00$$
$$12.50-\left(0.25x+13.5-0.45x\right)=3.00$$
$$12.50-\left(13.5-0.20x\right)=3.00$$
$$12.50-13.50+0.20x=3.00$$
$$-1.00+0.20x=3.00$$
$$0.20x=4.00$$
$$x=20$$

The box should contain 20 caramels and 10 cremes.

27. Let r represent the speed of the current.

	Rate	Time	Distance
Upstream	$16-r$	$\frac{20}{60}=\frac{1}{3}$	$\frac{16-r}{3}$
Downstream	$16+r$	$\frac{15}{60}=\frac{1}{4}$	$\frac{16+r}{4}$

Since the distance is the same in each direction:

$$\frac{16-r}{3}=\frac{16+r}{4}$$
$$4(16-r)=3(16+r)$$
$$64-4r=48+3r$$
$$16=7r$$
$$r=\frac{16}{7}\approx 2.286$$

The speed of the current is approximately 2.286 miles per hour.

28. Let r represent the speed of the motorboat.

	Rate	Time	Distance
Upstream	$r-3$	5	$5(r-3)$
Downstream	$r+3$	2.5	$2.5(r+3)$

The distance is the same in each direction:

$$5(r-3)=2.5(r+3)$$
$$5r-15=2.5r+7.5$$
$$2.5r=22.5$$
$$r=9$$

The speed of the motorboat is 9 miles per hour.

29. Let r represent the speed of the current.

	Rate	Time	Distance
Upstream	$15-r$	$\frac{10}{15-r}$	10
Downstream	$15+r$	$\frac{10}{15+r}$	10

Since the total time is 1.5 hours, we have:

$$\frac{10}{15-r}+\frac{10}{15+r}=1.5$$
$$10(15+r)+10(15-r)=1.5(15-r)(15+r)$$
$$150+10r+150-10r=1.5(225-r^2)$$
$$300=1.5(225-r^2)$$
$$200=225-r^2$$
$$r^2-25=0$$
$$(r-5)(r+5)=0$$
$$r=5 \text{ or } r=-5$$

Speed must be positive, so disregard $r=-5$.
The speed of the current is 5 miles per hour.

30. Let r represent the rate of the slower car. Then $r+10$ represents the rate of the faster car.

	Rate	Time	Distance
Slower car	r	3.5	$3.5r$
Faster car	$r+10$	3	$3(r+10)$

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$$3.5r = 3(r+10)$$
$$3.5r = 3r+30$$
$$0.5r = 30$$
$$r = 60$$

The slower car travels at a rate of 60 miles per hour. The faster car travels at a rate of 70 miles per hour. The distance is (70)(3) = 210 miles.

31. Let r represent Karen's normal walking speed.

	Rate	Time	Distance
With walkway	$r+2.5$	$\frac{50}{r+2.5}$	50
Against walkway	$r-2.5$	$\frac{50}{r-2.5}$	50

Since the total time is 48 seconds:

$$\frac{50}{r+2.5}+\frac{50}{r-2.5}=48$$
$$50(r-2.5)+50(r+2.5)=48(r-2.5)(r+2.5)$$
$$50r-125+50r+125=48(r^2-6.25)$$
$$100r=48r^2-300$$
$$0=48r^2-100r-300$$
$$0=12r^2-25r-75$$
$$r=\frac{-(-25)\pm\sqrt{(-25)^2-4(12)(-75)}}{2(12)}$$
$$=\frac{25\pm\sqrt{4225}}{24}$$
$$r\approx 3.75 \text{ or } r\approx -1.67$$

Speed must be positive, so disregard $r\approx -1.67$. Karen' normal walking speed is approximately 3.75 feet per second.

32. Let r represent the speed of the airport walkway.

	Rate	Time	Distance
Walking with	$1.5+r$	$\frac{280}{1.5+r}$	280
Standing still	r	$\frac{280}{r}$	280

Walking with the walkway takes 60 seconds less time than standing still on the walkway:

$$\frac{280}{1.5+r}=\frac{280}{r}-60$$
$$280r=280(1.5+r)-60r(r+1.5)$$
$$280r=420+280r-60r^2-90r$$
$$60r^2+90r-420=0$$
$$2r^2+3r-14=0$$
$$(2r+7)(r-2)=0$$
$$2r+7=0 \quad \text{or} \quad r-2=0$$
$$r=-\frac{7}{2} \quad \text{or} \quad r=2$$

Speed must be positive, so disregard $r=-\frac{7}{2}$.

The speed of the airport walkway is 2 meters per second.

33. Let w represent the width of a regulation doubles tennis court. Then $2w+6$ represents the length. The area is 2808 square feet:

$$w(2w+6)=2808$$
$$2w^2+6w=2808$$
$$2w^2+6w-2808=0$$
$$w^2+3w-1404=0$$
$$(w+39)(w-36)=0$$
$$w+39=0 \quad \text{or} \quad w-36=0$$
$$w=-39 \text{ or } w=36$$

The width must be positive, so disregard $w=-39$. The width of a regulation doubles tennis court is 36 feet and the length is 2(36) + 6 = 78 feet.

34. Let t represent the time it takes the Brother HL-L8350CDW to complete the print job alone. Then $t+9$ represents the time it takes the Xerox VersaLink C500 to complete the print job alone.

	Time to do job	Part of job done in one minute
Brother	t	$\frac{1}{t}$
Xerox	$t+9$	$\frac{1}{t+9}$
Together	20	$\frac{1}{20}$

$$\frac{1}{t}+\frac{1}{t+9}=\frac{1}{20}$$
$$20(t+9)+20t=t(t+9)$$
$$20t+180+20t=t^2+9t$$
$$0=t^2-31t-180$$
$$0=(t-36)(t+5)$$

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$t-36=0 \quad \text{or} \quad t+5=0$

$t=36 \quad \text{or} \quad t=-5$

Time must be positive, so disregard $t=-5$.
The Brother HL-L8350CDW takes 36 minutes to complete the job alone, printing $\frac{1440}{36}=40$ pages per minute. Xerox VersaLink C500 takes $36+9=45$ minutes to complete the job alone, printing $\frac{1440}{45}=32$ pages per minute.

35. Let t represent the time it takes to do the job together.

	Time to do job	Part of job done in one minute
Trent	30	$\frac{1}{30}$
Lois	20	$\frac{1}{20}$
Together	t	$\frac{1}{t}$

$$\frac{1}{30}+\frac{1}{20}=\frac{1}{t}$$
$$2t+3t=60$$
$$5t=60$$
$$t=12$$

Working together, the job can be done in 12 minutes.

36. Let t represent the time it takes April to do the job working alone.

	Time to do job	Part of job done in one hour
Patrice	10	$\frac{1}{10}$
April	t	$\frac{1}{t}$
Together	6	$\frac{1}{6}$

$$\frac{1}{10}+\frac{1}{t}=\frac{1}{6}$$
$$3t+30=5t$$
$$2t=30$$
$$t=15$$

April would take 15 hours to paint the rooms.

