Trigonometry 3rd edition Blitzer Solutions Manual

SKU: 9780136921738-SOLUTIONS

INSTRUCTOR'S SOLUTIONS MANUAL

DANIEL S. MILLER

Niagara County Community College

TRIGONOMETRY

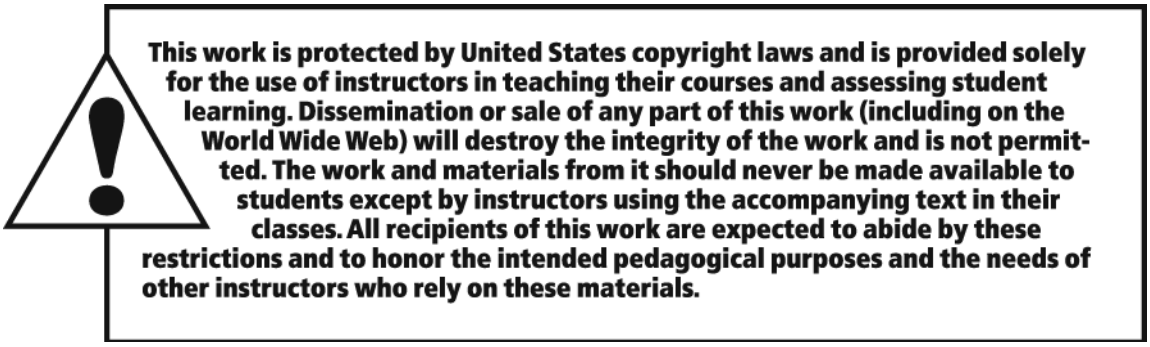
THIRD EDITION

Robert Blitzer

Miami Dade College

Pearson

Trigonometry 3rd edition Blitzer Solutions Manual



The author and publisher of this book have used their best efforts in preparing this book. These efforts include the development, research, and testing of the theories and programs to determine their effectiveness. The author and publisher make no warranty of any kind, expressed or implied, with regard to these programs or the documentation contained in this book. The author and publisher shall not be liable in any event for incidental or consequential damages in connection with, or arising out of, the furnishing, performance, or use of these programs.

Reproduced by Pearson from electronic files supplied by the author.

Copyright © 2022, 2018, 2014 by Pearson Education, Inc. 221 River Street, Hoboken, NJ 07030. All rights reserved.

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording, or otherwise, without the prior written permission of the publisher. Printed in the United States of America.



ISBN-13: 978-0-13-731631-1
ISBN-10: 0-13-731631-3

Trigonometry 3rd edition Blitzer Solutions Manual

TABLE OF CONTENTS for INSTRUCTOR SOLUTIONS

TRIGONOMETRY 3E

Chapter 1	Angles and the Trigonometric Functions	1
Chapter 2	Graphs of the Trigonometric Functions; Inverse Trigonometric Functions	55
Chapter 3	Trigonometric Identities and Equations	183
Chapter 4	Laws of Sines and Cosines; Vectors	309
Chapter 5	Complex Numbers, Polar Coordinates, and Parametric Equations	383

Trigonometry 3rd edition Blitzer Solutions Manual

Trigonometry 3rd edition Blitzer Solutions Manual

Chapter 1
Angles and the Trigonometric Functions

Section 1.1

Check Point Exercises

1. The radian measure of a central angle is the length of the intercepted arc, s, divided by the circle's radius, r. The length of the intercepted arc is 42 feet: $s = 42$ feet. The circle's radius is 12 feet: $r = 12$ feet. Now use the formula for radian measure to find the radian measure of θ.

$$\theta = \frac{s}{r} = \frac{42 \text{ feet}}{12 \text{ feet}} = 3.5$$

Thus, the radian measure of θ is 3.5

2. **a.**
$$60° = 60° \cdot \frac{\pi \text{ radians}}{180°} = \frac{60\pi}{180} \text{ radians} = \frac{\pi}{3} \text{ radians}$$

b.
$$270° = 270° \cdot \frac{\pi \text{ radians}}{180°} = \frac{270\pi}{180} \text{ radians} = \frac{3\pi}{2} \text{ radians}$$

c.
$$-300° = -300° \cdot \frac{\pi \text{ radians}}{180°} = \frac{-300\pi}{180} \text{ radians} = -\frac{5\pi}{3} \text{ radians}$$

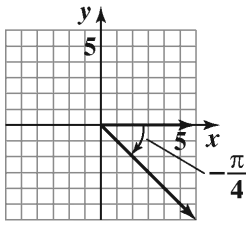
3. **a.**
$$\frac{\pi}{4} \text{ radians} = \frac{\pi \text{ radians}}{4} \cdot \frac{180^{\circ}}{\pi \text{ radians}} = \frac{180^{\circ}}{4} = 45^{\circ}$$

b.
$$-\frac{4\pi}{3} \text{ radians} = -\frac{4\pi \text{ radians}}{3} \cdot \frac{180^{\circ}}{\pi} = -\frac{4 \cdot 180^{\circ}}{3} = -240^{\circ}$$

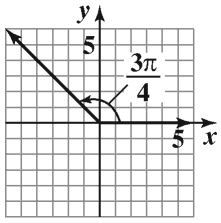
c.
$$6 \text{ radians} = 6 \text{ radians} \cdot \frac{180^{\circ}}{\pi \text{ radians}} = \frac{6 \cdot 180^{\circ}}{\pi} \approx 343.8^{\circ}$$

d.
$$-4.7 \text{ radians} = -4.7 \text{ radians} \cdot \frac{180^{\circ}}{\pi \text{ radians}} = \frac{-4.7 \cdot 180^{\circ}}{\pi} \approx -269.3^{\circ}$$

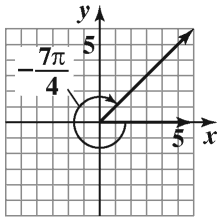
4. **a.**



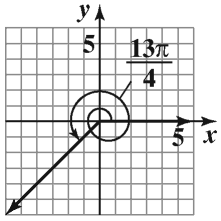
b.



c.



d.



5. **a.** For a 400° angle, subtract 360° to find a positive coterminal angle.
$400° - 360° = 40°$

b. For a –135° angle, add 360° to find a positive coterminal angle.
$-135° + 360° = 225°$

6. **a.**
$$\frac{13\pi}{5} - 2\pi = \frac{13\pi}{5} - \frac{10\pi}{5} = \frac{3\pi}{5}$$

b.
$$-\frac{\pi}{15} + 2\pi = -\frac{\pi}{15} + \frac{30\pi}{15} = \frac{29\pi}{15}$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

7. **a.** $855° - 360° \cdot 2 = 855° - 720° = 135°$

b. $\frac{17\pi}{3} - 2\pi \cdot 2 = \frac{17\pi}{3} - 4\pi$

$= \frac{17\pi}{3} - \frac{12\pi}{3} = \frac{5\pi}{3}$

c. $-\frac{25\pi}{6} + 2\pi \cdot 3 = -\frac{25\pi}{6} + 6\pi$

$= -\frac{25\pi}{6} + \frac{36\pi}{6} = \frac{11\pi}{6}$

d. $17.4 \approx 17.4\left(57^\circ\right) = 991.8^\circ$

For a 991.8° angle, we need to subtract two multiples of 360° to find a positive coterminal angle less than 360°.

$17.4 - 2\pi \cdot 2 = 17.4 - 4\pi \approx 4.8$

8. The formula $s = r\theta$ can only be used when θ is expressed in radians. Thus, we begin by converting $45°$ to radians. Multiply by $\frac{\pi \text{ radians}}{180°}$.

$45° = 45° \cdot \frac{\pi \text{ radians}}{180°} = \frac{45}{180}\pi \text{ radians}$

$= \frac{\pi}{4} \text{ radians}$

Now we can use the formula $s = r\theta$ to find the length of the arc. The circle's radius is 6 inches : $r = 6$ inches. The measure of the central angle in radians is $\frac{\pi}{4} : \theta = \frac{\pi}{4}$. The length of the arc intercepted by this central angle is

$s = r\theta$

$= (6 \text{ inches})\left(\frac{\pi}{4}\right)$

$= \frac{6\pi}{4} \text{ inches}$

$= \frac{3\pi}{2} \text{ inches}$

≈ 4.71 inches.

9. The formula $A = \frac{1}{2}r^2\theta$ can only be used when θ is expressed in radians. Thus, we begin by converting $150°$ to radians. Multiply by $\frac{\pi \text{ radians}}{180°}$.

$150° = 150° \cdot \frac{\pi \text{ radians}}{180°}$

$= \frac{150}{180}\pi \text{ radians}$

$= \frac{5\pi}{6} \text{ radians}$

The circle's radius is 6 feet.

Now use the formula $A = \frac{1}{2}r^2\theta$ to find the area of the sector.:

$A = \frac{1}{2}r^2\theta$

$= \frac{1}{2}(6 \text{ feet})^2\left(\frac{5\pi}{6}\right)$

$= 15\pi$ square feet

≈ 47.12 square feet

10. We are given ω, the angular speed.

$\omega = 45$ revolutions per minute

We use the formula $v = r\omega$ to find v, the linear speed. Before applying the formula, we must express ω in radians per minute.

$\omega = \frac{45 \text{ revolutions}}{1 \text{ minute}} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}}$

$= \frac{90\pi \text{ radians}}{1 \text{ minute}}$

The angular speed of the propeller is 90π radians per minute. The linear speed is

$v = r\omega$

$= 1.5 \text{ inches} \cdot \frac{90\pi}{1 \text{ minute}}$

$= \frac{135\pi \text{ inches}}{\text{minute}}$

$= 135\pi \frac{\text{inches}}{\text{minute}}$

$\approx 424 \frac{\text{inches}}{\text{minute}}$

The linear speed is 135π inches per minute, which is approximately 424 inches per minute.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

Concept and Vocabulary Check 1.1

C1. origin; x-axis

C2. counterclockwise; clockwise

C3. acute; right; obtuse; straight

C4. $\frac{s}{r}$

C5. $\frac{\pi}{180^\circ}$

C6. $\frac{180^\circ}{\pi}$

C7. coterminal; 360°; 2π

C8. $r\theta$

C9. $\frac{1}{2}r^2\theta$

C10. false

C11. $r\omega$; angular

Exercise Set 1.1

1. obtuse

2. obtuse

3. acute

4. acute

5. straight

6. right

7. $\theta = \frac{s}{r} = \frac{40 \text{ inches}}{10 \text{ inches}} = 4$ radians

8. $\theta = \frac{s}{r} = \frac{30 \text{ feet}}{5 \text{ feet}} = 6$ radians

9. $\theta = \frac{s}{r} = \frac{8 \text{ yards}}{6 \text{ yards}} = \frac{4}{3}$ radians

10. $\theta = \frac{s}{r} = \frac{18 \text{ yards}}{8 \text{ yards}} = 2.25$ radians

11. $\theta = \frac{s}{r} = \frac{400 \text{ centimeters}}{100 \text{ centimeters}} = 4$ radians

12. $\theta = \frac{s}{r} = \frac{600 \text{ centimeters}}{100 \text{ centimeters}} = 6$ radians

13. $45^\circ = 45^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{45\pi}{180} \text{ radians} = \frac{\pi}{4} \text{ radians}$

14. $18^\circ = 18^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{18\pi}{180} \text{ radians} = \frac{\pi}{10} \text{ radians}$

15. $135^\circ = 135^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{135\pi}{180} \text{ radians} = \frac{3\pi}{4} \text{ radians}$

16. $150^\circ = 150^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{150\pi}{180} \text{ radians} = \frac{5\pi}{6} \text{ radians}$

17. $300^\circ = 300^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{300\pi}{180} \text{ radians} = \frac{5\pi}{3} \text{ radians}$

18. $330^\circ = 330^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{330\pi}{180} \text{ radians} = \frac{11\pi}{6} \text{ radians}$

19. $-225^\circ = -225^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = -\frac{225\pi}{180} \text{ radians} = -\frac{5\pi}{4} \text{ radians}$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

20. $$-270^\circ = -270^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = -\frac{270\pi}{180} \text{ radians} = -\frac{3\pi}{2} \text{ radians}$$

21. $$\frac{\pi}{2} \text{ radians} = \frac{\pi \text{ radians}}{2} \cdot \frac{180^\circ}{\pi \text{ radians}} = \frac{180^\circ}{2} = 90^\circ$$

22. $$\frac{\pi}{9} \text{ radians} = \frac{\pi \text{ radians}}{9} \cdot \frac{180^\circ}{\pi \text{ radians}} = \frac{180^\circ}{9} = 20^\circ$$

23. $$\frac{2\pi}{3} \text{ radians} = \frac{2\pi \text{ radians}}{3} \cdot \frac{180^\circ}{\pi \text{ radians}} = \frac{2 \cdot 180^\circ}{3} = 120^\circ$$

24. $$\frac{3\pi \text{ radians}}{4} \cdot \frac{180^0}{\pi \text{ radians}} = \frac{3 \cdot 180^\circ}{4} = 135^\circ$$

25. $$\frac{7\pi}{6} \text{ radians} = \frac{7\pi \text{ radians}}{6} \cdot \frac{180^\circ}{\pi \text{ radians}} = \frac{7 \cdot 180^\circ}{6} = 210^\circ$$

26. $$\frac{11\pi \text{ radians}}{6} \cdot \frac{180^\circ}{\pi \text{ radians}} = \frac{11 \cdot 180^\circ}{6} = 330^\circ$$

27. $$-3\pi \text{ radians} = -3\pi \text{ radians} \cdot \frac{180^\circ}{\pi \text{ radians}} = -3 \cdot 180^\circ = -540^\circ$$

28. $$-4\pi \text{ radians} \cdot \frac{180^\circ}{\pi \text{ radians}} = -4 \cdot 180^\circ = -720^\circ$$

29. $$18^\circ = 18^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{18\pi}{180} \text{ radians} \approx 0.31 \text{ radians}$$

30. $$76^\circ = 76^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{76\pi}{180} \text{ radians} \approx 1.33 \text{ radians}$$

31. $$-40^\circ = -40^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = -\frac{40\pi}{180} \text{ radians} \approx -0.70 \text{ radians}$$

32. $$-50^\circ = -50^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = -\frac{50\pi}{180} \text{ radians} \approx -0.87 \text{ radians}$$

33. $$200^\circ = 200^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{200\pi}{180} \text{ radians} \approx 3.49 \text{ radians}$$

34. $$250^\circ = 250^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{250\pi}{180} \text{ radians} \approx 4.36 \text{ radians}$$

35. $$2 \text{ radians} = 2 \text{ radians} \cdot \frac{180^\circ}{\pi \text{ radians}} = \frac{2 \cdot 180^\circ}{\pi} \approx 114.59^\circ$$

36. $$3 \text{ radians} \cdot \frac{180^\circ}{\pi \text{ radians}} = \frac{3 \cdot 180^\circ}{\pi} \approx 171.89^\circ$$

37. $$\frac{\pi}{13} \text{ radians} = \frac{\pi \text{ radians}}{13} \cdot \frac{180^\circ}{\pi \text{ radians}} = \frac{180^\circ}{13} \approx 13.85^\circ$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

38. $\frac{\pi}{17}\text{radians}\cdot\frac{180^{\circ}}{\pi\text{radians}}=\frac{180^{\circ}}{17}\approx 10.59^{\circ}$

39. $-4.8\ \text{radians}=-4.8\ \text{radians}\cdot\frac{180^{\circ}}{\pi\ \text{radians}}$

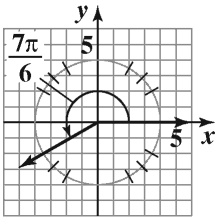
$$=\frac{-4.8\cdot 180^{\circ}}{\pi}$$

$$\approx -275.02^{\circ}$$

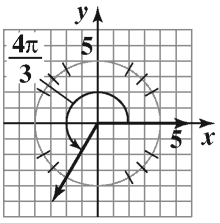
40. $-5.2\ \text{radians}\cdot\frac{180^{\circ}}{\pi\text{radians}}=\frac{-5.2\cdot 180^{\circ}}{\pi}$

$$\approx -297.94^{\circ}$$

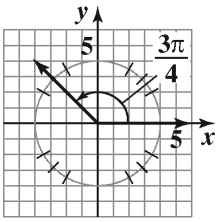
41.