37. $l=$ length of the garden
$w=$ width of the garden

a. The length of the garden is to be twice its width. Thus, $l=2w$.
The dimensions of the fence are $l+4$ and $w+4$.
The perimeter is 46 feet, so:

$$2(l+4)+2(w+4)=46$$
$$2(2w+4)+2(w+4)=46$$
$$4w+8+2w+8=46$$
$$6w+16=46$$
$$6w=30$$
$$w=5$$

The dimensions of the garden are 5 feet by 10 feet.

b. Area $=l\cdot w=5\cdot 10=50$ square feet

c. If the dimensions of the garden are the same, then the length and width of the fence are also the same $(l+4)$. The perimeter is 46 feet, so:

$$2(l+4)+2(l+4)=46$$
$$2l+8+2l+8=46$$
$$4l+16=46$$
$$4l=30$$
$$l=7.5$$

The dimensions of the garden are 7.5 feet by 7.5 feet.

d. Area $=l\cdot w=7.5(7.5)=56.25$ square feet.

38. $l=$ length of the pond
$w=$ width of the pond

a. The pond is to be a square. Thus, $l=w$.
The dimensions of the fenced area are $w+6$ on each side. The perimeter is 100 feet, so:

$$4(w+6)=100$$
$$4w+24=100$$
$$4w=76$$
$$w=19$$

The dimensions of the pond are 19 feet by 19 feet.

b. The length of the pond is to be three times the width. Thus, $l=3w$. The dimensions of the fenced area are $w+6$ and $l+6$. The perimeter is 100 feet, so:

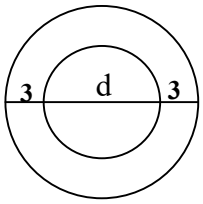
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$$2(w+6)+2(l+6)=100$$
$$2(w+6)+2(3w+6)=100$$
$$2w+12+6w+12=100$$
$$8w+24=100$$
$$8w=76$$
$$w=9.5$$
$$l=3(9.5)=28.5$$

The dimensions of the pond are 9.5 feet by 28.5 feet.

c. If the pond is circular, the diameter is d and the diameter of the circle with the pond and the deck is $d+6$.



The perimeter is 100 feet, so:

$$\pi(d+6)=100$$
$$\pi d+6\pi=100$$
$$\pi d=100-6\pi$$
$$d=\frac{100}{\pi}-6\approx 25.83$$

The diameter of the pond is 25.83 feet.

d. $\text{Area}_{\text{square}}=l\cdot w=19(19)=361 \text{ ft}^2$.

$\text{Area}_{\text{rectangle}}=l\cdot w=28.5(9.5)=270.75 \text{ ft}^2$.

$\text{Area}_{\text{circle}}=\pi r^2=\pi\left(\frac{25.83}{2}\right)^2\approx 524 \text{ ft}^2$.

The circular pond has the largest area.

39. Let t represent the time it takes for the defensive back to catch the tight end.

	Time to run 100 yards	Time	Rate	Distance
Tight End	12 sec	t	$\frac{100}{12}=\frac{25}{3}$	$\frac{25}{3}t$
Def. Back	10 sec	t	$\frac{100}{10}=10$	$10t$

Since the defensive back has to run 5 yards farther, we have:

$$\frac{25}{3}t+5=10t$$
$$25t+15=30t$$
$$15=5t$$
$$t=3 \quad \rightarrow \quad 10t=30$$

The defensive back will catch the tight end at the 45 yard line (15 + 30 = 45).

40. Let x represent the number of highway miles traveled. Then $30,000-x$ represents the number of city miles traveled.

$$\frac{x}{40}+\frac{30,000-x}{25}=900$$
$$200\left(\frac{x}{40}+\frac{30,000-x}{25}\right)=200(900)$$
$$5x+240,000-8x=180,000$$
$$-3x+240,000=180,000$$
$$-3x=-60,000$$
$$x=20,000$$

Therese is allowed to claim 20,000 miles as a business expense.

41. Let x represent the number of gallons of pure water. Then $x+1$ represents the number of gallons in the 60% solution.

$$(\%)(\text{gallons})+(\%)(\text{gallons})=(\%)(\text{gallons})$$
$$0(x)+1(1)=0.60(x+1)$$
$$1=0.6x+0.6$$
$$0.4=0.6x$$
$$x=\frac{4}{6}=\frac{2}{3}$$

$\frac{2}{3}$ gallon of pure water should be added.

42. Let x represent the number of liters to be drained and replaced with pure antifreeze.

$$(\%)(\text{liters})+(\%)(\text{liters})=(\%)(\text{liters})$$
$$1(x)+0.40(15-x)=0.60(15)$$
$$x+6-0.40x=9$$
$$0.60x=3$$
$$x=5$$

5 liters should be drained and replaced with pure antifreeze.

43. Let x represent the number of ounces of water to be evaporated; the amount of salt remains the same. Therefore, we get

$$0.04(32)=0.06(32-x)$$
$$1.28=1.92-0.06x$$
$$0.06x=0.64$$
$$x=\frac{0.64}{0.06}=\frac{64}{6}=\frac{32}{3}=10\frac{2}{3}$$

$10\frac{2}{3}\approx 10.67$ ounces of water need to be evaporated.

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44. Let x represent the number of gallons of water to be evaporated; the amount of salt remains the same.

$$0.03(240) = 0.05(240 - x)$$
$$7.2 = 12 - 0.05x$$
$$0.05x = 4.8$$
$$x = \frac{4.8}{0.05} = 96$$

96 gallons of water need to be evaporated.

45. Let x represent the number of grams of pure gold. Then $60 - x$ represents the number of grams of 12 karat gold to be used.

$$x + \frac{1}{2}(60 - x) = \frac{2}{3}(60)$$
$$x + 30 - 0.5x = 40$$
$$0.5x = 10$$
$$x = 20$$

20 grams of pure gold should be mixed with 40 grams of 12 karat gold.

46. Let x represent the number of atoms of oxygen.
$2x$ represents the number of atoms of hydrogen.
$x + 1$ represents the number of atoms of carbon.

$$x + 2x + x + 1 = 45$$
$$4x = 44$$
$$x = 11$$

There are 11 atoms of oxygen and 22 atoms of hydrogen in the sugar molecule.

47. Let t represent the time it takes for Mike to catch up with Dan. Since the distances are the same, we have:

$$\frac{1}{6}t = \frac{1}{9}(t + 1)$$
$$3t = 2t + 2$$
$$t = 2$$

Mike will pass Dan after 2 minutes, which is a distance of $\frac{1}{3}$ mile.

48. Let t represent the time of flight with the wind. The distance is the same in each direction:

$$330t = 270(5 - t)$$
$$330t = 1350 - 270t$$
$$600t = 1350$$
$$t = 2.25$$

The distance the plane can fly and still return safely is 330(2.25) = 742.5 miles.

49. Let t represent the time the auxiliary pump needs to run. Since the two pumps are emptying one tanker, we have:

$$\frac{3}{4} + \frac{t}{9} = 1$$
$$27 + 4t = 36$$
$$4t = 9$$
$$t = \frac{9}{4} = 2.25$$

The auxiliary pump must run for 2.25 hours. It must be started at 9:45 a.m.

50. Let x represent the number of pounds of pure cement. Then $x + 20$ represents the number of pounds in the 40% mixture.

$$x + 0.25(20) = 0.40(x + 20)$$
$$x + 5 = 0.4x + 8$$
$$0.6x = 3$$
$$x = \frac{30}{6} = 5$$

5 pounds of pure cement should be added.

51. Let t represent the time for the tub to fill with the faucets on and the stopper removed. Since one tub is being filled, we have:

$$\frac{t}{15} + \left(-\frac{t}{20}\right) = 1$$
$$4t - 3t = 60$$
$$t = 60$$

60 minutes is required to fill the tub.

52. Let t be the time the 5 horsepower pump needs to run to finish emptying the pool. Since the two pumps are emptying one pool, we have:

$$\frac{t+2}{5} + \frac{2}{8} = 1$$
$$4(2 + t) + 5 = 20$$
$$8 + 4t + 5 = 20$$
$$4t = 7$$
$$t = 1.75$$

The 5 horsepower pump must run for an additional 1.75 hours or 1 hour and 45 minutes to empty the pool.

53. Let t represent the time spent running. Then $5 - t$ represents the time spent biking.

	Rate	Time	Distance
Run	6	t	$6t$
Bike	25	$5 - t$	$25(5 - t)$

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The total distance is 87 miles:

$$6t + 25(5 - t) = 87$$
$$6t + 125 - 25t = 87$$
$$-19t + 125 = 87$$
$$-19t = -38$$
$$t = 2$$

The time spent running is 2 hours, so the distance of the run is $6(2) = 12$ miles. The distance of the bicycle race is $25(5 - 2) = 75$ miles.

54. Let r represent the speed of the eastbound cyclist. Then $r + 5$ represents the speed of the westbound cyclist.

	Rate	Time	Distance
Eastbound	r	6	$6r$
Westbound	$r + 5$	6	$6(r + 5)$

The total distance is 246 miles:

$$6r + 6(r + 5) = 246$$
$$6r + 6r + 30 = 246$$
$$12r + 30 = 246$$
$$12r = 216$$
$$r = 18$$

The speed of the eastbound cyclist is 18 miles per hour, and the speed of the westbound cyclist is $18 + 5 = 23$ miles per hour.

55. Burke's rate is $\frac{100}{12}$ meters/sec. In 9.81 seconds, Burke will run $\frac{100}{12}(9.81) = 81.75$ meters. Bolt would win by 100-81.75=18.25 meters.

56. $A = 2\pi r^2 + 2\pi r h$. Since $A = 58.9\pi$ square inches and $h = 6.4$ inches,

$$2\pi r^2 + 2\pi r(6.4) = 58.9\pi$$
$$2\pi r^2 + 12.8\pi r - 58.9\pi = 0$$
$$2r^2 + 12.8r - 58.9 = 0$$

$$r = \frac{-12.8 \pm \sqrt{(12.8)^2 - 4(2)(-58.9)}}{2(2)}.$$
$$= \frac{-12.8 \pm \sqrt{635.04}}{4}$$

$r = 3.1$ or ~~$r = -9.5$~~

The radius of the coffee can is 3.1 inches.

57. Let the individual times to complete the project be E for Elaine, B for Brian, and D for either daughter. Using the respective rates gives

$\frac{1}{E} + \frac{1}{B} = \frac{1}{2}, \frac{1}{E} + \frac{1}{D} + \frac{1}{D} = \frac{1}{2}$ (or $\frac{1}{E} + \frac{2}{D} = \frac{1}{2}$), and $\frac{1}{B} + \frac{1}{D} = \frac{1}{4}$. From the first two equations, $\frac{1}{B} = \frac{2}{D}$. Substituting into the third equation gives $\frac{2}{D} + \frac{1}{D} = \frac{1}{4}$ or $\frac{3}{D} = \frac{1}{4} \rightarrow D = 12$ hours. Then $\frac{1}{E} + \frac{2}{12} = \frac{1}{2} \rightarrow E = 3$ hours and $\frac{1}{B} + \frac{1}{12} = \frac{1}{4} \rightarrow B = 6$ hours. The combined rate of Elaine, Brian, and one of their daughters is $\frac{1}{3} + \frac{1}{6} + \frac{1}{12} = \frac{7}{12}$ project per hour, so it will take them $\frac{12}{7}$ hours to complete the project.

58. If x = liters of original solution, then there were originally $0.2x$ liters of salt and 0.8 liters of pure water. Over time, the solution loses $0.25(0.8x) = 0.2x$ liters of pure water. She adds 20 liters of salt so the total amount of salt is $0.2x + 20$ liters. She also adds 10 liters of pure water, so the total amount of pure water is $0.8x - 0.2x + 10 = 0.6x + 10$ liters. The resulting concentration is 33 1/3% which means $\frac{0.2x + 20}{0.2x + 20 + 0.6x + 10} = \frac{1}{3}$ or $\frac{0.2x + 20}{0.8x + 30} = \frac{1}{3}$ or $0.6x + 60 = 0.8x + 30 \rightarrow x = 150$. There were initially 150 liters of solution in the vat.

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59. The speed of the train relative to the man is 30 – 4 = 26 miles per hour. The time is

$$5 \text{ sec} = \frac{5}{60} \text{ min} = \frac{5}{3600} \text{ h} = \frac{1}{720} \text{ h.}$$

$$d = rt$$

$$= 26\left(\frac{1}{720}\right)$$

$$= \frac{26}{720} \text{ miles}$$

$$= \frac{26}{720} \cdot 5280 \approx 190.67 \text{ feet}$$

The freight train is about 190.67 feet long.

60. Answers will vary.

61. Let x be the original selling price of the shirt.

Profit = Revenue – Cost

$4 = x - 0.40x - 20 \rightarrow 24 = 0.60x \rightarrow x = 40$

The original price should be \$40 to ensure a profit of \$4 after the sale.

If the sale is 50% off, the profit is:

$40 - 0.50(40) - 20 = 40 - 20 - 20 = 0$

At 50% off there will be no profit.

62. Let t_1 and t_2 represent the times for the two segments of the trip. Since Atlanta is halfway between Chicago and Miami, the distances are equal.

$$45t_1 = 55t_2$$

$$t_1 = \frac{55}{45}t_2$$

$$t_1 = \frac{11}{9}t_2$$

Computing the average speed:

$$\text{Avg Speed} = \frac{\text{Distance}}{\text{Time}} = \frac{45t_1 + 55t_2}{t_1 + t_2}$$

$$= \frac{45\left(\frac{11}{9}t_2\right) + 55t_2}{\frac{11}{9}t_2 + t_2} = \frac{55t_2 + 55t_2}{\left(\frac{11t_2 + 9t_2}{9}\right)}$$

$$= \frac{110t_2}{\left(\frac{20t_2}{9}\right)} = \frac{990t_2}{20t_2}$$

$$= \frac{99}{2} = 49.5 \text{ miles per hour}$$

The average speed for the trip from Chicago to Miami is 49.5 miles per hour.

63. The time traveled with the tail wind was:

$t = \frac{919}{550} \approx 1.67091$ hours.

Since they were 20 minutes $\left(\frac{1}{3} \text{ hour}\right)$ early, the time in still air would have been:

$$1.67091 \text{ hrs} + 20 \text{ min} = (1.67091 + 0.33333) \text{ hrs}$$

$$\approx 2.00424 \text{ hrs}$$

Thus, with no wind, the ground speed is $\frac{919}{2.00424} \approx 458.53$. Therefore, the tail wind is $550 - 458.53 = 91.47$ knots.

64. It is impossible to mix two solutions with a lower concentration and end up with a new solution with a higher concentration.

Algebraic Solution:

Let x = the number of liters of 25% solution.

$$(\%)(\text{liters}) + (\%)(\text{liters}) = (\%)(\text{liters})$$

$$0.25x + 0.48(20) = 0.58(20 + x)$$

$$0.25x + 9.6 = 10.6 + 0.58x$$

$$-0.33x = 1$$

$$x \approx -3.03 \text{ liters}$$

(not possible)

Chapter 1 Review

1. $2 - \frac{x}{3} = 8$

$6 - x = 24$

$x = -18$

The solution set is $\{-18\}$.