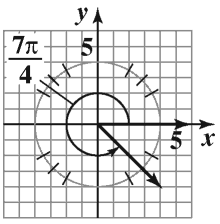
42.



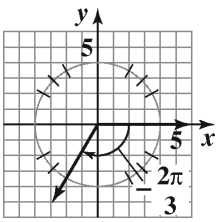
43.



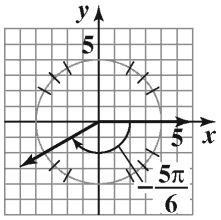
44.



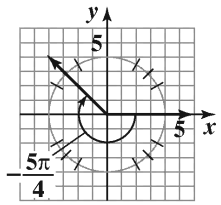
45.



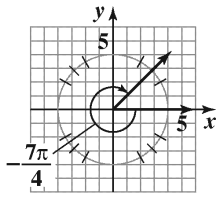
46.



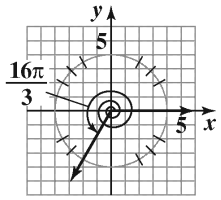
47.



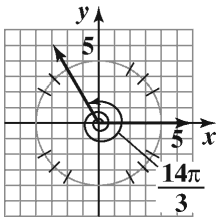
48.



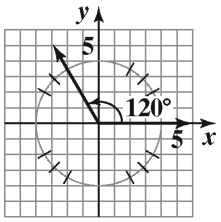
49.



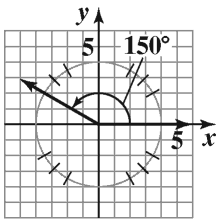
50.



51.



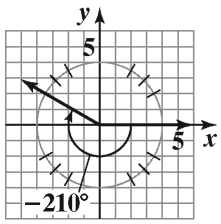
52.



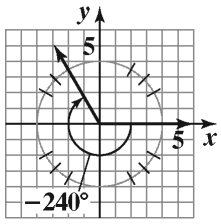
Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

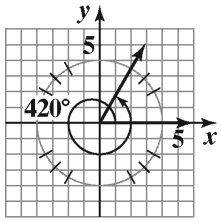
53.



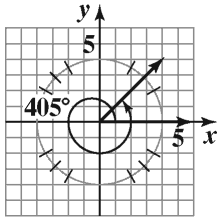
54.



55.



56.



57. $395^\circ - 360^\circ = 35^\circ$

58. $415^\circ - 360^\circ = 55^\circ$

59. $-150^\circ + 360^\circ = 210^\circ$

60. $-160^\circ + 360^\circ = 200^\circ$

61. $-765^\circ + 360^\circ \cdot 3 = -765^\circ + 1080^\circ = 315^\circ$

62. $-760^\circ + 360^\circ \cdot 3 = -760^\circ + 1080^\circ = 320^\circ$

63. $\frac{19\pi}{6} - 2\pi = \frac{19\pi}{6} - \frac{12\pi}{6} = \frac{7\pi}{6}$

64. $\frac{17\pi}{5} - 2\pi = \frac{17\pi}{5} - \frac{10\pi}{5} = \frac{7\pi}{5}$

65. $\frac{23\pi}{5} - 2\pi \cdot 2 = \frac{23\pi}{5} - 4\pi = \frac{23\pi}{5} - \frac{20\pi}{5} = \frac{3\pi}{5}$

66. $\frac{25\pi}{6} - 2\pi \cdot 2 = \frac{25\pi}{6} - 4\pi = \frac{25\pi}{6} - \frac{24\pi}{6} = \frac{\pi}{6}$

67. $-\frac{\pi}{50} + 2\pi = -\frac{\pi}{50} + \frac{100\pi}{50} = \frac{99\pi}{50}$

68. $-\frac{\pi}{40} + 2\pi = -\frac{\pi}{40} + \frac{80\pi}{40} = \frac{79\pi}{40}$

69. $-\frac{31\pi}{7} + 2\pi \cdot 3 = -\frac{31\pi}{7} + 6\pi$

$= -\frac{31\pi}{7} + \frac{42\pi}{7} = \frac{11\pi}{7}$

70. $-\frac{38\pi}{9} + 2\pi \cdot 3 = -\frac{38\pi}{9} + 6\pi = -\frac{38\pi}{9} + \frac{54\pi}{9} = \frac{16\pi}{9}$

71. $r = 12$ inches, $\theta = 45^\circ$

Begin by converting 45° to radians, in order to use the formula $s = r\theta$.

$45^\circ = 45^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{\pi}{4}$ radians

Now use the formula $s = r\theta$.

$s = r\theta = 12 \cdot \frac{\pi}{4} = 3\pi$ inches ≈ 9.42 inches

72. $r = 16$ inches, $\theta = 60^\circ$

Begin by converting 60° to radians, in order to use the formula $s = r\theta$.

$60^\circ = 60^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{\pi}{3}$ radians

Now use the formula $s = r\theta$.

$s = r\theta = 16 \cdot \frac{\pi}{3} = \frac{16\pi}{3}$ inches ≈ 16.76 inches

73. $r = 8$ feet, $\theta = 225^\circ$

Begin by converting 225° to radians, in order to use the formula $s = r\theta$.

$225^\circ = 225^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{5\pi}{4}$ radians

Now use the formula $s = r\theta$.

$s = r\theta = 8 \cdot \frac{5\pi}{4} = 10\pi$ feet ≈ 31.42 feet

74. $r = 9$ yards, $\theta = 315^\circ$

Begin by converting 315° to radians, in order to use the formula $s = r\theta$.

$315^\circ = 315^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{7\pi}{4}$ radians

Now use the formula $s = r\theta$.

$s = r\theta = 9 \cdot \frac{7\pi}{4} = \frac{63\pi}{4}$ yards ≈ 49.48 yards

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

75. Begin by converting the angle to radians.

$$18^\circ = 18^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{\pi}{10} \text{ radians}$$

Now use the formula $A = \frac{1}{2}r^2\theta$ to find the area of the sector.:

$$A = \tfrac{1}{2}r^2\theta$$

$$= \tfrac{1}{2}(10 \text{ meters})^2\left(\frac{\pi}{10}\right)$$

$$= 5\pi \text{ square meters}$$

$$\approx 15.71 \text{ square meters}$$

76. Begin by converting the angle to radians.

$$15^\circ = 15^\circ \cdot \frac{\pi \text{ radians}}{180^\circ}$$

$$= \frac{\pi}{12} \text{ radians}$$

Now use the formula $A = \frac{1}{2}r^2\theta$ to find the area of the sector.:

$$A = \tfrac{1}{2}r^2\theta$$

$$= \tfrac{1}{2}(6 \text{ yards})^2\left(\frac{\pi}{12}\right)$$

$$= \frac{3\pi}{2} \text{ square yards}$$

$$\approx 4.71 \text{ square yards}$$

77. Begin by converting the angle to radians.

$$240^\circ = 240^\circ \cdot \frac{\pi \text{ radians}}{180^\circ}$$

$$= \frac{4\pi}{3} \text{ radians}$$

Now use the formula $A = \frac{1}{2}r^2\theta$ to find the area of the sector.:

$$A = \tfrac{1}{2}r^2\theta$$

$$= \tfrac{1}{2}(4 \text{ inches})^2\left(\frac{4\pi}{3}\right)$$

$$= \frac{32\pi}{3} \text{ square inches}$$

$$\approx 33.51 \text{ square inches}$$

78. Begin by converting the angle to radians.

$$330^\circ = 330^\circ \cdot \frac{\pi \text{ radians}}{180^\circ}$$

$$= \frac{11\pi}{6} \text{ radians}$$

Now use the formula $A = \frac{1}{2}r^2\theta$ to find the area of the sector.:

$$A = \tfrac{1}{2}r^2\theta$$

$$= \tfrac{1}{2}(3 \text{ inches})^2\left(\frac{11\pi}{6}\right)$$

$$= \frac{33\pi}{4} \text{ square inches}$$

$$\approx 25.92 \text{ square inches}$$

79. 6 revolutions per second

$$= \frac{6 \text{ revolutions}}{1 \text{ second}} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolutions}} = \frac{12\pi \text{ radians}}{1 \text{ seconds}}$$
$$= 12\pi \text{ radians per second}$$

80. 20 revolutions per second

$$= \frac{20 \text{ revolutions}}{1 \text{ second}} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}} = \frac{40\pi \text{ radians}}{1 \text{ second}}$$
$$= 40\pi \text{ radians per second}$$

81. $-\frac{4\pi}{3}$ and $\frac{2\pi}{3}$

82. $-\frac{7\pi}{6}$ and $\frac{5\pi}{6}$

83. $-\frac{3\pi}{4}$ and $\frac{5\pi}{4}$

84. $-\frac{\pi}{4}$ and $\frac{7\pi}{4}$

85. $-\frac{\pi}{2}$ and $\frac{3\pi}{2}$

86. $-\pi$ and π

87. $\frac{55}{60} \cdot 2\pi = \frac{11\pi}{6}$

88. $\frac{35}{60} \cdot 2\pi = \frac{7\pi}{6}$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

89. 3 minutes and 40 seconds equals 220 seconds.

$$\frac{220}{60}\cdot 2\pi = \frac{22\pi}{3}$$

90. 4 minutes and 25 seconds equals 265 seconds.

$$\frac{265}{60}\cdot 2\pi = \frac{53\pi}{6}$$

91.
$$A = \tfrac{1}{2}r^2\theta$$

$$25 \text{ square feet} = \tfrac{1}{2}(10 \text{ feet})^2\theta$$

$$\frac{25 \text{ square feet}}{\frac{1}{2}(10 \text{ feet})^2} = \theta$$

$$\frac{25}{50} = \theta$$

$$\theta = \frac{1}{2} \text{ radians}$$

92.
$$A = \tfrac{1}{2}r^2\theta$$

$$36 \text{ square yards} = \tfrac{1}{2}(6 \text{ yards})^2\theta$$

$$\frac{36 \text{ square yards}}{\frac{1}{2}(6 \text{ yards})^2} = \theta$$

$$\frac{36}{18} = \theta$$

$$\theta = 2 \text{ radians}$$

93. First, convert to degrees.

$$\frac{1}{6} \text{ revolution} = \frac{1}{6} \text{ revolution}\cdot\frac{360^\circ}{1 \text{ revolution}}$$

$$= \frac{1}{6}\cdot 360^\circ = 60^\circ$$

Now, convert 60° to radians.

$$60^\circ = 60^\circ\cdot\frac{\pi \text{ radians}}{180^\circ} = \frac{60\pi}{180} \text{ radians}$$

$$= \frac{\pi}{3} \text{ radians}$$

Therefore, $\frac{1}{6}$ revolution is equivalent to 60° or $\frac{\pi}{3}$ radians.

94. First, convert to degrees.

$$\frac{1}{3}\text{revolutions} = \frac{1}{3} \text{ revolutions}\cdot\frac{360^\circ}{1 \text{ revolution}}$$

$$= \frac{1}{3}\cdot 360^\circ = 120^\circ$$

Now, convert 120° to radians.

$$120^\circ = 120^\circ\cdot\frac{\pi \text{ radians}}{180^\circ} = \frac{120\pi}{180} \text{ radians} = \frac{2\pi}{3} \text{ radians}$$

Therefore, $\frac{1}{3}$ revolution is equivalent to 120° or $\frac{2\pi}{3}$ radians.

95. The distance that the tip of the minute hand moves is given by its arc length, *s*. Since $s = r\theta$, we begin by finding *r* and θ. We are given that *r* = 8 inches. The minute hand moves from 12 to 2 o'clock, or $\frac{1}{6}$ of a complete revolution. The formula $s = r\theta$ can only be used when θ is expressed in radians. We must convert $\frac{1}{6}$ revolution to radians.

$$\frac{1}{6} \text{ revolution} = \frac{1}{6} \text{ revolution}\cdot\frac{2\pi \text{ radians}}{1 \text{ revolution}}$$

$$= \frac{\pi}{3} \text{ radians}$$

The distance the tip of the minute hand moves is

$$s = r\theta = (8 \text{ inches})\left(\frac{\pi}{3}\right) = \frac{8\pi}{3} \text{ inches} \approx 8.38 \text{ inches}.$$

96. The distance that the tip of the minute hand moves is given by its arc length, *s*. Since $s = r\theta$, we begin by finding *r* and θ. We are given that *r* = 6 inches. The minute hand moves from 12 to 4 o'clock, or $\frac{1}{3}$ of a complete revolution. The formula $s = r\theta$ can only be used when θ is expressed in radians. We must convert $\frac{1}{3}$ revolution to radians.

$$\frac{1}{3} \text{ revolution} = \frac{1}{3}\text{revolution}\cdot\frac{2\pi \text{ radians}}{1 \text{ revolution}}$$

$$= \frac{2\pi}{3} \text{ radians}$$

The distance the tip of the minute hand moves is

$$s = r\theta = (6 \text{ inches})\left(\frac{2\pi}{3}\right) = \frac{12\pi}{3} \text{ inches}$$

$$= 4\pi \text{ inches} \approx 12.57 \text{ inches}.$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

97. The length of each arc is given by $s = r\theta$. We are given that $r = 24$ inches and $\theta = 90°$. The formula $s = r\theta$ can only be used when θ is expressed in radians.

$$90° = 90° \cdot \frac{\pi \text{ radians}}{180°} = \frac{90\pi}{180} \text{ radians}$$
$$= \frac{\pi}{2} \text{ radians}$$

The length of each arc is

$$s = r\theta = (24 \text{ inches})\left(\frac{\pi}{2}\right) = 12\pi \text{ inches}$$
$$\approx 37.70 \text{ inches.}$$

98. The distance that the wheel moves is given by $s = r\theta$. We are given that $r = 80$ centimeters and $\theta = 60°$. The formula $s = r\theta$ can only be used when θ is expressed in radians.

$$60° = 60° \cdot \frac{\pi \text{ radians}}{180°} = \frac{60\pi}{180} \text{ radians}$$
$$= \frac{\pi}{3} \text{ radians}$$

The length that the wheel moves is

$$s = r\theta = (80 \text{ centimeters})\left(\frac{\pi}{3}\right) = \frac{80\pi}{3} \text{ centimeters}$$
$$\approx 83.78 \text{ centimeters.}$$

99. Begin by converting the angle to radians.

$$135° = 135° \cdot \frac{\pi \text{ radians}}{180°}$$
$$= \frac{3\pi}{4} \text{ radians}$$

Now use the formula $A = \frac{1}{2}r^2\theta$ to find the area of the sector.:

$$A = \tfrac{1}{2}r^2\theta$$
$$= \tfrac{1}{2}(40 \text{ feet})^2\left(\frac{3\pi}{4}\right)$$
$$= 600\pi \text{ square feet}$$
$$\approx 1884.96 \text{ square feet}$$

100. Begin by converting the angle to radians.

$$120° = 120° \cdot \frac{\pi \text{ radians}}{180°}$$
$$= \frac{2\pi}{3} \text{ radians}$$

Now use the formula $A = \frac{1}{2}r^2\theta$ to find the area of the sector.:

$$A = \tfrac{1}{2}r^2\theta$$
$$= \tfrac{1}{2}(30 \text{ feet})^2\left(\frac{2\pi}{3}\right)$$
$$= 300\pi \text{ square feet}$$
$$\approx 942.48 \text{ square feet}$$

101. Recall that $\theta = \frac{s}{r}$. We are given that $s = 8000$ miles and $r = 4000$ miles.

$$\theta = \frac{s}{r} = \frac{8000 \text{ miles}}{4000 \text{ miles}} = 2 \text{ radians}$$

Now, convert 2 radians to degrees.

$$2 \text{ radians} = 2 \text{ radians} \cdot \frac{180^{\text{o}}}{\pi \text{ radians}} \approx 114.59^{\text{o}}$$

102. Recall that $\theta = \frac{s}{r}$. We are given that $s = 10{,}000$ miles and $r = 4000$ miles.

$$\theta = \frac{s}{r} = \frac{10{,}000 \text{ miles}}{4000 \text{ miles}} = 2.5 \text{ radians}$$

Now, convert 2.5 radians to degrees.

$$2.5 \text{ radians} \cdot \frac{180^{\text{o}}}{2\pi \text{ radians}} \approx 143.24^{\text{o}}$$

103. Recall that $s = r\theta$. We are given that $r = 4000$ miles and $\theta = 30°$. The formula $s = r\theta$ can only be used when θ is expressed in radians.

$$30° = 30° \cdot \frac{\pi \text{ radians}}{180°} = \frac{30\pi}{180} \text{ radians}$$
$$= \frac{\pi}{6} \text{ radians}$$
$$s = r\theta = (4000 \text{ miles})\left(\frac{\pi}{6}\right) \approx 2094 \text{ miles}$$

To the nearest mile, the distance from A to B is 2094 miles.

104. Recall that $s = r\theta$. We are given that $r = 4000$ miles and $\theta = 10°$. We can only use the formula $s = r\theta$ when θ is expressed in radians.

$$10° = 10° \cdot \frac{\pi \text{ radians}}{180°} = \frac{10\pi}{180} \text{ radians}$$
$$= \frac{\pi}{18} \text{ radians}$$
$$s = r\theta = (4000 \text{ miles})\left(\frac{\pi}{18}\right) \approx 698 \text{ miles}$$

To the nearest mile, the distance from A to B is 698 miles.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

105. Linear speed is given by $v = r\omega$. We are given that $\omega = \frac{\pi}{12}$ radians per hour and $r = 4000$ miles. Therefore,

$$v = r\omega = (4000 \text{ miles})\left(\frac{\pi}{12}\right)$$
$$= \frac{4000\pi}{12} \text{ miles per hour}$$
$$\approx 1047 \text{ miles per hour}$$

The linear speed is about 1047 miles per hour.

106. Linear speed is given by $v = r\omega$. We are given that $r = 25$ feet and the wheel rotates at 2 revolutions per minute. We need to convert 2 revolutions per minute to radians per minute.

2 revolutions per minute

$$= 2 \text{ revolutions per minute} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}}$$
$$= 4\pi \text{ radians per minute}$$
$$v = r\omega = (25 \text{ feet})(4\pi) \approx 314 \text{ feet per minute}$$

The linear speed of the Ferris wheel is about 314 feet per minute.

107. Linear speed is given by $v = r\omega$. We are given that $r = 12$ feet and the wheel rotates at 20 revolutions per minute.

20 revolutions per minute

$$= 20 \text{ revolutions per minute} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}}$$
$$= 40\pi \text{ radians per minute}$$
$$v = r\omega = (12 \text{ feet})(40\pi)$$
$$\approx 1508 \text{ feet per minute}$$

The linear speed of the wheel is about 1508 feet per minute.

108. Begin by converting 2.5 revolutions per minute to radians per minute.

2.5 revolutions per minute

$$= 2.5 \text{ revolutions per minute} \cdot \frac{2\pi \text{ radians}}{1 \text{ revolution}}$$
$$= 5\pi \text{ radians per minute}$$

The linear speed of the animals in the outer rows is

$$v = r\omega = (20 \text{ feet})(5\pi) \approx 100 \text{ feet per minute}$$

The linear speed of the animals in the inner rows is

$$v = r\omega = (10 \text{ feet})(5\pi) \approx 50 \text{ feet per minute}$$

The difference is $100\pi - 50\pi = 50\pi$ feet per minute or about 157 feet per minute.

109. – 121. Answers may vary.

122. $30^\circ 15'10'' = 30.25^\circ$

123. $65^\circ 45'20'' = 65.76^\circ$

124. $30.42^\circ = 30^\circ 25'12''$

125. $50.42^\circ = 50^\circ 25'12''$

126. does not make sense; Explanations will vary. Sample explanation: Angles greater than π will exceed a straight angle.

127. does not make sense; Explanations will vary. Sample explanation: It is possible for π to be used in an angle measured using degrees.

128. makes sense

129. does not make sense; Explanations will vary. Sample explanation: That will not be possible if the angle is a multiple of 2π.

130. A right angle measures 90° and

$$90^\circ = \frac{\pi}{2} \text{ radians} \approx 1.57 \text{ radians}.$$

If $\theta = \frac{3}{2}$ radians $= 1.5$ radians, θ is smaller than a right angle.

131. $s = r\theta$

Begin by changing $\theta = 20^\circ$ to radians.

$$20^\circ = 20^\circ \cdot \frac{\pi}{180^\circ} = \frac{\pi}{9} \text{ radians}$$
$$100 = \frac{\pi}{9} r$$
$$r = \frac{900}{\pi} \approx 286 \text{ miles}$$

To the nearest mile, a radius of 286 miles should be used.

132.
$$A = \tfrac{1}{2} r^2 \theta$$
$$700 \text{ square feet} = \tfrac{1}{2}(30 \text{ feet})^2 \theta$$
$$\frac{700 \text{ square feet}}{\frac{1}{2}(30 \text{ feet})^2} = \theta$$
$$\frac{700}{450} = \theta$$
$$\theta = \frac{14}{9} \text{ radians}$$

Covvert radians to degrees:

$$\frac{14}{9} \text{ radians} = \frac{14}{9} \cdot \frac{180^\circ}{\pi} \approx 89^\circ$$

The sprinkler should rotate about 89°.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

133. $s = r\theta$

Begin by changing $\theta = 26°$ to radians.

$$26° = 26° \cdot \frac{\pi}{180°} = \frac{13\pi}{90} \text{ radians}$$

$$s = 4000 \cdot \frac{13\pi}{90}$$
$$\approx 1815 \text{ miles}$$

To the nearest mile, Miami, Florida is 1815 miles north of the equator.

134. First find the hypotenuse.

$$c^2 = a^2 + b^2$$
$$c^2 = 5^2 + 12^2$$
$$c^2 = 25 + 144$$
$$c^2 = 169$$
$$c = 13$$

Next write the ratio.

$$\frac{a}{c} = \frac{5}{13}$$

135. First find the hypotenuse.

$$c^2 = a^2 + b^2$$
$$c^2 = 1^2 + 1^2$$
$$c^2 = 1 + 1$$
$$c^2 = 2$$
$$c = \sqrt{2}$$

Next write the ratio and simplify.

$$\frac{a}{c} = \frac{1}{\sqrt{2}}$$
$$= \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}}$$
$$= \frac{\sqrt{2}}{2}$$

136. $\left(\frac{a}{c}\right)^2 + \left(\frac{b}{c}\right)^2 = \frac{a^2}{c^2} + \frac{b^2}{c^2}$

$$= \frac{a^2 + b^2}{c^2}$$

Since $c^2 = a^2 + b^2$, continue simplifying by substituting c^2 for $a^2 + b^2$ which gives 1.

Section 1.2

Check Point Exercises

1. Use the Pythagorean Theorem, $c^2 = a^2 + b^2$, to find c.

$$a = 3, b = 4$$
$$c^2 = a^2 + b^2 = 3^2 + 4^2 = 9 + 16 = 25$$
$$c = \sqrt{25} = 5$$

Referring to these lengths as opposite, adjacent, and hypotenuse, we have

$$\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{3}{5}$$
$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{4}{5}$$
$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{3}{4}$$
$$\csc\theta = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{5}{3}$$
$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{5}{4}$$
$$\cot\theta = \frac{\text{adjacent}}{\text{opposite}} = \frac{4}{3}$$

2. Use the Pythagorean Theorem, $c^2 = a^2 + b^2$, to find b.

$$a^2 + b^2 = c^2$$
$$1^2 + b^2 = 5^2$$
$$1 + b^2 = 25$$
$$b^2 = 24$$
$$b = \sqrt{24} = 2\sqrt{6}$$

Note that side a is opposite θ and side b is adjacent to θ.

$$\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{1}{5}$$
$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{2\sqrt{6}}{5}$$
$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{1}{2\sqrt{6}} = \frac{\sqrt{6}}{12}$$
$$\csc\theta = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{5}{1} = 5$$
$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{5}{2\sqrt{6}} = \frac{5\sqrt{6}}{12}$$
$$\cot\theta = \frac{\text{adjacent}}{\text{opposite}} = \frac{2\sqrt{6}}{1} = 2\sqrt{6}$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

3. Apply the definitions of these three trigonometric functions.

$$\csc 45° = \frac{\text{length of hypotenuse}}{\text{length of side opposite } 45°}$$
$$= \frac{\sqrt{2}}{1} = \sqrt{2}$$
$$\sec 45° = \frac{\text{length of hypotenuse}}{\text{length of side adjacent to } 45°}$$
$$= \frac{\sqrt{2}}{1} = \sqrt{2}$$
$$\cot 45° = \frac{\text{length of side adjacent to } 45°}{\text{length of side opposite } 45°}$$
$$= \frac{1}{1} = 1$$

4.
$$\tan 60° = \frac{\text{length of side opposite } 60°}{\text{length of side adjacent to } 60°}$$
$$= \frac{\sqrt{3}}{1} = \sqrt{3}$$
$$\tan 30° = \frac{\text{length of side opposite } 30°}{\text{length of side adjacent to } 30°}$$
$$= \frac{1}{\sqrt{3}} = \frac{1}{\sqrt{3}} \cdot \frac{\sqrt{3}}{3} = \frac{\sqrt{3}}{3}$$

5.
$$\tan\theta = \frac{\sin\theta}{\cos\theta} = \frac{\frac{2}{3}}{\frac{\sqrt{5}}{3}}$$
$$= \frac{2}{3} \cdot \frac{3}{\sqrt{5}} = \frac{2}{\sqrt{5}}$$
$$= \frac{2}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{2\sqrt{5}}{5}$$

$$\csc\theta = \frac{1}{\sin\theta} = \frac{1}{\frac{2}{3}} = \frac{3}{2}$$
$$\sec\theta = \frac{1}{\cos\theta} = \frac{1}{\frac{\sqrt{5}}{3}} = \frac{3}{\sqrt{5}}$$
$$= \frac{3}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{3\sqrt{5}}{5}$$
$$\cot\theta = \frac{1}{\tan\theta} = \frac{1}{\frac{2}{\sqrt{5}}} = \frac{\sqrt{5}}{2}$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

6. We can find the value of $\cos\theta$ by using the Pythagorean identity.

$$\sin^2\theta+\cos^2\theta=1$$
$$\left(\frac{1}{2}\right)^2+\cos^2\theta=1$$
$$\frac{1}{4}+\cos^2\theta=1$$
$$\cos^2\theta=1-\frac{1}{4}$$
$$\cos^2\theta=\frac{3}{4}$$
$$\cos\theta=\sqrt{\frac{3}{4}}=\frac{\sqrt{3}}{2}$$

7. **a.** $\sin 46^\circ=\cos(90^\circ-46^\circ)=\cos 44^\circ$

b.
$$\cot\frac{\pi}{12}=\tan\left(\frac{\pi}{2}-\frac{\pi}{12}\right)$$
$$=\tan\left(\frac{6\pi}{12}-\frac{\pi}{12}\right)$$
$$=\tan\frac{5\pi}{12}$$

8.

	Many Scientific Calculators			
	Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
a.	sin 72.8°	Degree	72.8 SIN	0.9553
b.	csc 1.5	Radian	1.5 SIN 1/*x*	1.0025

	Many Graphing Calculators			
	Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
a.	sin 72.8°	Degree	SIN 72.8 ENTER	0.9553
b.	csc 1.5	Radian	(SIN 1.5) x^{-1} ENTER	1.0025

9. Because we have a known angle, an unknown opposite side, and a known adjacent side, we select the tangent function.

$$\tan 24^\circ=\frac{a}{750}$$
$$a=750\tan 24^\circ$$
$$a\approx 750(0.4452)\approx 333.9$$

The distance across the lake is approximately 333.9 yards.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

10. $\tan\theta = \dfrac{\text{side opposite}}{\text{side adjacent}} = \dfrac{14}{10}$

Use a calculator in degree mode to find θ.

Many Scientific Calculators	Many Graphing Calculators
$\boxed{\text{TAN}^{-1}}\ \boxed{(}\ 14\ \boxed{\div}\ 10\ \boxed{)}\ \boxed{\text{ENTER}}$	$\boxed{\text{TAN}}\ \boxed{(}\ 14\ \div\ 10\ \boxed{)}\ \boxed{\text{ENTER}}$

The display should show approximately 54. Thus, the angle of elevation of the sun is approximately 54°.