2. $-2(5 - 3x) + 8 = 4 + 5x$

$-10 + 6x + 8 = 4 + 5x$

$6x - 2 = 4 + 5x$

$x = 6$

The solution set is $\{6\}$.

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3. $\dfrac{x}{x-1}=\dfrac{6}{5}$

$5x=6x-6$

$6=x$

Since $x=6$ does not cause a denominator to equal zero, the solution set is $\{6\}$.

4. $(2x+7)^2=20$

$2x+7=\pm\sqrt{20}$

$2x+7=\pm 2\sqrt{5}$

$2x=-7\pm 2\sqrt{5}$

$x=\dfrac{-7\pm 2\sqrt{5}}{2}$

The solution set is $\left\{\dfrac{-7-2\sqrt{5}}{2},\dfrac{-7+2\sqrt{5}}{2}\right\}$

5. $x(1-x)=6$

$x-x^2=6$

$0=x^2-x+6$

$b^2-4ac=(-1)^2-4(1)(6)$

$=1-24=-23$

Therefore, there are no real solutions.

6. $x(1+x)=6$

$x+x^2=6$

$x^2+x-6=0$

$(x+3)(x-2)=0$

$x=-3$ or $x=2$

The solution set is $\{-3,2\}$.

7. $\dfrac{1}{2}\left(x-\dfrac{1}{3}\right)=\dfrac{3}{4}-\dfrac{x}{6}$

$(12)\left(\dfrac{1}{2}\right)\left(x-\dfrac{1}{3}\right)=\left(\dfrac{3}{4}-\dfrac{x}{6}\right)(12)$

$6x-2=9-2x$

$8x=11$

$x=\dfrac{11}{8}$

The solution set is $\left\{\dfrac{11}{8}\right\}$.

8. $\dfrac{1-3x}{4}=\dfrac{x+6}{3}+\dfrac{1}{2}$

$(12)\left(\dfrac{1-3x}{4}\right)=\left(\dfrac{x+6}{3}+\dfrac{1}{2}\right)(12)$

$3(1-3x)=4(x+6)+6$

$3-9x=4x+24+6$

$-13x=27$

$x=-\dfrac{27}{13}$

The solution set is $\left\{-\dfrac{27}{13}\right\}$.

9. $(x-1)(2x+3)=3$

$2x^2+x-3=3$

$2x^2+x-6=0$

$(2x-3)(x+2)=0$

$x=\dfrac{3}{2}$ or $x=-2$

The solution set is $\left\{-2,\dfrac{3}{2}\right\}$.

10. $2x+3=4x^2$

$0=4x^2-2x-3$

$x=\dfrac{-(-2)\pm\sqrt{(-2)^2-4(4)(-3)}}{2(4)}$

$=\dfrac{2\pm\sqrt{52}}{8}=\dfrac{2\pm 2\sqrt{13}}{8}=\dfrac{1\pm\sqrt{13}}{4}$

The solution set is $\left\{\dfrac{1-\sqrt{13}}{4},\dfrac{1+\sqrt{13}}{4}\right\}$.

11. $\sqrt[3]{x^2-1}=2$

$\left(\sqrt[3]{x^2-1}\right)^3=(2)^3$

$x^2-1=8$

$x^2=9$

$x=\pm 3$

Check $x=-3$:

$\sqrt[3]{(-3)^2-1}=2$

$\sqrt[3]{9-1}=2$

$\sqrt[3]{8}=2$

$2=2$

Check $x=3$:

$\sqrt[3]{(3)^2-1}=2$

$\sqrt[3]{9-1}=2$

$\sqrt[3]{8}=2$

$2=2$

The solution set is $\{-3,3\}$.

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12. $\sqrt{1+x^3} = 3$

$\left(\sqrt{1+x^3}\right)^2 = (3)^2$

$1+x^3 = 9$

$x^3 = 8$

$x = \sqrt[3]{8} = 2$

Check $x = 2$: $\sqrt{1+(2)^3} = 3$

$\sqrt{9} = 3$

$3 = 3$

The solution set is $\{2\}$.

13. $x(x+1)+2 = 0$

$x^2 + x + 2 = 0$

$x = \dfrac{-1 \pm \sqrt{(1)^2 - 4(1)(2)}}{2(1)} = \dfrac{-1 \pm \sqrt{-7}}{2}$

No real solution.

14. $x^4 - 5x^2 + 4 = 0$

$(x^2 - 4)(x^2 - 1) = 0$

$x^2 - 4 = 0$ or $x^2 - 1 = 0$

$x = \pm 2$ or $x = \pm 1$

The solution set is $\{-2, -1, 1, 2\}$.

15. $\sqrt{2x-3} + x = 3$

$\sqrt{2x-3} = 3 - x$

$2x - 3 = 9 - 6x + x^2$

$x^2 - 8x + 12 = 0$

$(x-2)(x-6) = 0$

$x = 2$ or $x = 6$

Check $x = 2$: $\sqrt{2(2)-3} + 2 = \sqrt{1} + 2 = 3$

Check $x = 6$: $\sqrt{2(6)-3} + 6 = \sqrt{9} + 6 = 9 \neq 3$

The solution set is $\{2\}$.

16. $\sqrt[4]{2x+3} = 2$

$\left(\sqrt[4]{2x+3}\right)^4 = 2^4$

$2x + 3 = 16$

$2x = 13$

$x = \dfrac{13}{2}$

Check $x = \dfrac{13}{2}$:

$\sqrt[4]{2\left(\dfrac{13}{2}\right)+3} = \sqrt[4]{13+3} = \sqrt[4]{16} = 2$

The solution set is $\left\{\dfrac{13}{2}\right\}$.

17. $\sqrt{4x^2 + x - 6} = \sqrt{x-1}$

$\left(\sqrt{4x^2 + x - 6}\right)^2 = \left(\sqrt{x-1}\right)^2$

$4x^2 + x - 6 = x - 1$

$4x^2 = 5$

$x^2 = \dfrac{5}{4}$

$x = \pm\sqrt{\dfrac{5}{4}} = \pm\dfrac{\sqrt{5}}{2}$

Check $x = \dfrac{\sqrt{5}}{2}$:

$\sqrt{4\left(\dfrac{\sqrt{5}}{2}\right)^2 + \dfrac{\sqrt{5}}{2} - 6} = \sqrt{\left(\dfrac{\sqrt{5}}{2}\right) - 1}$

$0.34356 = 0.34356$

Check $x = -\dfrac{\sqrt{5}}{2}$:

$\sqrt{4\left(-\dfrac{\sqrt{5}}{2}\right)^2 - \dfrac{\sqrt{5}}{2} - 6} = \sqrt{\left(-\dfrac{\sqrt{5}}{2}\right) - 1}$

The second solution is not possible because it makes the radicand negative.

The solution set is $\left\{\dfrac{\sqrt{5}}{2}\right\}$.

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18. $\sqrt{2x-1}-\sqrt{x-5}=3$

$$\sqrt{2x-1}=3+\sqrt{x-5}$$
$$\left(\sqrt{2x-1}\right)^2=\left(3+\sqrt{x-5}\right)^2$$
$$2x-1=9+6\sqrt{x-5}+x-5$$
$$x-5=6\sqrt{x-5}$$
$$(x-5)^2=\left(6\sqrt{x-5}\right)^2$$
$$x^2-10x+25=36(x-5)$$
$$x^2-10x+25=36x-180$$
$$x^2-46x+205=0$$
$$(x-41)(x-5)=0$$
$$x=41 \text{ or } x=5$$

Check $x=41$:

$\sqrt{2(41)-1}-\sqrt{41-5}=\sqrt{81}-\sqrt{36}=9-6=3$

Check $x=5$:

$\sqrt{2(5)-1}-\sqrt{5-5}=\sqrt{9}-\sqrt{0}=3-0=3$

The solution set is $\{5,41\}$.