Concept and Vocabulary Check 1.2

C1. $\sin\theta = \dfrac{a}{c}$; $\csc\theta = \dfrac{c}{a}$; $\cos\theta = \dfrac{b}{c}$; $\sec\theta = \dfrac{c}{b}$' $\tan\theta = \dfrac{a}{b}$; $\cot\theta = \dfrac{b}{a}$

C2. opposite; adjacent to; hypotenuse

C3. true

C4. $\sin\theta$; $\cos\theta$; $\tan\theta$;

C5. $\tan\theta$; $\cot\theta$

C6. 1; $\sec^2\theta$; $\csc^2\theta$

C7. $\sin\theta$; $\tan\theta$; $\sec\theta$

Exercise Set 1.2

1. $c^2 = 9^2 + 12^2 = 225$

$c = \sqrt{225} = 15$

$\sin\theta = \dfrac{\text{opposite}}{\text{hypotenuse}} = \dfrac{9}{15} = \dfrac{3}{5}$

$\cos\theta = \dfrac{\text{adjacent}}{\text{hypotenuse}} = \dfrac{12}{15} = \dfrac{4}{5}$

$\tan\theta = \dfrac{\text{opposite}}{\text{adjacent}} = \dfrac{9}{12} = \dfrac{3}{4}$

$\csc\theta = \dfrac{\text{hypotenuse}}{\text{opposite}} = \dfrac{15}{9} = \dfrac{5}{3}$

$\sec\theta = \dfrac{\text{hypotenuse}}{\text{adjacent}} = \dfrac{15}{12} = \dfrac{5}{4}$

$\cot\theta = \dfrac{\text{adjacent}}{\text{opposite}} = \dfrac{12}{9} = \dfrac{4}{3}$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

2. $c^2 = 6^2 + 8^2 = 100$

$c = \sqrt{100} = 10$

$$\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{6}{10} = \frac{3}{5}$$
$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{8}{10} = \frac{4}{5}$$
$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{6}{8} = \frac{3}{4}$$
$$\csc\theta = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{10}{6} = \frac{5}{3}$$
$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{10}{8} = \frac{5}{4}$$
$$\cot\theta = \frac{\text{adjacent}}{\text{opposite}} = \frac{8}{6} = \frac{4}{3}$$

3. $a^2 + 21^2 = 29^2$

$a^2 = 841 - 441 = 400$

$a = \sqrt{400} = 20$

$$\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{20}{29}$$
$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{21}{29}$$
$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{20}{21}$$
$$\csc\theta = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{29}{20}$$
$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{29}{21}$$
$$\cot\theta = \frac{\text{adjacent}}{\text{opposite}} = \frac{21}{20}$$

4. $a^2 + 15^2 = 17^2$

$a^2 = 289 - 225 = 64$

$a = \sqrt{64} = 8$

$$\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{8}{17}$$
$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{15}{17}$$
$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{8}{15}$$
$$\csc\theta = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{17}{8}$$
$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{17}{15}$$
$$\cot\theta = \frac{\text{adjacent}}{\text{opposite}} = \frac{15}{8}$$

5. $10^2 + b^2 = 26^2$

$b^2 = 676 - 100 = 576$

$b = \sqrt{576} = 24$

$$\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{10}{26} = \frac{5}{13}$$
$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{24}{26} = \frac{12}{13}$$
$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{10}{24} = \frac{5}{12}$$
$$\csc\theta = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{26}{10} = \frac{13}{5}$$
$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{26}{24} = \frac{13}{12}$$
$$\cot\theta = \frac{\text{adjacent}}{\text{opposite}} = \frac{24}{10} = \frac{12}{5}$$

6. $a^2 + 40^2 = 41^2$

$a^2 = 1681 - 1600 = 81$

$a = \sqrt{81} = 9$

$$\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{9}{41}$$
$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{40}{41}$$
$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{9}{40}$$
$$\csc\theta = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{41}{9}$$
$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{41}{40}$$
$$\cot\theta = \frac{\text{adjacent}}{\text{opposite}} = \frac{40}{9}$$

7. $21^2 + b^2 = 35^2$

$b^2 = 1225 - 441 = 784$

$b = \sqrt{784} = 28$

$$\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{28}{35} = \frac{4}{5}$$
$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{21}{35} = \frac{3}{5}$$
$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{28}{21} = \frac{4}{3}$$
$$\csc\theta = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{35}{28} = \frac{5}{4}$$
$$\sec\theta = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{35}{21} = \frac{5}{3}$$
$$\cot\theta = \frac{\text{adjacent}}{\text{opposite}} = \frac{21}{28} = \frac{3}{4}$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

8. $a^2 + 24^2 = 25^2$

$a^2 = 625 - 576 = 49$

$a = \sqrt{49} = 7$

$\sin\theta = \dfrac{\text{opposite}}{\text{hypotenuse}} = \dfrac{24}{25}$

$\cos\theta = \dfrac{\text{adjacent}}{\text{hypotenuse}} = \dfrac{7}{25}$

$\tan\theta = \dfrac{\text{opposite}}{\text{adjacent}} = \dfrac{24}{7}$

$\csc\theta = \dfrac{\text{hypotenuse}}{\text{opposite}} = \dfrac{25}{24}$

$\sec\theta = \dfrac{\text{hypotenuse}}{\text{adjacent}} = \dfrac{25}{7}$

$\cot\theta = \dfrac{\text{adjacent}}{\text{opposite}} = \dfrac{7}{24}$

9. $\cos 30° = \dfrac{\text{length of side adjacent to } 30°}{\text{length of hypotenuse}} = \dfrac{\sqrt{3}}{2}$

10. $\tan 30° = \dfrac{\text{length of side opposite } 30°}{\text{length of side adjacent to } 30°} = \dfrac{1}{\sqrt{3}} = \dfrac{1}{\sqrt{3}} \cdot \dfrac{\sqrt{3}}{\sqrt{3}} = \dfrac{\sqrt{3}}{3}$

11. $\sec 45° = \dfrac{\text{length of hypotenuse}}{\text{length of side adjacent to } 45°} = \dfrac{\sqrt{2}}{1} = \sqrt{2}$

12. $\csc 45° = \dfrac{\text{length of hypotenuse}}{\text{length of side opposite } 45°} = \dfrac{\sqrt{2}}{1} = \sqrt{2}$

13. $\tan\dfrac{\pi}{3} = \tan 60° = \dfrac{\text{length of side opposite } 60°}{\text{length of side adjacent to } 60°} = \dfrac{\sqrt{3}}{1} = \sqrt{3}$

14. $\cot\dfrac{\pi}{3} = \cot 60° = \dfrac{\text{length of side adjacent to } 60°}{\text{length of side opposite } 60°} = \dfrac{1}{\sqrt{3}} = \dfrac{1}{\sqrt{3}} \cdot \dfrac{\sqrt{3}}{\sqrt{3}} = \dfrac{\sqrt{3}}{3}$

15. $\sin\dfrac{\pi}{4} - \cos\dfrac{\pi}{4} = \sin 45° - \cos 45° = \dfrac{1}{\sqrt{2}} - \dfrac{1}{\sqrt{2}} = 0$

16. $\tan\dfrac{\pi}{4} + \csc\dfrac{\pi}{6} = \tan 45° + \csc 30° = \dfrac{1}{1} + \dfrac{2}{1} = 1 + 2 = 3$

17. $\tan\theta = \dfrac{\sin\theta}{\cos\theta} = \dfrac{\frac{8}{17}}{\frac{15}{17}} = \dfrac{8}{15}$

$\csc\theta = \dfrac{1}{\sin\theta} = \dfrac{1}{\frac{8}{17}} = \dfrac{17}{8}$

$\sec\theta = \dfrac{1}{\cos\theta} = \dfrac{1}{\frac{15}{17}} = \dfrac{17}{15}$

$\cot\theta = \dfrac{\cos\theta}{\sin\theta} = \dfrac{\frac{15}{17}}{\frac{8}{17}} = \dfrac{15}{8}$

18. $\tan\theta = \dfrac{\frac{3}{5}}{\frac{4}{5}} = \dfrac{3}{4}$

$\csc\theta = \dfrac{1}{\sin\theta} = \dfrac{1}{\frac{3}{5}} = \dfrac{5}{3}$

$\sec\theta = \dfrac{1}{\cos\theta} = \dfrac{1}{\frac{4}{5}} = \dfrac{5}{4}$

$\cot\theta = \dfrac{\cos\theta}{\sin\theta} = \dfrac{\frac{4}{5}}{\frac{3}{5}} = \dfrac{4}{3}$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

19. $\tan\theta = \dfrac{\sin\theta}{\cos\theta} = \dfrac{\frac{1}{3}}{\frac{2\sqrt{2}}{3}} = \dfrac{1}{2\sqrt{2}}$

$= \dfrac{1}{2\sqrt{2}} \cdot \dfrac{\sqrt{2}}{\sqrt{2}} = \dfrac{\sqrt{2}}{4}$

$\csc\theta = \dfrac{1}{\sin\theta} = \dfrac{1}{\frac{1}{3}} = \dfrac{3}{1} = 3$

$\sec\theta = \dfrac{1}{\cos\theta} = \dfrac{1}{\frac{2\sqrt{2}}{3}} = \dfrac{3}{2\sqrt{2}}$

$= \dfrac{3}{2\sqrt{2}} \cdot \dfrac{\sqrt{2}}{\sqrt{2}} = \dfrac{3\sqrt{2}}{4}$

$\cot\theta = \dfrac{\cos\theta}{\sin\theta} = \dfrac{\frac{2\sqrt{2}}{3}}{\frac{1}{3}} = \dfrac{2\sqrt{2}}{1} = 2\sqrt{2}$

20. $\tan\theta = \dfrac{\sin\theta}{\cos\theta} = \dfrac{\frac{6}{7}}{\frac{\sqrt{13}}{7}} = \dfrac{6}{\sqrt{13}} = \dfrac{6}{\sqrt{13}} \cdot \dfrac{\sqrt{13}}{\sqrt{13}} = \dfrac{6\sqrt{13}}{13}$

$\csc\theta = \dfrac{1}{\sin\theta} = \dfrac{1}{\frac{6}{7}} = \dfrac{7}{6}$

$\sec\theta = \dfrac{1}{\cos\theta} = \dfrac{1}{\frac{\sqrt{13}}{7}} = \dfrac{7}{\sqrt{13}} \cdot \dfrac{\sqrt{13}}{\sqrt{13}} = \dfrac{7\sqrt{13}}{13}$

$\cot\theta = \dfrac{\cos\theta}{\sin\theta} = \dfrac{\frac{\sqrt{13}}{7}}{\frac{6}{7}} = \dfrac{\sqrt{13}}{6}$

21. $\sin^2\theta + \cos^2\theta = 1$

$\left(\dfrac{6}{7}\right)^2 + \cos^2\theta = 1$

$\dfrac{36}{49} + \cos^2\theta = 1$

$\cos^2\theta = 1 - \dfrac{36}{49}$

$\cos^2\theta = \dfrac{13}{49}$

$\cos\theta = \sqrt{\dfrac{13}{49}} = \dfrac{\sqrt{13}}{7}$

22. $\sin^2\theta + \cos^2\theta = 1$

$\left(\dfrac{7}{8}\right)^2 + \cos^2\theta = 1$

$\dfrac{49}{64} + \cos^2\theta = 1$

$\cos^2\theta = 1 - \dfrac{49}{64}$

$\cos^2\theta = \dfrac{15}{64}$

$\cos\theta = \sqrt{\dfrac{15}{64}} = \dfrac{\sqrt{15}}{8}$

23. $\sin^2\theta + \cos^2\theta = 1$

$\left(\dfrac{\sqrt{39}}{8}\right)^2 + \cos^2\theta = 1$

$\dfrac{39}{64} + \cos^2\theta = 1$

$\cos^2\theta = 1 - \dfrac{39}{64}$

$\cos^2\theta = \dfrac{25}{64}$

$\cos\theta = \sqrt{\dfrac{25}{64}} = \dfrac{5}{8}$

24. $\sin^2\theta + \cos^2\theta = 1$

$\left(\dfrac{\sqrt{21}}{5}\right)^2 + \cos^2\theta = 1$

$\dfrac{21}{25} + \cos^2\theta = 1$

$\cos^2\theta = 1 - \dfrac{21}{25}$

$\cos^2\theta = \dfrac{4}{25}$

$\cos\theta = \sqrt{\dfrac{4}{25}} = \dfrac{2}{5}$

25. $\sin 37^0 \csc 37^0 = \sin 37^0 \cdot \dfrac{1}{\sin 37^0} = 1$

26. $\cos 53^0 \sec 53^0 = \cos 53^0 \dfrac{1}{\cos 52^0} = 1$

27. $\sin^2\theta + \cos^2\theta = 1$

$\sin^2\dfrac{\pi}{9} + \cos^2\dfrac{\pi}{9} = 1$

28. We can find the value of the expression by using the Pythagorean identity $\sin^2\theta + \cos^2\theta = 1$

$\sin^2\dfrac{\pi}{10} + \cos^2\dfrac{\pi}{10} = 1$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

29. $1+\tan^2\theta=\sec^2\theta$

$1+\tan^2 23^0=\sec^2 23^0$

$1=\sec^2 23^0-\tan^2 23^0$

30. We can find the value of the expression by using the Pythagorean identity $1+\cot^2\theta=\csc^2\theta$

$\csc^2 63^0-\cot^2 63^0=1$

31. $\sin 7^\circ=\cos(90^\circ-7^\circ)=\cos 83^\circ$

32. $\sin 19^\circ=\cos(90^\circ-19^\circ)=\cos 71^\circ$

33. $\csc 25^\circ=\sec(90^\circ-25^\circ)=\sec 65^\circ$

34. $\csc 35^\circ=\sec(90^\circ-35^\circ)=\sec 55^\circ$

35. $\tan\frac{\pi}{9}=\cot\left(\frac{\pi}{2}-\frac{\pi}{9}\right)$

$=\cot\left(\frac{9\pi}{18}-\frac{2\pi}{18}\right)$

$=\cot\frac{7\pi}{18}$

36. $\tan\frac{\pi}{7}=\cot\left(\frac{\pi}{2}-\frac{\pi}{7}\right)=\cot\left(\frac{7\pi}{14}-\frac{2\pi}{14}\right)=\cot\frac{5\pi}{14}$

37. $\cos\frac{2\pi}{5}=\sin\left(\frac{\pi}{2}-\frac{2\pi}{5}\right)$

$=\sin\left(\frac{5\pi}{10}-\frac{4\pi}{10}\right)$

$=\sin\frac{\pi}{10}$

38. $\cos\frac{3\pi}{8}=\sin\left(\frac{\pi}{2}-\frac{3\pi}{8}\right)=\sin\left(\frac{4\pi}{8}-\frac{3\pi}{8}\right)=\sin\frac{\pi}{8}$

39.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
sin 38°	Degree	38 SIN	0.6157

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
sin 38°	Degree	SIN 38 ENTER	0.6157

40.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
cos 21°	Degree	21 COS	0.9336

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
cos 21°	Degree	COS 21 ENTER	0.9336

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

41.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
tan 32.7°	Degree	32.7 TAN	0.6420

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
tan 32.7°	Degree	TAN 32.7 ENTER	0.6420

42.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
tan 52.6°	Degree	52.6 TAN	1.3079

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
tan 52.6°	Degree	TAN 52.6 ENTER	1.3079

43.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
csc 17°	Degree	17 SIN $1/x$	3.4203

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
csc17°	Degree	(SIN 17) x^{-1} ENTER	3.4203

44.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
sec 55°	Degree	55 COS $1/x$	1.7434

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
sec 55°	Degree	(COS 55) x^{-1} ENTER	1.7434

45.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
$\cos\frac{\pi}{10}$	Radian	π ÷ 10 = COS	0.9511

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
$\cos\frac{\pi}{10}$	Radian	COS (π ÷ 10) ENTER	0.9511

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

46.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
$\sin\frac{3\pi}{10}$	Radian	$3 \times \pi \div 10 =$ SIN	0.8090

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
$\sin\frac{3\pi}{10}$	Radian	SIN ($3\pi \div 10$) ENTER	0.8090

47.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
$\cot\frac{\pi}{12}$	Radian	$\pi \div 12 =$ TAN $1/x$	3.7321

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
$\cot\frac{\pi}{12}$	Radian	(TAN ($\pi \div 12$)) x^{-1} ENTER	3.7321

48.

Many Scientific Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
$\cot\frac{\pi}{18}$	Radian	$\pi \div 18 =$ TAN $1/x$	5.6713

Many Graphing Calculators			
Function	**Mode**	**Keystrokes**	**Display** (rounded to four places)
$\cot\frac{\pi}{18}$	Radian	(TAN ($\pi \div 18$)) x^{-1} ENTER	5.6713

49. $\tan 37° = \frac{a}{250}$
$a = 250 \tan 37°$
$a \approx 250(0.7536) \approx 188$ cm

50. $\tan 61° = \frac{a}{10}$
$a = 10 \tan 61°$
$a \approx 10(1.8040) \approx 18$ cm

51. $\cos 34° = \frac{b}{220}$
$b = 220 \cos 34°$
$b \approx 220(0.8290) \approx 182$ in.

52. $\sin 34° = \frac{a}{13}$
$a = 13 \sin 34°$
$a \approx 13(0.5592) \approx 7$ m

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

53. $\sin 23° = \dfrac{16}{c}$

$c = \dfrac{16}{\sin 23°} \approx \dfrac{16}{0.3907} \approx 41 \text{ m}$

54. $\tan 44° = \dfrac{23}{b}$

$b = \dfrac{23}{\tan 44°} \approx \dfrac{23}{0.9657} \approx 24 \text{ yd}$

55.

Scientific Calculator	Graphing Calculator	Display (rounded to the nearest degree)
0.2974 $\boxed{\text{SIN}^{-1}}$	$\boxed{\text{SIN}^{-1}}$ 0.2974 $\boxed{\text{ENTER}}$	17

If $\sin\theta = 0.2974$, then $\theta \approx 17°$.

56.

Scientific Calculator	Graphing Calculator	Display (rounded to the nearest degree)
0.877 $\boxed{\text{COS}^{-1}}$	$\boxed{\text{COS}^{-1}}$ 0.877 $\boxed{\text{ENTER}}$	29

If $\cos\theta = 0.877$, then $\theta \approx 29°$.

57.

Scientific Calculator	Graphing Calculator	Display (rounded to the nearest degree)
4.6252 $\boxed{\text{TAN}^{-1}}$	$\boxed{\text{TAN}^{-1}}$ 4.6252 $\boxed{\text{ENTER}}$	78

If $\tan\theta = 4.6252$, then $\theta \approx 78°$.

58.

Scientific Calculator	Graphing Calculator	Display (rounded to the nearest degree)
26.0307 $\boxed{\text{TAN}^{-1}}$	$\boxed{\text{TAN}^{-1}}$ 26.0307 $\boxed{\text{ENTER}}$	88

If $\tan\theta = 26.0307$, then $\theta \approx 88°$.

59.

Scientific Calculator	Graphing Calculator	Display (rounded to three places)
0.4112 $\boxed{\text{COS}^{-1}}$	$\boxed{\text{COS}^{-1}}$ 0.4112 $\boxed{\text{ENTER}}$	1.147

If $\cos\theta = 0.4112$, then $\theta \approx 1.147$ radians.

60.

Scientific Calculator	Graphing Calculator	Display (rounded to three places)
0.9499 $\boxed{\text{SIN}^{-1}}$	$\boxed{\text{SIN}^{-1}}$ 0.9499 $\boxed{\text{ENTER}}$	1.253

If $\sin\theta = 0.9499$, then $\theta = 1.253$ radians.

61.

Scientific Calculator	Graphing Calculator	Display (rounded to three places)
0.4169 $\boxed{\text{TAN}^{-1}}$	$\boxed{\text{TAN}^{-1}}$ 0.4169 $\boxed{\text{ENTER}}$	0.395

If $\tan\theta = 0.4169$, then $\theta \approx 0.395$ radians.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

62.

Scientific Calculator	Graphing Calculator	Display (rounded to three places)
0.5117 $\boxed{\text{TAN}^{-1}}$	$\boxed{\text{TAN}^{-1}}$ 0.5117 $\boxed{\text{ENTER}}$	0.473

If $\tan\theta = 0.5117$, then $\theta = 0.473$

63.
$$\frac{\tan\frac{\pi}{3}}{2} - \frac{1}{\sec\frac{\pi}{6}} = \frac{\sqrt{3}}{2} - \frac{1}{\frac{1}{\cos\frac{\pi}{6}}}$$
$$= \frac{\sqrt{3}}{2} - \frac{1}{\frac{1}{\frac{\sqrt{3}}{2}}}$$
$$= \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2}$$
$$= 0$$

64.
$$\frac{1}{\cot\frac{\pi}{4}} - \frac{2}{\csc\frac{\pi}{6}} = \frac{1}{\frac{1}{\tan\frac{\pi}{4}}} - \frac{2}{\frac{1}{\sin\frac{\pi}{6}}}$$
$$= \frac{1}{\frac{1}{1}} - \frac{2}{\frac{1}{\frac{1}{2}}}$$
$$= \frac{1}{1} - \frac{2}{2}$$
$$= 1 - 1$$
$$= 0$$

65. $1 + \sin^2 40° + \sin^2 50°$
$$= 1 + \sin^2(90° - 50°) + \sin^2 50°$$
$$= 1 + \cos^2 50° + \sin^2 50°$$
$$= 1 + 1$$
$$= 2$$

66. $1 - \tan^2 10° + \csc^2 80°$
$$= 1 - \cot^2 80° + \csc^2 80°$$
$$= 1 + \csc^2 80° - \cot^2 80°$$
$$= 1 + 1$$
$$= 2$$

67. $\csc 37° \sec 53° - \tan 53° \cot 37°$
$$= \sec 53° \sec 53° - \tan 53° \tan 53°$$
$$= \sec^2 53° - \tan^2 53°$$
$$= 1$$

68. $\cos 12° \sin 78° + \cos 78° \sin 12°$
$$= \sin 78° \sin 78° + \cos 78° \cos 78°$$
$$= \sin^2 78° + \cos^2 78°$$
$$= 1$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

69. $f(\theta) = 2\cos\theta - \cos 2\theta$

$$f\left(\frac{\pi}{6}\right) = 2\cos\frac{\pi}{6} - \cos\left(2\cdot\frac{\pi}{6}\right)$$
$$= 2\left(\frac{\sqrt{3}}{2}\right) - \cos\left(\frac{\pi}{3}\right)$$
$$= \frac{2\sqrt{3}}{2} - \frac{1}{2}$$
$$= \frac{2\sqrt{3}-1}{2}$$

70. $f(\theta) = 2\sin\theta - \sin\frac{\theta}{2}$

$$f\left(\frac{\pi}{3}\right) = 2\sin\frac{\pi}{3} - \sin\frac{\frac{\pi}{3}}{2}$$
$$= 2\left(\frac{\sqrt{3}}{2}\right) - \sin\left(\frac{\pi}{6}\right)$$
$$= \frac{2\sqrt{3}}{2} - \frac{1}{2}$$
$$= \frac{2\sqrt{3}-1}{2}$$

71. $\tan\left(\frac{\pi}{2} - \theta\right) = \cot\theta = \frac{1}{4}$

72. $\csc\left(\frac{\pi}{2} - \theta\right) = \sec\theta = \frac{1}{\cos\theta} = \frac{1}{\frac{1}{3}} = 3$

73. $\tan 40° = \frac{a}{630}$

$a = 630\tan 40°$

$a \approx 630(0.8391) \approx 529$

The distance across the lake is approximately 529 yards.

74. $\tan 40° = \frac{h}{35}$

$h = 35\tan 40°$

$h \approx 35(0.8391) \approx 29$

The tree's height is approximately 29 feet.

75. $\tan\theta = \frac{125}{172}$

Use a calculator in degree mode to find θ.

Many Scientific Calculators	Many Graphing Calculators
125 ÷ 172 = TAN^{-1}	TAN^{-1} (125 ÷ 172) ENTER

The display should show approximately 36. Thus, the angle of elevation of the sun is approximately 36°.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

76. $\tan\dfrac{555}{1320}$

Use a calculator in degree mode to find θ.

Many Scientific Calculators	Many Graphing Calculators
555 ÷ 1320 = TAN^{-1}	TAN^{-1} (555 ÷ 1320) ENTER

The display should show approximately 23. Thus, the angle of elevation is approximately 23°.

77. $\sin 10° = \dfrac{500}{c}$

$c = \dfrac{500}{\sin 10°} \approx \dfrac{500}{0.1736} \approx 2880$

The plane has flown approximately 2880 feet.

78. $\sin 5° = \dfrac{a}{5000}$

$a = 5000\sin 5° \approx 5000(0.0872) = 436$

The driver's increase in altitude was approximately 436 feet.

79. $\cos\theta = \dfrac{60}{75}$

Use a calculator in degree mode to find θ.

Many Scientific Calculators	Many Graphing Calculators
60 ÷ 75 = COS^{-1}	COS^{-1} (60 ÷ 75) ENTER

The display should show approximately 37. Thus, the angle between the wire and the pole is approximately 37°.

80. $\cos\theta = \dfrac{55}{80}$

Use a calculator in degree mode to find θ.

Many Scientific Calculators	Many Graphing Calculators
55 ÷ 80 = COS^{-1}	COS^{-1} (55 ÷ 80) ENTER

The display should show approximately 47. Thus, the angle between the wire and the pole is approximately 47°.

81. – 91. Answers may vary.

92.

θ	0.4	0.3	0.2	0.1	0.01	0.001	0.0001	0.00001
$\sin\theta$	0.3894	0.2955	0.1987	0.0998	0.0099998	9.999998×10^{-4}	9.99999998×10^{-5}	1×10^{-5}
$\dfrac{\sin\theta}{\theta}$	0.9736	0.9851	0.9933	0.9983	0.99998	0.9999998	0.999999998	1

$\dfrac{\sin\theta}{\theta}$ approaches 1 as θ approaches 0.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

93.

θ	0.4	0.3	0.2	0.1	0.01	0.001	0.0001	0.00001
$\cos\theta$	0.92106	0.95534	0.98007	0.99500	0.99995	0.9999995	0.999999995	1
$\frac{\cos\theta-1}{\theta}$	–0.19735	–0.148878	–0.099667	–0.04996	–0.005	–0.0005	–0.00005	0

$\frac{\cos\theta-1}{\theta}$ approaches 0 as θ approaches 0.

94. does not make sense; Explanations will vary. Sample explanation: An increase in the size of a triangle does not affect the ratios of the sides.

95. does not make sense; Explanations will vary. Sample explanation: This value is irrational. Irrational numbers are rounded on calculators.

96. makes sense

97. makes sense

98. false; Changes to make the statement true will vary. A sample change is: $\frac{\tan 45^\circ}{\tan 15^\circ} \neq \tan\left(\frac{45^\circ}{15^\circ}\right)$

99. true

100. false; Changes to make the statement true will vary. A sample change is: $\sin 45^\circ + \cos 45^\circ = \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} = \frac{2}{\sqrt{2}} \neq 1$

101. true

102. In a right triangle, the hypotenuse is greater than either other side. Therefore both $\frac{\text{opposite}}{\text{hypotenuse}}$ and $\frac{\text{adjacent}}{\text{hypotenuse}}$ must be less than 1 for an acute angle in a right triangle.

103. Use a calculator in degree mode to generate the following table. Then use the table to describe what happens to the tangent of an acute angle as the angle gets close to 90°.

θ	60	70	80	89	89.9	89.99	89.999	89.9999
tanθ	1.7321	2.7475	5.6713	57	573	5730	57,296	572,958

As θ approaches 90°, tanθ increases without bound. At 90°, tanθ is undefined.

104. a. Let a = distance of the ship from the lighthouse.

$$\tan 35^\circ = \frac{250}{a}$$

$$a = \frac{250}{\tan 35^\circ} \approx \frac{250}{0.7002} \approx 357$$

The ship is approximately 357 feet from the lighthouse.

b. Let b = the plane's height above the lighthouse.

$$\tan 22^\circ = \frac{b}{357}$$

$$b = 357\tan 22^\circ \approx 357(0.4040) \approx 144$$

$$144 + 250 = 394$$

The plane is approximately 394 feet above the water.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

105. a. $\frac{y}{r}$

b. First find r: $r=\sqrt{x^2+y^2}$

$r=\sqrt{(-3)^2+4^2}$

$r=5$

$\frac{y}{r}=\frac{4}{5}$, which is positive.

106. a. $\frac{x}{r}$

b. First find r: $r=\sqrt{x^2+y^2}$

$r=\sqrt{(-3)^2+5^2}$

$r=\sqrt{34}$

$\frac{x}{r}=\frac{-3}{\sqrt{34}}=\frac{-3}{\sqrt{34}}\cdot\frac{\sqrt{34}}{\sqrt{34}}=\frac{-3\sqrt{34}}{34}$, which is negative.

107. a. $\theta'=360^{\circ}-345^{\circ}=15^{\circ}$

b. $\theta'=\pi-\frac{5\pi}{6}=\frac{6\pi}{6}-\frac{5\pi}{6}=\frac{\pi}{6}$

Section 1.3

Check Point Exercises

1. $r=\sqrt{x^2+y^2}$

$r=\sqrt{1^2+(-3)^2}=\sqrt{1+9}=\sqrt{10}$

Now that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$\sin\theta=\frac{y}{r}=\frac{-3}{\sqrt{10}}=-\frac{3\sqrt{10}}{10}$

$\cos\theta=\frac{x}{r}=\frac{1}{\sqrt{10}}=\frac{\sqrt{10}}{10}$

$\tan\theta=\frac{y}{x}=\frac{-3}{1}=-3$

$\csc\theta=\frac{r}{y}=\frac{\sqrt{10}}{-3}=-\frac{\sqrt{10}}{3}$

$\sec\theta=\frac{r}{x}=\frac{\sqrt{10}}{1}=\sqrt{10}$

$\cot\theta=\frac{x}{y}=\frac{1}{-3}=-\frac{1}{3}$

2. a. $\theta=0^{\circ}=0$ radians

The terminal side of the angle is on the positive *x*-axis. Select the point

$P=(1,0)$: $x=1, y=0, r=1$

Apply the definitions of the cosine and cosecant functions.

$\cos 0^{\circ}=\cos 0=\frac{x}{r}=\frac{1}{1}=1$

$\csc 0^{\circ}=\csc 0=\frac{r}{y}=\frac{1}{0}$, undefined

b. $\theta=90^{\circ}=\frac{\pi}{2}$ radians

The terminal side of the angle is on the positive *y*-axis. Select the point

$P=(0,1)$: $x=0, y=1, r=1$

Apply the definitions of the cosine and cosecant functions.

$\cos 90^{\circ}=\cos\frac{\pi}{2}=\frac{x}{r}=\frac{0}{1}=0$

$\csc 90^{\circ}=\csc\frac{\pi}{2}=\frac{r}{y}=\frac{1}{1}=1$

c. $\theta=180^{\circ}=\pi$ radians

The terminal side of the angle is on the negative *x*-axis. Select the point

$P=(-1,0)$: $x=-1, y=0, r=1$

Apply the definitions of the cosine and cosecant functions.

$\cos 180^{\circ}=\cos\pi=\frac{x}{r}=\frac{-1}{1}=-1$

$\csc 180^{\circ}=\csc\pi=\frac{r}{y}=\frac{1}{0}$, undefined

d. $\theta=270^{\circ}=\frac{3\pi}{2}$ radians

The terminal side of the angle is on the negative *y*-axis. Select the point

$P=(0,-1)$: $x=0, y=-1, r=1$

Apply the definitions of the cosine and cosecant functions.