19. $2x^{1/2}-3=0$

$$2x^{1/2}=3$$
$$\left(2x^{1/2}\right)^2=3^2$$
$$4x=9$$
$$x=\frac{9}{4}$$

Check $x=\frac{9}{4}$:

$$2\left(\frac{9}{4}\right)^{1/2}-3=2\left(\frac{3}{2}\right)-3=3-3=0$$

The solution set is $\left\{\frac{9}{4}\right\}$.

20. $x^{-6}-7x^{-3}-8=0$

Let $u=x^{-3}$ so that $u^2=x^{-6}$.

$$u^2-7u-8=0$$
$$(u-8)(u+1)=0$$
$$u=8 \quad \text{or} \quad u=-1$$
$$x^{-3}=8 \quad \text{or} \quad x^{-3}=-1$$
$$\left(x^{-3}\right)^{-1/3}=(8)^{-1/3} \quad \text{or} \quad \left(x^{-3}\right)^{-1/3}=(-1)^{-1/3}$$
$$x=\frac{1}{2} \quad \text{or} \quad x=-1$$

Check $\frac{1}{2}$: $\left(\frac{1}{2}\right)^{-6}-7\left(\frac{1}{2}\right)^{-3}-8=64-56-8=0$

Check -1: $(-1)^{-6}-7(-1)^{-3}-8=1+7-8=0$

The solution set is $\left\{-1,\frac{1}{2}\right\}$.

21.
$$x^2+m^2=2mx+(nx)^2$$
$$x^2+m^2=2mx+n^2x^2$$
$$x^2-n^2x^2-2mx+m^2=0$$
$$(1-n^2)x^2-2mx+m^2=0$$
$$x=\frac{-(-2m)\pm\sqrt{(-2m)^2-4(1-n^2)m^2}}{2(1-n^2)}$$
$$=\frac{2m\pm\sqrt{4m^2-4m^2+4m^2n^2}}{2(1-n^2)}$$
$$=\frac{2m\pm\sqrt{4m^2n^2}}{2(1-n^2)}=\frac{2m\pm 2mn}{2(1-n^2)}$$
$$=\frac{2m(1\pm n)}{2(1-n^2)}=\frac{m(1\pm n)}{1-n^2}$$
$$x=\frac{m(1+n)}{1-n^2}=\frac{m(1+n)}{(1+n)(1-n)}=\frac{m}{1-n}$$

or

$$x=\frac{m(1-n)}{1-n^2}=\frac{m(1-n)}{(1+n)(1-n)}=\frac{m}{1+n}$$

The solution set is $\left\{\frac{m}{1-n},\frac{m}{1+n}\right\}$, $n\neq 1$, $n\neq -1$.

22. $10a^2x^2-2abx-36b^2=0$

$$5a^2x^2-abx-18b^2=0$$
$$(5ax+9b)(ax-2b)=0$$
$$5ax+9b=0 \quad \text{or} \quad ax-2b=0$$
$$5ax=-9b \qquad ax=2b$$
$$x=-\frac{9b}{5a} \qquad x=\frac{2b}{a}$$

The solution set is $\left\{-\frac{9b}{5a},\frac{2b}{a}\right\}$, $a\neq 0$.

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23. $\sqrt{x^2+3x+7}-\sqrt{x^2-3x+9}+2=0$

$\sqrt{x^2+3x+7}=\sqrt{x^2-3x+9}-2$

$\left(\sqrt{x^2+3x+7}\right)^2=\left(\sqrt{x^2-3x+9}-2\right)^2$

$x^2+3x+7=x^2-3x+9-4\sqrt{x^2-3x+9}+4$

$6x-6=-4\sqrt{x^2-3x+9}$

$\left(6(x-1)\right)^2=\left(-4\sqrt{x^2-3x+9}\right)^2$

$36(x^2-2x+1)=16(x^2-3x+9)$

$36x^2-72x+36=16x^2-48x+144$

$20x^2-24x-108=0$

$5x^2-6x-27=0$

$(5x+9)(x-3)=0$

$x=-\frac{9}{5}$ or $x=3$

Check $x=-\frac{9}{5}$:

$\sqrt{\left(-\frac{9}{5}\right)^2+3\left(-\frac{9}{5}\right)+7}-\sqrt{\left(-\frac{9}{5}\right)^2-3\left(-\frac{9}{5}\right)+9}+2$

$=\sqrt{\frac{81}{25}-\frac{27}{5}+7}-\sqrt{\frac{81}{25}+\frac{27}{5}+9}+2$

$=\sqrt{\frac{81-135+175}{25}}-\sqrt{\frac{81+135+225}{25}}+2$

$=\sqrt{\frac{121}{25}}-\sqrt{\frac{441}{25}}+2=\frac{11}{5}-\frac{21}{5}+2=0$

Check $x=3$:

$\sqrt{(3)^2+3(3)+7}-\sqrt{(3)^2-3(3)+9}+2$

$=\sqrt{9+9+7}-\sqrt{9-9+9}+2$

$=\sqrt{25}-\sqrt{9}+2=2+2$

$=4\neq 0$

The solution set is $\left\{-\frac{9}{5}\right\}$.

24. $|2x+3|=7$

$2x+3=7$ or $2x+3=-7$

$2x=4$ or $2x=-10$

$x=2$ or $x=-5$

The solution set is $\{-5, 2\}$.

25. $|2-3x|+2=9$

$|2-3x|=7$

$2-3x=7$ or $2-3x=-7$

$-3x=5$ or $-3x=-9$

$x=-\frac{5}{3}$ or $x=3$

The solution set is $\left\{-\frac{5}{3},3\right\}$

26. $2x^3=3x^2$

$2x^3-3x^2=0$

$x^2(2x-3)=0$

$x^2=0$ or $2x-3=0$

$x=0$ or $x=\frac{3}{2}$

The solution set is $\left\{0,\frac{3}{2}\right\}$.

27. $2x^3+5x^2-8x-20=0$

$x^2(2x+5)-4(2x+5)=0$

$(2x+5)(x^2-4)=0$

$2x+5=0$ or $x^2-4=0$

$2x=-5$ or $x^2=4$

$x=-\frac{5}{2}$ or $x=\pm 2$

The solution set is $\left\{-\frac{5}{2},-2,2\right\}$.

28. $\frac{2x-3}{5}+2\le\frac{x}{2}$

$2(2x-3)+10(2)\le 5x$

$4x-6+20\le 5x$

$14\le x$

$x\ge 14$

$\{x\,|\,x\ge 14\}$ or $[14,\infty)$



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29. $-9 \le \dfrac{2x+3}{-4} \le 7$

$36 \ge 2x+3 \ge -28$

$33 \ge \quad 2x \quad \ge -31$

$\dfrac{33}{2} \ge \quad x \quad \ge -\dfrac{31}{2}$

$-\dfrac{31}{2} \le \quad x \quad \le \dfrac{33}{2}$

$\left\{x \middle| -\dfrac{31}{2} \le x \le \dfrac{33}{2}\right\}$ or $\left[-\dfrac{31}{2}, \dfrac{33}{2}\right]$



30. $2 < \dfrac{3-3x}{12} < 6$

$24 < 3-3x < 72$

$21 < \ -3x \ < 69$

$-7 > \quad x \quad > -23$

$\{x \mid -23 < x < -7\}$ or $(-23, -7)$



31. $\left|3x+4\right| < \dfrac{1}{2}$

$-\dfrac{1}{2} < 3x+4 < \dfrac{1}{2}$

$-\dfrac{9}{2} < \quad 3x \quad < -\dfrac{7}{2}$

$-\dfrac{3}{2} < \quad x \quad < -\dfrac{7}{6}$

$\left\{x \middle| -\dfrac{3}{2} < x < -\dfrac{7}{6}\right\}$ or $\left(-\dfrac{3}{2}, -\dfrac{7}{6}\right)$



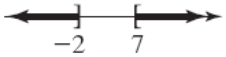
32. $\left|2x-5\right| \ge 9$

$2x-5 \le -9$ or $2x-5 \ge 9$

$2x \le -4$ or $2x \ge 14$

$x \le -2$ or $x \ge 7$

$\{x \mid x \le -2 \text{ or } x \ge 7\}$ or $(-\infty, -2] \cup [7, \infty)$



33. $2 + \left|2-3x\right| \le 4$

$\left|2-3x\right| \le 2$

$-2 \le 2-3x \le 2$

$-4 \le -3x \le 0$

$\dfrac{4}{3} \ge x \ge 0$

$\left\{x \middle| 0 \le x \le \dfrac{4}{3}\right\}$ or $\left[0, \dfrac{4}{3}\right]$



34. $1 - \left|2-3x\right| < -4$

$-\left|2-3x\right| < -5$

$\left|2-3x\right| > 5$

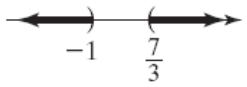
$2-3x < -5$ or $2-3x > 5$

$7 < 3x$ or $-3 > 3x$

$\dfrac{7}{3} < x$ or $-1 > x$

$x < -1$ or $x > \dfrac{7}{3}$

$\left\{x \middle| x < -1 \text{ or } x > \dfrac{7}{3}\right\}$ or $(-\infty, -1) \cup \left(\dfrac{7}{3}, \infty\right)$



35. $(6+3i)-(2-4i) = (6-2)+(3-(-4))i = 4+7i$

36. $4(3-i)+3(-5+2i) = 12-4i-15+6i = -3+2i$

37. $\dfrac{3}{3+i} = \dfrac{3}{3+i} \cdot \dfrac{3-i}{3-i} = \dfrac{9-3i}{9-3i+3i-i^2}$

$= \dfrac{9-3i}{10} = \dfrac{9}{10} - \dfrac{3}{10}i$

38. $i^{50} = i^{48} \cdot i^2 = \left(i^4\right)^{12} \cdot i^2 = 1^{12}(-1) = -1$

39. $(2+3i)^3 = (2+3i)^2(2+3i)$

$= \left(4+12i+9i^2\right)(2+3i)$

$= (-5+12i)(2+3i)$

$= -10-15i+24i+36i^2$

$= -46+9i$

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40. $x^2+x+1=0$

$a=1, b=1, c=1,$

$b^2-4ac=1^2-4(1)(1)=1-4=-3$

$x=\dfrac{-1\pm\sqrt{-3}}{2(1)}=\dfrac{-1\pm\sqrt{3}\,i}{2}=-\dfrac{1}{2}\pm\dfrac{\sqrt{3}}{2}i$

The solution set is $\left\{-\dfrac{1}{2}-\dfrac{\sqrt{3}}{2}i,\ -\dfrac{1}{2}+\dfrac{\sqrt{3}}{2}i\right\}$.

41. $2x^2+x-2=0$

$a=2, b=1, c=-2,$

$b^2-4ac=1^2-4(2)(-2)=1+16=17$

$x=\dfrac{-1\pm\sqrt{17}}{2(2)}=\dfrac{-1\pm\sqrt{17}}{4}$

The solution set is $\left\{\dfrac{-1-\sqrt{17}}{4},\ \dfrac{-1+\sqrt{17}}{4}\right\}$.

42. $x^2+3=x$

$x^2-x+3=0$

$a=1, b=-1, c=3,$

$b^2-4ac=(-1)^2-4(1)(3)=1-12=-11$

$x=\dfrac{-(-1)\pm\sqrt{-11}}{2(1)}=\dfrac{1\pm\sqrt{11}\,i}{2}=\dfrac{1}{2}\pm\dfrac{\sqrt{11}}{2}i$

The solution set is $\left\{\dfrac{1}{2}-\dfrac{\sqrt{11}}{2}i,\ \dfrac{1}{2}+\dfrac{\sqrt{11}}{2}i\right\}$.

43. $x(1-x)=6$

$-x^2+x-6=0$

$a=-1, b=1, c=-6,$

$b^2-4ac=1^2-4(-1)(-6)=1-24=-23$

$x=\dfrac{-1\pm\sqrt{-23}}{2(-1)}=\dfrac{-1\pm\sqrt{23}\,i}{-2}=\dfrac{1}{2}\pm\dfrac{\sqrt{23}}{2}i$

The solution set is $\left\{\dfrac{1}{2}-\dfrac{\sqrt{23}}{2}i,\ \dfrac{1}{2}+\dfrac{\sqrt{23}}{2}i\right\}$.

44. $c=50,000+95x$

45. Let x represent the amount of money invested in bonds. Then $70,000-x$ represents the amount of money invested in CD's.
Since the total interest is to be \$5000, we have:

$$0.08x+0.05(70,000-x)=5000$$
$$(100)(0.08x+0.05(70,000-x))=(5000)(100)$$
$$8x+350,000-5x=500,000$$
$$3x+350,000=500,000$$
$$3x=150,000$$
$$x=50,000$$

\$50,000 should be invested in bonds at 8% and \$20,000 should be invested in CD's at 5%.

46. Using $s=vt$, we have $t=3$ and $v=1100$.
Finding the distance s in feet:
$s=1100(3)=3300$
The storm is 3300 feet away.

47. $1600\le I\le 3600$

$$1600\le\frac{900}{x^2}\le 3600$$
$$\frac{1}{1600}\ge\frac{x^2}{900}\ge\frac{1}{3600}$$
$$\frac{9}{16}\ge x^2\ge\frac{1}{4}$$
$$\frac{3}{4}\ge x\ge\frac{1}{2}$$

The range of distances is from 0.5 meters to 0.75 meters, inclusive.

48. Let s represent the distance the plane can travel.

	With wind	Against wind
Rate	$250+30=280$	$250-30=220$
Time	$\dfrac{(s/2)}{280}$	$\dfrac{(s/2)}{220}$
Dist.	$\frac{s}{2}$	$\frac{s}{2}$

Since the total time is at most 5 hours, we have:

$$\frac{(s/2)}{280}+\frac{(s/2)}{220}\le 5$$
$$\frac{s}{560}+\frac{s}{440}\le 5$$
$$11s+14s\le 5(6160)$$
$$25s\le 30,800$$
$$s\le 1232$$

The plane can travel at most 1232 miles or 616 miles one way and return 616 miles.

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49. Let t represent the time it takes the helicopter to reach the raft.