$\cos 270^{\circ}=\cos\frac{3\pi}{2}=\frac{x}{r}=\frac{0}{1}=0$

$\csc 270^{\circ}=\csc\frac{3\pi}{2}=\frac{r}{y}=\frac{1}{-1}=-1$

3. Because $\sin\theta<0$, θ cannot lie in quadrant I; all the functions are positive in quadrant I. Furthermore, θ cannot lie in quadrant II; $\sin\theta$ is positive in quadrant II. Thus, with $\sin\theta<0$, θ lies in quadrant III or quadrant IV. We are also given that $\cos\theta<0$. Because quadrant III is the only quadrant in which cosine is negative and the sine is negative, we conclude that θ lies in quadrant III.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

4. Because the tangent is negative and the cosine is negative, θ lies in quadrant II. In quadrant II, x is negative and y is positive. Thus,

$$\tan\theta = -\frac{1}{3} = \frac{y}{x} = \frac{1}{-3}$$
$$x = -3,\ y = 1$$

Furthermore,

$$r = \sqrt{x^2 + y^2} = \sqrt{(-3)^2 + 1^2} = \sqrt{9+1} = \sqrt{10}$$

Now that we know x, y, and r, we can find $\sin\theta$ and $\sec\theta$.

$$\sin\theta = \frac{y}{r} = \frac{1}{\sqrt{10}} = \frac{1}{\sqrt{10}} \cdot \frac{\sqrt{10}}{\sqrt{10}} = \frac{\sqrt{10}}{10}$$
$$\sec\theta = \frac{r}{x} = \frac{\sqrt{10}}{-3} = -\frac{\sqrt{10}}{3}$$

5. a. Because 210° lies between 180° and 270°, it is in quadrant III. The reference angle is $\theta' = 210° - 180° = 30°$.

b. Because $\frac{7\pi}{4}$ lies between $\frac{3\pi}{2} = \frac{6\pi}{4}$ and $2\pi = \frac{8\pi}{4}$, it is in quadrant IV. The reference angle is $\theta' = 2\pi - \frac{7\pi}{4} = \frac{8\pi}{4} - \frac{7\pi}{4} = \frac{\pi}{4}$.

c. Because –240° lies between –180° and –270°, it is in quadrant II. The reference angle is $\theta = 240 - 180 = 60°$.

d. Because 3.6 lies between $\pi \approx 3.14$ and $\frac{3\pi}{2} \approx 4.71$, it is in quadrant III. The reference angle is $\theta' = 3.6 - \pi \approx 0.46$.

6. a. $665° - 360° = 305°$
This angle is in quadrant IV, thus the reference angle is $\theta' = 360° - 305° = 55°$.

b. $\frac{15\pi}{4} - 2\pi = \frac{15\pi}{4} - \frac{8\pi}{4} = \frac{7\pi}{4}$
This angle is in quadrant IV, thus the reference angle is $\theta' = 2\pi - \frac{7\pi}{4} = \frac{8\pi}{4} - \frac{7\pi}{4} = \frac{\pi}{4}$.

c. $-\frac{11\pi}{3} + 2 \cdot 2\pi = -\frac{11\pi}{3} + \frac{12\pi}{3} = \frac{\pi}{3}$
This angle is in quadrant I, thus the reference angle is $\theta' = \frac{\pi}{3}$.

7. a. 300° lies in quadrant IV. The reference angle is $\theta' = 360° - 300° = 60°$.

$$\sin 60° = \frac{\sqrt{3}}{2}$$

Because the sine is negative in quadrant IV,

$$\sin 300° = -\sin 60° = -\frac{\sqrt{3}}{2}.$$

b. $\frac{5\pi}{4}$ lies in quadrant III. The reference angle is

$$\theta' = \frac{5\pi}{4} - \pi = \frac{5\pi}{4} - \frac{4\pi}{4} = \frac{\pi}{4}.$$

$$\tan\frac{\pi}{4} = 1$$

Because the tangent is positive in quadrant III,

$$\tan\frac{5\pi}{4} = +\tan\frac{\pi}{4} = 1.$$

c. $-\frac{\pi}{6}$ lies in quadrant IV. The reference angle is

$$\theta' = \frac{\pi}{6}.$$

$$\sec\frac{\pi}{6} = \frac{2\sqrt{3}}{3}$$

Because the secant is positive in quadrant IV,

$$\sec\left(-\frac{\pi}{6}\right) = +\sec\frac{\pi}{6} = \frac{2\sqrt{3}}{3}.$$

8. a. $\frac{17\pi}{6} - 2\pi = \frac{17\pi}{6} - \frac{12\pi}{6} = \frac{5\pi}{6}$ lies in quadrant II.

The reference angle is $\theta' = \pi - \frac{5\pi}{6} = \frac{\pi}{6}$.

The function value for the reference angle is

$$\cos\frac{\pi}{6} = \frac{\sqrt{3}}{2}.$$

Because the cosine is negative in quadrant II,

$$\cos\frac{17\pi}{6} = \cos\frac{5\pi}{6} = -\cos\frac{\pi}{6} = -\frac{\sqrt{3}}{2}.$$

b. $\frac{-22\pi}{3} + 8\pi = \frac{-22\pi}{3} + \frac{24\pi}{3} = \frac{2\pi}{3}$ lies in quadrant II. The reference angle is

$$\theta' = \pi - \frac{2\pi}{3} = \frac{\pi}{3}.$$

The function value for the reference angle is

$$\sin\frac{\pi}{3} = \frac{\sqrt{3}}{2}.$$

Because the sine is positive in quadrant II,

$$\sin\frac{-22\pi}{3} = \sin\frac{2\pi}{3} = \sin\frac{\pi}{3} = \frac{\sqrt{3}}{2}.$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

Concept and Vocabulary Check 1.3

C1. $\sin\theta = \frac{y}{r}$; $\csc\theta = \frac{r}{y}$; $\cos\theta = \frac{x}{r}$; $\sec\theta = \frac{r}{x}$,
$\tan\theta = \frac{y}{x}$; $\cot\theta = \frac{x}{y}$

C2. $\tan\theta$; $\sec\theta$; $\cot\theta$; $\csc\theta$; $\tan\theta$; $\cot\theta$

C3. $\sin\theta$; $\csc\theta$;

C4. $\tan\theta$; $\cot\theta$;

C5. $\cos\theta$; $\sec\theta$

C6. terminal; x

C7. **(a)** $180° - \theta$; **(b)** $\theta - 180°$; **(c)** $360° - \theta$

Exercise Set 1.3

1. We need values for *x, y,* and *r.* Because $P = (-4, 3)$ is a point on the terminal side of θ, $x = -4$ and $y = 3$. Furthermore,

$r = \sqrt{x^2 + y^2} = \sqrt{(-4)^2 + 3^2} = \sqrt{16 + 9} = \sqrt{25} = 5$ No w that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$\sin\theta = \frac{y}{r} = \frac{3}{5}$
$\cos\theta = \frac{x}{r} = \frac{-4}{5} = -\frac{4}{5}$
$\tan\theta = \frac{y}{x} = \frac{3}{-4} = -\frac{3}{4}$
$\csc\theta = \frac{r}{y} = \frac{5}{3}$
$\sec\theta = \frac{r}{x} = \frac{5}{-4} = -\frac{5}{4}$
$\cot\theta = \frac{x}{y} = \frac{-4}{3} = -\frac{4}{3}$

2. We need values for *x, y,* and *r,* Because $P = (-12, 5)$ is a point on the terminal side of θ, $x = -12$ and $y = 5$. Furthermore,

$r = \sqrt{x^2 + y^2} = \sqrt{(-12)^2 + 5^2} = \sqrt{144 + 25}$
$= \sqrt{169} = 13$

Now that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$\sin\theta = \frac{y}{r} = \frac{5}{13}$
$\cos\theta = \frac{x}{r} = \frac{-12}{13} = -\frac{12}{13}$
$\tan\theta = \frac{y}{x} = \frac{5}{-12} = -\frac{5}{12}$

$\csc\theta = \frac{r}{y} = \frac{13}{5}$
$\sec\theta = \frac{r}{x} = \frac{13}{-12} = -\frac{13}{12}$
$\cot\theta = \frac{x}{y} = \frac{-12}{5} - \frac{12}{5}$

3. We need values for *x, y,* and *r.* Because $P = (2, 3)$ is a point on the terminal side of θ, $x = 2$ and $y = 3$. Furthermore,

$r = \sqrt{x^2 + y^2} = \sqrt{2^2 + 3^2} = \sqrt{4 + 9} = \sqrt{13}$

Now that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$\sin\theta = \frac{y}{r} = \frac{3}{\sqrt{13}} = \frac{3}{\sqrt{13}} \cdot \frac{\sqrt{13}}{\sqrt{13}} = \frac{3\sqrt{13}}{13}$
$\cos\theta = \frac{x}{r} = \frac{2}{\sqrt{13}} = \frac{2}{\sqrt{13}} \cdot \frac{\sqrt{13}}{\sqrt{13}} = \frac{2\sqrt{13}}{13}$
$\tan\theta = \frac{y}{x} = \frac{3}{2}$
$\csc\theta = \frac{r}{y} = \frac{\sqrt{13}}{3}$
$\sec\theta = \frac{r}{x} = \frac{\sqrt{13}}{2}$
$\cot\theta = \frac{x}{y} = \frac{2}{3}$

4. We need values for *x, y,* and *r,* Because $P = (3, 7)$ is a point on the terminal side of θ, $x = 3$ and $y = 7$. Furthermore,

$r = \sqrt{x^2 + y^2} = \sqrt{3^2 + 7^2} = \sqrt{9 + 49} = \sqrt{58}$

Now that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$\sin\theta = \frac{y}{r} = \frac{7}{\sqrt{58}} = \frac{7}{\sqrt{58}} \cdot \frac{\sqrt{58}}{\sqrt{58}} = \frac{7\sqrt{58}}{58}$
$\cos\theta = \frac{x}{r} = \frac{3}{\sqrt{58}} = \frac{3}{\sqrt{58}} \cdot \frac{\sqrt{58}}{\sqrt{58}} = \frac{3\sqrt{58}}{58}$
$\tan\theta = \frac{y}{x} = \frac{7}{3}$
$\csc\theta = \frac{r}{y} = \frac{\sqrt{58}}{7}$
$\sec\theta = \frac{r}{x} = \frac{\sqrt{58}}{3}$
$\cot\theta = \frac{x}{y} = \frac{3}{7}$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

5. We need values for *x, y,* and *r.* Because $P = (3, -3)$ is a point on the terminal side of θ, $x = 3$ and $y = -3$.

Furthermore, $r = \sqrt{x^2 + y^2} = \sqrt{3^2 + (-3)^2} = \sqrt{9+9}$
$= \sqrt{18} = 3\sqrt{2}$

Now that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-3}{3\sqrt{2}} = -\frac{-1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = -\frac{\sqrt{2}}{2}$$
$$\cos\theta = \frac{x}{r} = \frac{3}{3\sqrt{2}} = \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$
$$\tan\theta = \frac{y}{x} = \frac{-3}{3} = -1$$
$$\csc\theta = \frac{r}{y} = \frac{3\sqrt{2}}{-3} = -\sqrt{2}$$
$$\sec\theta = \frac{r}{x} = \frac{3\sqrt{2}}{3} = \sqrt{2}$$
$$\cot\theta = \frac{x}{y} = \frac{3}{-3} = -1$$

6. We need values for *x, y,* and *r,* Because $P = (5, -5)$ is a point on the terminal side of θ, $x = 5$ and $y = -5$.

Furthermore,

$r = \sqrt{x^2 + y^2} = \sqrt{5 + (-5)^2} = \sqrt{25+25} = \sqrt{50}$
$= 5\sqrt{2}$

Now that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-5}{5\sqrt{2}} = \frac{-1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = -\frac{\sqrt{2}}{2}$$
$$\cos\theta = \frac{x}{r} = \frac{5}{5\sqrt{2}} = \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$
$$\tan\theta = \frac{y}{x} = \frac{-5}{5} = -1$$
$$\csc\theta = \frac{r}{y} = \frac{5\sqrt{2}}{-5} = -\sqrt{2}$$
$$\sec\theta = \frac{r}{x} = \frac{5\sqrt{2}}{5} = \sqrt{2}$$
$$\cot\theta = \frac{x}{y} = \frac{5}{-5} = -1$$

7. We need values for *x, y,* and *r.* Because $P = (-2, -5)$ is a point on the terminal side of θ, $x = -2$ and $y = -5$. Furthermore,

$r = \sqrt{x^2 + y^2} = \sqrt{(-2)^2 + (-5)^2} = \sqrt{4+25} = \sqrt{29}$ No w that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-5}{\sqrt{29}} = \frac{-5}{\sqrt{29}} \cdot \frac{\sqrt{29}}{\sqrt{29}} = -\frac{5\sqrt{29}}{29}$$
$$\cos\theta = \frac{x}{r} = \frac{-2}{\sqrt{29}} = \frac{-2}{\sqrt{29}} \cdot \frac{\sqrt{29}}{\sqrt{29}} = -\frac{2\sqrt{29}}{29}$$
$$\tan\theta = \frac{y}{x} = \frac{-5}{-2} = \frac{5}{2}$$
$$\csc\theta = \frac{r}{y} = \frac{\sqrt{29}}{-5} = -\frac{\sqrt{29}}{5}$$
$$\sec\theta = \frac{r}{x} = \frac{\sqrt{29}}{-2} = -\frac{\sqrt{29}}{2}$$
$$\cot\theta = \frac{x}{y} = \frac{-2}{-5} = \frac{2}{5}$$

8. We need values for *x, y,* and *r,* Because $P = (-1, -3)$ is a point on the terminal side of θ, $x = -1$ and $y = -3$. Furthermore,

$r = \sqrt{x^2 + y^2} = \sqrt{(-1)^2 + (-3)^2} = \sqrt{1+9} = \sqrt{10}$

Now that we know *x, y,* and *r,* we can find the six trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-3}{\sqrt{10}} = \frac{-3}{\sqrt{10}} \cdot \frac{\sqrt{10}}{\sqrt{10}} = -\frac{3\sqrt{10}}{10}$$
$$\cos\theta = \frac{x}{r} = \frac{-1}{\sqrt{10}} = \frac{-1}{\sqrt{10}} \cdot \frac{\sqrt{10}}{\sqrt{10}} = -\frac{\sqrt{10}}{10}$$
$$\tan\theta = \frac{y}{x} = \frac{-3}{-1} = 3$$
$$\csc\theta = \frac{r}{y} = \frac{\sqrt{10}}{-3} = -\frac{\sqrt{10}}{3}$$
$$\sec\theta = \frac{r}{x} = \frac{\sqrt{10}}{-1} = -\sqrt{10}$$
$$\cot\theta = \frac{x}{y} = \frac{-1}{-3} = \frac{1}{3}$$

9. $\theta = \pi$ radians

The terminal side of the angle is on the negative *x*-axis. Select the point $P = (-1, 0)$:

$x = -1,\ y = 0,\ r = 1$ Apply the definition of the cosine function.

$$\cos\pi = \frac{x}{r} = \frac{-1}{1} = -1$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

10. $\theta = \pi$ radians
The terminal side of the angle is on the negative x-axis. Select the point $P = (-1, 0)$: $x = -1, y = 0, r = 1$
Apply the definition of the tangent function.
$\tan \pi = \frac{y}{x} = \frac{0}{-1} = 0$

11. $\theta = \pi$ radians
The terminal side of the angle is on the negative x-axis. Select the point $P = (-1, 0)$: $x = -1, y = 0, r = 1$ Apply the definition of the secant function.
$\sec \pi = \frac{r}{x} = \frac{1}{-1} = -1$

12. $\theta = \pi$ radians
The terminal side of the angle is on the negative x-axis. Select the point $P = (-1, 0)$: $x = -1, y = 0, r = 1$
Apply the definition of the cosecant function.
$\csc \pi = \frac{r}{y} = \frac{1}{0}$, undefined

13. $\theta = \frac{3\pi}{2}$ radians
The terminal side of the angle is on the negative y-axis. Select the point $P = (0, -1)$: $x = 0, y = -1, r = 1$ Apply the definition of the tangent function. $\tan \frac{3\pi}{2} = \frac{y}{x} = \frac{-1}{0}$, undefined

14. $\theta = \frac{3\pi}{2}$ radians
The terminal side of the angle is on the negative y-axis. Select the point $P = (0, -1)$: $x = 0, y = -1, r = 1$
Apply the definition of the cosine function.
$\cos \frac{3\pi}{2} = \frac{x}{r} = \frac{0}{1} = 0$

15. $\theta = \frac{\pi}{2}$ radians
The terminal side of the angle is on the positive y-axis. Select the point $P = (0, 1)$: $x = 0, y = 1, r = 1$ Apply the definition of the cotangent function. $\cot \frac{\pi}{2} = \frac{x}{y} = \frac{0}{1} = 0$

16. $\theta = \frac{\pi}{2}$ radians
The terminal side of the angle is on the positive y-axis. Select the point $P = (0, 1)$: $x = 0, y = 1, r = 1$
Apply the definition of the tangent function.
$\tan \frac{\pi}{2} = \frac{y}{x} = \frac{1}{0}$, undefined

17. Because $\sin \theta > 0$, θ cannot lie in quadrant III or quadrant IV; the sine function is negative in those quadrants. Thus, with $\sin \theta > 0$, θ lies in quadrant I or quadrant II. We are also given that $\cos \theta > 0$. Because quadrant I is the only quadrant in which the cosine is positive and sine is positive, we conclude that θ lies in quadrant I.