	Raft	Helicopter
Rate	5	90
Time	t	t
Dist.	$5t$	$90t$

Since the total distance is 150 miles, we have:

$5t+90t=150$

$95t=150$

$t\approx 1.58$ hours $\approx$ 1 hour and 35 minutes

The helicopter will reach the raft in about 1 hour and 35 minutes.

50. Given that $s=1280-32t-16t^2$,

a. The object hits the ground when $s=0$.

$0=1280-32t-16t^2$

$t^2+2t-80=0$

$(t+10)(t-8)=0$

$t=-10, t=8$

The object hits the ground after 8 seconds.

b. After 4 seconds, the object's height is

$s=1280-32(4)-16(4)^2=896$ feet.

51. Let t represent the time it takes Clarissa to complete the job by herself.

	Clarissa	Shawna
Time to do job alone	t	$t+5$
Part of job done in 1 day	$\frac{1}{t}$	$\frac{1}{t+5}$
Time on job (days)	6	6
Part of job done by each person	$\frac{6}{t}$	$\frac{6}{t+5}$

Since the two people paint one house, we have:

$\frac{6}{t}+\frac{6}{t+5}=1$

$6(t+5)+6t=t(t+5)$

$6t+30+6t=t^2+5t$

$t^2-7t-30=0$

$(t-10)(t+3)=0$

$t=10$ or $t=-3$

It takes Clarissa 10 days to paint the house when working by herself.

52. Let t represent the time it takes the smaller pump to empty the tank.

	Small Pump	Large Pump
Time to do job alone	t	$t-4$
Part of job done in 1 hr	$\frac{1}{t}$	$\frac{1}{t-4}$
Time on job (hrs)	5	5
Part of job done by each pump	$\frac{5}{t}$	$\frac{5}{t-4}$

Since the two pumps empty one tank, we have:

$\frac{5}{t}+\frac{5}{t-4}=1$

$5(t-4)+5t=t(t-4)$

$5t-20+5t=t^2-4t$

$t^2-14t+20=0$

We can solve this equation for t by using the quadratic formula:

$t=\frac{-(-14)\pm\sqrt{(-14)^2-4(1)(20)}}{2(1)}$

$=\frac{14\pm\sqrt{116}}{2}=\frac{14\pm 2\sqrt{29}}{2}$

$=7\pm\sqrt{29}\approx 7+5.385$

$t=12.385$ or $t=1.615$ (not feasible)

It takes the small pump approximately 12.385 hours (12 hr 23 min) to empty the tank.

53. Let x represent the amount of water added.

% salt	Tot. amt.	amt. of salt
10%	64	$(0.10)(64)$
0%	x	$(0.00)(x)$
2%	$64+x$	$(0.02)(64+x)$

$(0.10)(64)+(0.00)(x)=(0.02)(64+x)$

$6.4=1.28+0.02x$

$5.12=0.02x$

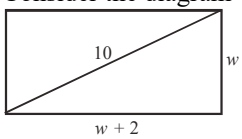
$x=256$

256 ounces of water must be added.

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54. Consider the diagram



By the Pythagorean Theorem we have

$$w^2+(w+2)^2=(10)^2$$
$$w^2+w^2+4w+4=100$$
$$2w^2+4w-96=0$$
$$w^2+2w-48=0$$
$$(w+8)(w-6)=0$$
$$w=-8 \quad \text{or} \quad w=6$$

The width is 6 inches and the length is 6 + 2 = 8 inches.

55. Let x represent the amount of the 15% solution added.

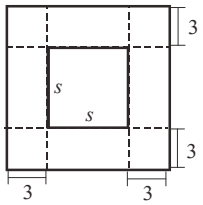
% acid	tot. amt.	amt. of acid
40%	60	$(0.40)(60)$
15%	x	$(0.15)(x)$
25%	$60+x$	$(0.25)(60+x)$

$$(0.40)(60)+(0.15)(x)=(0.25)(60+x)$$
$$24+0.15x=15+0.25x$$
$$9=0.1x$$
$$x=90$$

90 cubic centimeters of the 15% solution must be added, producing 150 cubic centimeters of the 25% solution.

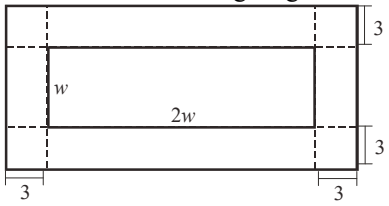
56. a. Consider the following diagram:

$$4(s+6)=50$$
$$4s+24=50$$
$$4s=26$$
$$s=6.5$$



The painting is 6.5 inches by 6.5 inches. $s+6=12.5$, so the frame is 12.5 inches by 12.5 inches.

b. Consider the following diagram:



$$2(2w+6)+2(w+6)=50$$
$$4w+12+2w+12=50$$
$$6w=26$$
$$w=\frac{26}{6}=4\tfrac{1}{3}$$
$$l=2w=8\tfrac{2}{3}$$

The painting is $8\frac{2}{3}$ inches by $4\frac{1}{3}$ inches.

The frame is $14\frac{2}{3}$ inches by $10\frac{1}{3}$ inches.

57. Let x represent the amount Scott receives. Then $\frac{3}{4}x$ represents the amount Alice receives and $\frac{1}{2}x$ represents the amount Tricia receives. The total amount is \$900,000, so we have:

$$x+\frac{3}{4}x+\frac{1}{2}x=900,000$$
$$4\left(x+\frac{3}{4}x+\frac{1}{2}x\right)=4(900,000)$$
$$4x+3x+2x=3,600,000$$
$$9x=3,600,000$$
$$x=400,000$$

So, $\frac{3}{4}x=\frac{3}{4}(400,000)=300,000$ and $\frac{1}{2}x=\frac{1}{2}(400,000)=200,000$.

Scott receives \$400,000, Alice receives \$300,000, and Tricia receives \$200,000.

58. Let t represent the time it takes the older machine to complete the job by itself.

	Old copier	New copier
Time to do job alone	t	$t-1$
Part of job done in 1 hr	$\frac{1}{t}$	$\frac{1}{t-1}$
Time on job (hrs)	1.2	1.2
Part of job done by each copier	$\frac{1.2}{t}$	$\frac{1.2}{t-1}$

Since the two copiers complete one job, we have:

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$$\frac{1.2}{t}+\frac{1.2}{t-1}=1$$
$$1.2(t-1)+1.2t=t(t-1)$$
$$1.2t-1.2+1.2t=t^2-t$$
$$t^2-3.4t+1.2=0$$
$$5t^2-17t+6=0$$
$$(5t-2)(t-3)=0$$
$$t=0.4 \text{ or } t=3$$

It takes the old copier 3 hours to do the job by itself. (0.4 hour is impossible since together it takes 1.2 hours.)

59. Let r_S represent Scott's rate and let r_T represent Todd's rate. The time for Scott to run 95 meters is the same as for Todd to run 100 meters.

$$\frac{95}{r_S}=\frac{100}{r_T}$$
$$r_S=0.95r_T$$
$$d_S=t\cdot r_s=t\left(0.95r_T\right)=0.95d_T$$

If Todd starts from 5 meters behind the start:

$$d_T=105$$
$$d_S=0.95d_T=0.95(105)=99.75$$

a. The race does not end in a tie.

b. Todd wins the race.

c. Todd wins by 0.25 meters.

d. To end in a tie:

$$100=0.95(100+x)$$
$$100=95+0.95x$$
$$5=0.95x$$
$$x\approx 5.26 \text{ meters}$$

e. $95=0.95(100)$ Therefore, the race ends in a tie.