18. Because $\sin \theta < 0$, θ cannot lie in quadrant I or quadrant II; the sine function is positive in those two quadrants. Thus, with $\sin \theta < 0$, θ lies in quadrant III or quadrant IV. We are also given that $\cos \theta > 0$. Because quadrant IV is the only quadrant in which the cosine is positive and the sine is negative, we conclude that θ lies in quadrant IV.

19. Because $\sin \theta < 0$, θ cannot lie in quadrant I or quadrant II; the sine function is positive in those two quadrants. Thus, with $\sin \theta < 0$, θ lies in quadrant III or quadrant IV. We are also given that $\cos \theta < 0$. Because quadrant III is the only quadrant in which the cosine is positive and the sine is negative, we conclude that θ lies in quadrant III.

20. Because $\tan \theta < 0$, θ cannot lie in quadrant I or quadrant III; the tangent function is positive in those two quadrants. Thus, with $\tan \theta < 0$, θ lies in quadrant II or quadrant IV. We are also given that $\sin \theta < 0$. Because quadrant IV is the only quadrant in which the sine is negative and the tangent is negative, we conclude that θ lies in quadrant IV.

21. Because $\tan \theta < 0$, θ cannot lie in quadrant I or quadrant III; the tangent function is positive in those quadrants. Thus, with $\tan \theta < 0$, θ lies in quadrant II or quadrant IV. We are also given that $\cos \theta < 0$. Because quadrant II is the only quadrant in which the cosine is negative and the tangent is negative, we conclude that θ lies in quadrant II.

22. Because $\cot \theta > 0$, θ cannot lie in quadrant II or quadrant IV; the cotangent function is negative in those two quadrants. Thus, with $\cot \theta > 0$, θ lies in quadrant I or quadrant III. We are also given that $\sec \theta < 0$. Because quadrant III is the only quadrant in which the secant is negative and the cotangent is positive, we conclude that θ lies in quadrant III.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

23. In quadrant III x is negative and y is negative. Thus,

$\cos\theta = -\frac{3}{5} = \frac{x}{r} = \frac{-3}{5}$, $x = -3$, $r = 5$. Furthermore,

$$r^2 = x^2 + y^2$$
$$5^2 = (-3)^2 + y^2$$
$$y^2 = 25 - 9 = 16$$
$$y = -\sqrt{16} = -4$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-4}{5} = -\frac{4}{5}$$
$$\tan\theta = \frac{y}{x} = \frac{-4}{-3} = \frac{4}{3}$$
$$\csc\theta = \frac{r}{y} = \frac{5}{-4} = -\frac{5}{4}$$
$$\sec\theta = \frac{r}{x} = \frac{5}{-3} = -\frac{5}{3}$$
$$\cot\theta = \frac{x}{y} = \frac{-3}{-4} = \frac{3}{4}$$

24. In quadrant III, x is negative and y is negative. Thus,

$\sin\theta = -\frac{12}{13} = \frac{y}{r} = \frac{-12}{13}$, $y = -12$, $r = 13$.

Furthermore,

$$x^2 + y^2 = r^2$$
$$x^2 + (-12)^2 = 13^2$$
$$x^2 = 169 - 144 = 25$$
$$x = -\sqrt{25} = -5$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\cos\theta = \frac{x}{r} = \frac{-5}{13} = -\frac{5}{13}$$
$$\tan\theta = \frac{y}{x} = \frac{-12}{-5} = \frac{12}{5}$$
$$\csc\theta = \frac{r}{y} = \frac{13}{-12} = -\frac{13}{12}$$
$$\sec\theta = \frac{r}{x} = \frac{13}{-5} = -\frac{13}{5}$$
$$\cot\theta = \frac{x}{y} = \frac{-5}{-12} = \frac{5}{12}$$

25. In quadrant II x is negative and y is positive. Thus,

$\sin\theta = \frac{5}{13} = \frac{y}{r}$, $y = 5$, $r = 13$. Furthermore,

$$x^2 + y^2 = r^2$$
$$x^2 + 5^2 = 13^2$$
$$x^2 = 169 - 25 = 144$$
$$x = -\sqrt{144} = -12$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\cos\theta = \frac{x}{r} = \frac{-12}{13} = -\frac{12}{13}$$
$$\tan\theta = \frac{y}{x} = \frac{5}{-12} = -\frac{5}{12}$$
$$\csc\theta = \frac{r}{y} = \frac{13}{5}$$
$$\sec\theta = \frac{r}{x} = \frac{13}{-12} = -\frac{13}{12}$$
$$\cot\theta = \frac{x}{y} = \frac{-12}{5} = -\frac{12}{5}$$

26. In quadrant IV, x is positive and y is negative. Thus,

$\cos\theta = \frac{4}{5} = \frac{x}{r}$, $x = 4$, $r = 5$.

Furthermore, $x^2 + y^2 = r^2$

$$4^2 + y^2 = 5^2$$
$$y^2 = 25 - 16 = 9$$
$$y = -\sqrt{9} = -3$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-3}{5} = -\frac{3}{5}$$
$$\tan\theta = \frac{y}{x} = \frac{-3}{4} = -\frac{3}{4}$$
$$\csc\theta = \frac{r}{y} = \frac{5}{-3} = -\frac{5}{3}$$
$$\sec\theta = \frac{r}{x} = \frac{5}{4}$$
$$\cot\theta = \frac{x}{y} = \frac{4}{-3} = -\frac{4}{3}$$

27. Because $270° < \theta < 360°$, θ is in quadrant IV. In quadrant IV x is positive and y is negative. Thus,

$\cos\theta = \frac{8}{17} = \frac{x}{r}$, $x = 8$,

$r = 17$. Furthermore

$$x^2 + y^2 = r^2$$
$$8^2 + y^2 = 17^2$$
$$y^2 = 289 - 64 = 225$$
$$y = -\sqrt{225} = -15$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-15}{17} = -\frac{15}{17}$$
$$\tan\theta = \frac{y}{x} = \frac{-15}{8} = -\frac{15}{8}$$
$$\csc\theta = \frac{r}{y} = \frac{17}{-15} = -\frac{17}{15}$$
$$\sec\theta = \frac{r}{x} = \frac{17}{8}$$
$$\cot\theta = \frac{x}{y} = \frac{8}{-15} = -\frac{8}{15}$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

28. Because $270° < \theta < 360°$, θ is in quadrant IV. In quadrant IV, x is positive and y is negative. Thus, $\cos\theta = \frac{1}{3} = \frac{x}{r}$, $x = 1$, $r = 3$. Furthermore,

$$x^2 + y^2 = r^2$$
$$1^2 + y^2 = 3^2$$
$$y^2 = 9 - 1 = 8$$
$$y = -\sqrt{8} = -2\sqrt{2}$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-2\sqrt{2}}{3} = -\frac{2\sqrt{2}}{3}$$
$$\tan\theta = \frac{y}{x} = \frac{-2\sqrt{2}}{1} = -2\sqrt{2}$$
$$\csc\theta = \frac{r}{y} = \frac{3}{-2\sqrt{2}} = \frac{3}{-2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = -\frac{3\sqrt{2}}{4}$$
$$\sec\theta = \frac{r}{x} = \frac{3}{1} = 3$$
$$\cot\theta = \frac{x}{y} = \frac{1}{-2\sqrt{2}} = \frac{1}{-2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = -\frac{\sqrt{2}}{4}$$

29. Because the tangent is negative and the sine is positive, θ lies in quadrant II. In quadrant II, x is negative and y is positive. Thus, $\tan\theta = -\frac{2}{3} = \frac{y}{x} = \frac{2}{-3}$, $x = -3$, $y = 2$. Furthermore,

$$r = \sqrt{x^2 + y^2} = \sqrt{(-3)^2 + 2^2} = \sqrt{9 + 4} = \sqrt{13}$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{2}{\sqrt{13}} = \frac{2}{\sqrt{13}} \cdot \frac{\sqrt{13}}{\sqrt{13}} = \frac{2\sqrt{13}}{13}$$
$$\cos\theta = \frac{x}{r} = \frac{-3}{\sqrt{13}} = \frac{-3}{\sqrt{13}} \cdot \frac{\sqrt{13}}{\sqrt{13}} = -\frac{3\sqrt{13}}{13}$$
$$\csc\theta = \frac{r}{y} = \frac{\sqrt{13}}{2}$$
$$\sec\theta = \frac{r}{x} = \frac{\sqrt{13}}{-3} = -\frac{\sqrt{13}}{3}$$
$$\cot\theta = \frac{x}{y} = \frac{-3}{2} = -\frac{3}{2}$$

30. Because the tangent is negative and the sine is positive, θ lies in quadrant II. In quadrant II, x is negative and y is positive. Thus, $\tan\theta = -\frac{1}{3} = \frac{y}{x} = \frac{1}{-3}$, $y = 1$, $x = -3$. Furthermore,

$$r = \sqrt{x^2 + y^2} = \sqrt{(-3)^2 + 1^2} = \sqrt{9 + 1} = \sqrt{10}$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{1}{\sqrt{10}} = \frac{1}{\sqrt{10}} \cdot \frac{\sqrt{10}}{\sqrt{10}} = \frac{\sqrt{10}}{10}$$
$$\cos\theta = \frac{x}{r} = \frac{-3}{\sqrt{10}} = \frac{-3}{\sqrt{10}} \cdot \frac{\sqrt{10}}{\sqrt{10}} = -\frac{3\sqrt{10}}{10}$$
$$\csc\theta = \frac{r}{y} = \frac{\sqrt{10}}{1} = \sqrt{10}$$
$$\sec\theta = \frac{r}{x} = \frac{\sqrt{10}}{-3} = -\frac{\sqrt{10}}{3}$$
$$\cot\theta = \frac{x}{y} = \frac{-3}{1} = -3$$

31. Because the tangent is positive and the cosine is negative, θ lies in quadrant III. In quadrant III, x is negative and y is negative. Thus, $\tan\theta = \frac{4}{3} = \frac{y}{x} = \frac{-4}{-3}$, $x = -3$, $y = -4$. Furthermore,

$$r = \sqrt{x^2 + y^2} = \sqrt{(-3)^2 + (-4)^2} = \sqrt{9 + 16}$$
$$= \sqrt{25} = 5$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-4}{5} = -\frac{4}{5}$$
$$\cos\theta = \frac{x}{r} = \frac{-3}{5} = -\frac{3}{5}$$
$$\csc\theta = \frac{r}{y} = \frac{5}{-4} = -\frac{5}{4}$$
$$\sec\theta = \frac{r}{x} = \frac{5}{-3} = -\frac{5}{3}$$
$$\cot\theta = \frac{x}{y} = \frac{-3}{-4} = \frac{3}{4}$$

32. Because the tangent is positive and the cosine is negative, θ lies in quadrant III. In quadrant III, x is negative and y is negative. Thus, $\tan\theta = \frac{5}{12} = \frac{y}{x} = \frac{-5}{-12}$, $x = -12$, $y = -5$. Furthermore,

$$r = \sqrt{x^2 + y^2} = \sqrt{(-12)^2 + (-5)^2} = \sqrt{144 + 25}$$
$$= \sqrt{169} = 13$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-5}{13} = -\frac{5}{13}$$
$$\cos\theta = \frac{x}{r} = \frac{-12}{13} = -\frac{12}{13}$$
$$\csc\theta = \frac{r}{y} = \frac{13}{-5} = -\frac{13}{5}$$
$$\sec\theta = \frac{r}{x} = \frac{13}{-12} = -\frac{13}{12}$$
$$\cot\theta = \frac{x}{y} = \frac{-12}{-5} = \frac{12}{5}$$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

33. Because the secant is negative and the tangent is positive, θ lies in quadrant III. In quadrant III, x is negative and y is negative. Thus,

$\sec\theta = -3 = \frac{r}{x} = \frac{3}{-1}$, $x = -1$, $r = 3$. Furthermore,

$$x^2 + y^2 = r^2$$
$$(-1)^2 + y^2 = 3^2$$
$$y^2 = 9 - 1 = 8$$
$$y = -\sqrt{8} = -2\sqrt{2}$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-2\sqrt{2}}{3} = -\frac{2\sqrt{2}}{3}$$
$$\cos\theta = \frac{x}{r} = \frac{-1}{3} = -\frac{1}{3}$$
$$\tan\theta = \frac{y}{x} = \frac{-2\sqrt{2}}{-1} = 2\sqrt{2}$$
$$\csc\theta = \frac{r}{y} = \frac{3}{-2\sqrt{2}} = \frac{3}{-2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = -\frac{3\sqrt{2}}{4}$$
$$\cot\theta = \frac{x}{y} = \frac{-1}{-2\sqrt{2}} = \frac{1}{2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{4}$$

34. Because the cosecant is negative and the tangent is positive, θ lies in quadrant III. In quadrant III, x is negative and y is negative. Thus,

$\csc\theta = -4 = \frac{r}{y} = \frac{4}{-1}$, $y = -1$, $r = 4$. Furthermore,

$$x^2 + y^2 = r^2$$
$$x^2 + (-1)^2 = 4^2$$
$$x^2 = 16 - 1 = 15$$
$$x = -\sqrt{15}$$

Now that we know x, y, and r, we can find the remaining trigonometric functions of θ.

$$\sin\theta = \frac{y}{r} = \frac{-1}{4} = -\frac{1}{4}$$
$$\cos\theta = \frac{x}{r} = \frac{-\sqrt{15}}{4} = -\frac{\sqrt{15}}{4}$$
$$\tan\theta = \frac{y}{x} = \frac{-1}{-\sqrt{15}} = \frac{1}{\sqrt{15}} \cdot \frac{\sqrt{15}}{\sqrt{15}} = \frac{\sqrt{15}}{15}$$
$$\sec\theta = \frac{r}{x} = \frac{4}{-\sqrt{15}} = -\frac{4}{\sqrt{15}} \cdot \frac{\sqrt{15}}{\sqrt{15}} = -\frac{4\sqrt{15}}{15}$$
$$\cot\theta = \frac{x}{y} = \frac{-\sqrt{15}}{-1} = \sqrt{15}$$

35. Because 160° lies between 90° and 180°, it is in quadrant II. The reference angle is $\theta' = 180° - 160° = 20°$.

36. Because 170° lies between 90° and 180°, it is in quadrant II. The reference angle is $\theta' = 180° - 170° = 10°$.

37. Because 205° lies between 180° and 270°, it is in quadrant III. The reference angle is $\theta' = 205° - 180° = 25°$.