60. We will use the formula for interest, $I=prt$.

Since she owed 27060 at the end of the loan she ad accumulated 3060 in interest and the principal is 24000.

$$I=prt$$
$$3060=(24000)r(3)$$
$$\frac{3060}{3(24000)}=r$$
$$0.0425=r$$

The interest rate is 4.25 %.

Chapter 1 Test

1.
$$\frac{2x}{3}-\frac{x}{2}=\frac{5}{12}$$
$$12\left(\frac{2x}{3}-\frac{x}{2}\right)=12\left(\frac{5}{12}\right)$$
$$8x-6x=5$$
$$2x=5$$
$$x=\frac{5}{2}$$

The solution set is $\left\{\frac{5}{2}\right\}$.

2.
$$x(x-1)=6$$
$$x^2-x=6$$
$$x^2-x-6=0$$
$$(x-3)(x+2)=0$$
$$x-3=0 \text{ or } x+2=0$$
$$x=3 \text{ or } x=-2$$

The solution set is $\{-2, 3\}$.

3.
$$x^4-3x^2-4=0$$
$$\left(x^2-4\right)\left(x^2+1\right)=0$$
$$x^2-4=0 \text{ or } x^2+1=0$$
$$x^2=4 \text{ or } x^2=-1$$
$$x=\pm 2 \text{ or Not real}$$

The solution set is $\{-2, 2\}$.

4.
$$\sqrt{2x-5}+2=4$$
$$\sqrt{2x-5}=2$$
$$\left(\sqrt{2x-5}\right)^2=(2)^2$$
$$2x-5=4$$
$$2x=9$$
$$x=\frac{9}{2}$$

Check: $\sqrt{2\left(\frac{9}{2}\right)-5}+2=4$

$$\sqrt{9-5}+2=4$$
$$\sqrt{4}+2=4$$
$$2+2=4$$
$$4=4$$

The solution set is $\left\{\frac{9}{2}\right\}$.

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5. $|2x-3|+7=10$

$|2x-3|=3$

$2x-3=3 \quad \text{or} \quad 2x-3=-3$

$2x=6 \quad \text{or} \quad 2x=0$

$x=3 \quad \text{or} \quad x=0$

The solutions set is $\{0, 3\}$.

6. $3x^3+2x^2-12x-8=0$

$x^2(3x+2)-4(3x+2)=0$

$(x^2-4)(3x+2)=0$

$(x+2)(x-2)(3x+2)=0$

$x+2=0 \quad \text{or} \quad x-2=0 \quad \text{or} \quad 3x+2=0$

$x=-2 \quad \text{or} \quad x=2 \quad \text{or} \quad x=-\frac{2}{3}$

The solution set is $\left\{-2, -\frac{2}{3}, 2\right\}$.

7. $3x^2-x+1=0$

$x=\frac{-(-1)\pm\sqrt{(-1)^2-4(3)(1)}}{2(3)}$

$=\frac{1\pm\sqrt{-11}}{6}$ (Not real)

This equation has no real solutions.

8. $-3\le\frac{3x-4}{2}\le 6$

$2(-3)\le 2\left(\frac{3x-4}{2}\right)\le 2(6)$

$-6\le 3x-4\le 12$

$-2\le 3x\le 16$

$-\frac{2}{3}\le x\le\frac{16}{3}$

$\left\{x\left|-\frac{2}{3}\le x\le\frac{16}{3}\right.\right\}$ or $\left[-\frac{2}{3}, \frac{16}{3}\right]$



9. $|3x+4|<8$

$-8<3x+4<8$

$-12<3x<4$

$-4<x<\frac{4}{3}$

$\left\{x\left|-4<x<\frac{4}{3}\right.\right\}$ or $\left(-4, \frac{4}{3}\right)$



10. $2+|2x-5|\ge 9$

$|2x-5|\ge 7$

$2x-5\le -7 \quad \text{or} \quad 2x-5\ge 7$

$2x\le -2 \quad \text{or} \quad 2x\ge 12$

$x\le -1 \quad \text{or} \quad x\ge 6$

$\{x|x\le -1 \text{ or } x\ge 6\}$ or $(-\infty,-1]\cup[6,\infty)$.



11. $\frac{-2}{3-i}=\frac{-2}{3-i}\cdot\frac{3+i}{3+i}=\frac{-6-2i}{9+3i-3i-i^2}=\frac{-6-2i}{9-(-1)}$

$=\frac{-6-2i}{10}=\frac{-3-i}{5}=-\frac{3}{5}-\frac{1}{5}i$

12. $4x^2-4x+5=0$

$x=\frac{-(-4)\pm\sqrt{(-4)^2-4(4)(5)}}{2(4)}$

$=\frac{4\pm\sqrt{-64}}{8}=\frac{4\pm 8i}{8}=\frac{1}{2}\pm i$

This solution set is $\left\{\frac{1}{2}-i, \frac{1}{2}+i\right\}$.

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13. Let x represent the amount of the \$8-per-pound coffee.

Amt. of coffee (pounds)	Price (\$)	Total \$
20	4	$(20)(4)$
x	8	$(8)(x)$
$20+x$	5	$(5)(20+x)$

$$80+8x=(5)(20+x)$$
$$80+8x=100+5x$$
$$3x=20$$
$$x=\frac{20}{3}=6\tfrac{2}{3}$$

Add $6\frac{2}{3}$ pounds of \$8/lb coffee to get $26\frac{2}{3}$ pounds of \$5/lb coffee.

Chapter 1 Projects

Project I

Internet-based Project

Project II

1. $T=\dfrac{n}{Cnp+L+M}$, $n=3,\ L=5,\ M=1,\ C=0.2$

$$T=\frac{3}{0.2(3)p+5+1}=\frac{3}{0.6p+6}=\frac{1}{0.2p+2}$$

2. All of the times given in problem 1 were in seconds, so $T=0.1$ board per second needs to used as the value for T in the equation found in problem 1.

$$0.1=\frac{1}{0.2p+2}$$
$$(0.2p+2)(0.1)=1$$
$$0.02p+0.2=1$$
$$0.02p=0.8$$
$$p=40 \text{ parts per board}$$

3. $T=0.15$ board per second

$$0.15=\frac{1}{0.2p+2}$$
$$(0.2p+2)(0.15)=1$$
$$0.03p+0.3=1$$
$$0.03p=0.7$$
$$p\approx 23.3 \text{ parts per board}$$

Thus, only 23 parts per board will work.

For problems 4 – 6, C is requested, so solve for C first:

$$T=\frac{n}{Cnp+L+M}$$
$$(Cnp+L+M)T=n$$
$$CnpT+LT+MT=n$$
$$CnpT=n-LT-MT$$
$$C=\frac{n-LT-MT}{npT}$$

4. $T=0.06,\ n=3,\ p=100,\ M=1,\ L=5$

$$C=\frac{3-5(0.06)-1(0.06)}{3(100)(0.06)}\approx 0.147 \text{ sec}$$

5. $T=0.06,\ n=3,\ p=150,\ M=1,\ L=5$

$$C=\frac{3-5(0.06)-1(0.06)}{3(150)(0.06)}\approx 0.098 \text{ sec}$$

6. $T=0.06,\ n=3,\ p=200,\ M=1,\ L=5$

$$C=\frac{3-5(0.06)-1(0.06)}{3(200)(0.06)}\approx 0.073 \text{ sec}$$

7. As the number of parts per board increases, the tact time decreases, if all the other factors remain constant.

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