38. Because 210° lies between 180° and 270°, it is in quadrant III. The reference angle is $\theta' = 210° - 180° = 30°$.

39. Because 355° lies between 270° and 360°, it is in quadrant IV. The reference angle is $\theta' = 360° - 355° = 5°$.

40. Because 351° lies between 270° and 360°, it is in quadrant IV. The reference angle is $\theta' = 360° - 351° = 9°$.

41. Because $\frac{7\pi}{4}$ lies between $\frac{3\pi}{2} = \frac{6\pi}{4}$ and $2\pi = \frac{8\pi}{4}$, it is in quadrant IV. The reference angle is

$$\theta' = 2\pi - \frac{7\pi}{4} = \frac{8\pi}{4} - \frac{7\pi}{4} = \frac{\pi}{4}.$$

42. Because $\frac{5\pi}{4}$ lies between $\pi = \frac{4\pi}{4}$ and $\frac{3\pi}{2} = \frac{6\pi}{4}$, it is in quadrant III. The reference angle is

$$\theta' = \frac{5\pi}{4} - \pi = \frac{5\pi}{4} - \frac{4\pi}{4} = \frac{\pi}{4}.$$

43. Because $\frac{5\pi}{6}$ lies between $\frac{\pi}{2} = \frac{3\pi}{6}$ and $\pi = \frac{6\pi}{6}$, it is in quadrant II. The reference angle is

$$\theta' = \pi - \frac{5\pi}{6} = \frac{6\pi}{6} - \frac{5\pi}{6} = \frac{\pi}{6}.$$

44. Because $\frac{5\pi}{7} = \frac{10\pi}{14}$ lies between $\frac{\pi}{2} = \frac{7\pi}{14}$ and $\pi = \frac{14\pi}{14}$, it is in quadrant II. The reference angle is

$$\theta' = \pi - \frac{5\pi}{7} = \frac{7\pi}{7} - \frac{5\pi}{7} = \frac{2\pi}{7}.$$

45. $-150° + 360° = 210°$
Because the angle is in quadrant III, the reference angle is $\theta' = 210° - 180° = 30°$.

46. $-250° + 360° = 110°$
Because the angle is in quadrant II, the reference angle is $\theta' = 180° - 110° = 70°$.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

47. $-335^\circ + 360^\circ = 25^\circ$
Because the angle is in quadrant I, the reference angle is $\theta' = 25^\circ$.

48. $-359^\circ + 360^\circ = 1^\circ$
Because the angle is in quadrant I, the reference angle is $\theta' = 1^\circ$.

49. Because 4.7 lies between $\pi \approx 3.14$ and $\frac{3\pi}{2} \approx 4.71$, it is in quadrant III. The reference angle is $\theta' = 4.7 - \pi \approx 1.56$.

50. Because 5.5 lies between $\frac{3\pi}{2} \approx 4.71$ and $2\pi \approx 6.28$, it is in quadrant IV. The reference angle is $\theta' = 2\pi - 5.5 \approx 0.78$.

51. $565^\circ - 360^\circ = 205^\circ$
Because the angle is in quadrant III, the reference angle is $\theta' = 205^\circ - 180^\circ = 25^\circ$.

52. $553^\circ - 360^\circ = 193^\circ$
Because the angle is in quadrant III, the reference angle is $\theta' = 193^\circ - 180^\circ = 13^\circ$.

53. $\frac{17\pi}{6} - 2\pi = \frac{17\pi}{6} - \frac{12\pi}{6} = \frac{5\pi}{6}$
Because the angle is in quadrant II, the reference angle is $\theta' = \pi - \frac{5\pi}{6} = \frac{\pi}{6}$.

54. $\frac{11\pi}{4} - 2\pi = \frac{11\pi}{4} - \frac{8\pi}{4} = \frac{3\pi}{4}$
Because the angle is in quadrant II, the reference angle is $\theta' = \pi - \frac{3\pi}{4} = \frac{\pi}{4}$.

55. $\frac{23\pi}{4} - 4\pi = \frac{23\pi}{4} - \frac{16\pi}{4} = \frac{7\pi}{4}$
Because the angle is in quadrant IV, the reference angle is $\theta' = 2\pi - \frac{7\pi}{4} = \frac{\pi}{4}$.

56. $\frac{17\pi}{3} - 4\pi = \frac{17\pi}{3} - \frac{12\pi}{3} = \frac{5\pi}{3}$
Because the angle is in quadrant IV, the reference angle is $\theta' = 2\pi - \frac{5\pi}{3} = \frac{\pi}{3}$.

57. $-\frac{11\pi}{4} + 4\pi = -\frac{11\pi}{4} + \frac{16\pi}{4} = \frac{5\pi}{4}$
Because the angle is in quadrant III, the reference angle is $\theta' = \frac{5\pi}{4} - \pi = \frac{\pi}{4}$.

58. $-\frac{17\pi}{6} + 4\pi = -\frac{17\pi}{6} + \frac{24\pi}{6} = \frac{7\pi}{6}$
Because the angle is in quadrant III, the reference angle is $\theta' = \frac{7\pi}{6} - \pi = \frac{\pi}{6}$.

59. $-\frac{25\pi}{6} + 6\pi = -\frac{25\pi}{6} + \frac{36\pi}{6} = \frac{11\pi}{6}$
Because the angle is in quadrant IV, the reference angle is $\theta' = 2\pi - \frac{11\pi}{6} = \frac{\pi}{6}$.

60. $-\frac{13\pi}{3} + 6\pi = -\frac{13\pi}{3} + \frac{18\pi}{3} = \frac{5\pi}{3}$
Because the angle is in quadrant IV, the reference angle is $\theta' = 2\pi - \frac{5\pi}{3} = \frac{\pi}{3}$.

61. 225° lies in quadrant III. The reference angle is $\theta' = 225^\circ - 180^\circ = 45^\circ$.
$\cos 45^\circ = \frac{\sqrt{2}}{2}$
Because the cosine is negative in quadrant III,
$\cos 225^\circ = -\cos 45^\circ = -\frac{\sqrt{2}}{2}$.

62. 300° lies in quadrant IV. The reference angle is $\theta' = 360^\circ - 300^\circ = 60^\circ$.
$\sin 60^\circ = \frac{\sqrt{3}}{2}$
Because the sine is negative in quadrant IV,
$\sin 300^\circ = -\sin 60^\circ = -\frac{\sqrt{3}}{2}$.

63. 210° lies in quadrant III. The reference angle is $\theta' = 210^\circ - 180^\circ = 30^\circ$.
$\tan 30^\circ = \frac{\sqrt{3}}{3}$
Because the tangent is positive in quadrant III,
$\tan 210^\circ = \tan 30^\circ = \frac{\sqrt{3}}{3}$.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

64. 240° lies in quadrant III. The reference angle is
$\theta' = 240° - 180° = 60°$.
$\sec 60° = 2$
Because the secant is negative in quadrant III,
$\sec 240° = -\sec 60° - 2$.

65. 420° lies in quadrant I. The reference angle is
$\theta' = 420° - 360° = 60°$.
$\tan 60° = \sqrt{3}$
Because the tangent is positive in quadrant I,
$\tan 420° = \tan 60° = \sqrt{3}$.

66. 405° lies in quadrant I. The reference angle is
$\theta' = 405° - 360° = 45°$.
$\tan 45° = 1$
Because the tangent is positive in quadrant I,
$\tan 405° = \tan 45° = 1$.

67. $\frac{2\pi}{3}$ lies in quadrant II. The reference angle is
$\theta' = \pi - \frac{2\pi}{3} = \frac{3\pi}{3} - \frac{2\pi}{3} = \frac{\pi}{3}$.
$\sin\frac{\pi}{3} = \frac{\sqrt{3}}{2}$
Because the sine is positive in quadrant II,
$\sin\frac{2\pi}{3} = \sin\frac{\pi}{3} = \frac{\sqrt{3}}{2}$.

68. $\frac{3\pi}{4}$ lies in quadrant II. The reference angle is
$\theta' = \pi - \frac{3\pi}{4} = \frac{4\pi}{4} - \frac{3\pi}{4} = \frac{\pi}{4}$.
$\cos\frac{\pi}{4} = \frac{\sqrt{2}}{2}$
Because the cosine is negative in quadrant II,
$\cos\frac{3\pi}{4} = -\cos\frac{\pi}{4} = -\frac{\sqrt{2}}{2}$.

69. $\frac{7\pi}{6}$ lies in quadrant III. The reference angle is
$\theta' = \frac{7\pi}{6} - \pi = \frac{7\pi}{6} - \frac{6\pi}{6} = \frac{\pi}{6}$.
$\csc\frac{\pi}{6} = 2$
Because the cosecant is negative in quadrant III,
$\csc\frac{7\pi}{6} = -\csc\frac{\pi}{6} = -2$.

70. $\frac{7\pi}{4}$ lies in quadrant IV. The reference angle is
$\theta' = 2\pi - \frac{7\pi}{4} = \frac{8\pi}{4} - \frac{7\pi}{4} = \frac{\pi}{4}$.
$\cot\frac{\pi}{4} = 1$
Because the cotangent is negative in quadrant IV,
$\cot\frac{7\pi}{4} = -\cot\frac{\pi}{4} = -1$.

71. $\frac{9\pi}{4}$ lies in quadrant I. The reference angle is
$\theta' = \frac{9\pi}{4} - 2\pi = \frac{9\pi}{4} - \frac{8\pi}{4} = \frac{\pi}{4}$.
$\tan\frac{\pi}{4} = 1$
Because the tangent is positive in quadrant I,
$\tan\frac{9\pi}{4} = \tan\frac{\pi}{4} = 1$

72. $\frac{9\pi}{2}$ lies on the positive y-axis. The reference angle is
$\theta' = \frac{9\pi}{2} - 4\pi = \frac{9\pi}{2} - \frac{8\pi}{2} = \frac{\pi}{2}$.
Because $\tan\frac{\pi}{2}$ is undefined, $\tan\frac{9\pi}{2}$ is also undefined.

73. –240° lies in quadrant II. The reference angle is
$\theta' = 240° - 180° = 60°$.
$\sin 60° = \frac{\sqrt{3}}{2}$
Because the sine is positive in quadrant II,
$\sin(-240°) = \sin 60° = \frac{\sqrt{3}}{2}$.

74. –225° lies in quadrant II. The reference angle is
$\theta' = 225° - 180° = 45°$.
$\sin 45° = \frac{\sqrt{2}}{2}$
Because the sine is positive in quadrant II,
$\sin(-225°) = \sin 45° = \frac{\sqrt{2}}{2}$.

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual

75. $-\frac{\pi}{4}$ lies in quadrant IV. The reference angle is $\theta' = \frac{\pi}{4}$.

$\tan\frac{\pi}{4} = 1$

Because the tangent is negative in quadrant IV,

$\tan\left(-\frac{\pi}{4}\right) = -\tan\frac{\pi}{4} = -1$

76. $-\frac{\pi}{6}$ lies in quadrant IV. The reference angle is $\theta = \frac{\pi}{6}$. $\tan\frac{\pi}{6} = \frac{\sqrt{3}}{3}$

Because the tangent is negative in quadrant IV,

$\tan\left(-\frac{\pi}{6}\right) = -\frac{\sqrt{3}}{3}$.

77. $\sec 495° = \sec 135° = -\sqrt{2}$

78. $\sec 510° = \sec 150° = -\frac{2\sqrt{3}}{3}$

79. $\cot\frac{19\pi}{6} = \cot\frac{7\pi}{6} = \sqrt{3}$

80. $\cot\frac{13\pi}{3} = \cot\frac{\pi}{3} = \frac{\sqrt{3}}{3}$

81. $\cos\frac{23\pi}{4} = \cos\frac{7\pi}{4} = \frac{\sqrt{2}}{2}$

82. $\cos\frac{35\pi}{6} = \cos\frac{11\pi}{6} = \frac{\sqrt{3}}{2}$

83. $\tan\left(-\frac{17\pi}{6}\right) = \tan\frac{7\pi}{6} = \frac{\sqrt{3}}{3}$

84. $\tan\left(-\frac{11\pi}{4}\right) = \tan\frac{\pi}{4} = 1$

85. $\sin\left(-\frac{17\pi}{3}\right) = \sin\frac{\pi}{3} = \frac{\sqrt{3}}{2}$

86. $\sin\left(-\frac{35\pi}{6}\right) = \sin\frac{\pi}{6} = \frac{1}{2}$

87. $\sin\frac{\pi}{3}\cos\pi - \cos\frac{\pi}{3}\sin\frac{3\pi}{2}$

$= \left(\frac{\sqrt{3}}{2}\right)(-1) - \left(\frac{1}{2}\right)(-1)$

$= -\frac{\sqrt{3}}{2} + \frac{1}{2}$

$= \frac{1-\sqrt{3}}{2}$

88. $\sin\frac{\pi}{4}\cos 0 - \sin\frac{\pi}{6}\cos\pi$

$= \left(\frac{\sqrt{2}}{2}\right)(1) - \left(\frac{1}{2}\right)(-1)$

$= \frac{\sqrt{2}}{2} + \frac{1}{2}$

$= \frac{\sqrt{2}+1}{2}$

89. $\sin\frac{11\pi}{4}\cos\frac{5\pi}{6} + \cos\frac{11\pi}{4}\sin\frac{5\pi}{6}$

$= \left(\frac{\sqrt{2}}{2}\right)\left(-\frac{\sqrt{3}}{2}\right) + \left(-\frac{\sqrt{2}}{2}\right)\left(\frac{1}{2}\right)$

$= -\frac{\sqrt{6}}{4} - \frac{\sqrt{2}}{4}$

$= -\frac{\sqrt{6}+\sqrt{2}}{4}$

90. $\sin\frac{17\pi}{3}\cos\frac{5\pi}{4} + \cos\frac{17\pi}{3}\sin\frac{5\pi}{4}$

$= \left(-\frac{\sqrt{3}}{2}\right)\left(-\frac{\sqrt{2}}{2}\right) + \left(\frac{1}{2}\right)\left(-\frac{\sqrt{2}}{2}\right)$

$= \frac{\sqrt{6}}{4} - \frac{\sqrt{2}}{4}$

$= \frac{\sqrt{6}-\sqrt{2}}{4}$

91. $\sin\frac{3\pi}{2}\tan\left(-\frac{15\pi}{4}\right) - \cos\left(-\frac{5\pi}{3}\right)$

$= (-1)(1) - \left(\frac{1}{2}\right)$

$= -1 - \frac{1}{2}$

$= -\frac{2}{2} - \frac{1}{2}$

$= -\frac{3}{2}$

Copyright © 2022 Pearson Education, Inc.

Trigonometry 3rd edition Blitzer Solutions Manual