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SKU: 9781305635128-SOLUTIONS

Chapter 2

Discrete-Time Signals and Systems

P2.1 Generate the following sequences using the basic MATLAB signal functions and the basic MATLAB signal operations discussed in this chapter. Plot signal samples using the `stem` function.

1. $x_1(n) = 3\delta(n+2) + 2\delta(n) - \delta(n-3) + 5\delta(n-7), -5 \leq n \leq 15$

```
% P0201a: x1(n) = 3*delta(n + 2) + 2*delta(n) - delta(n - 3) +
%                  5*delta(n - 7), -5 <= n <= 15.
clc; close all;
x1 = 3*impseq(-2,-5,15) + 2*impseq(0,-5,15) - impseq(3,-5,15) + 5*impseq(7,-5,15);
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0201a'); n1 = [-5:15];
Hs = stem(n1,x1,'filled'); set(Hs,'markersize',2);
axis([min(n1)-1,max(n1)+1,min(x1)-1,max(x1)+1]);
xlabel('n','FontSize',LFS); ylabel('x_1(n)','FontSize',LFS);
title('Sequence x_1(n)','FontSize',TFS);
set(gca,'XTickMode','manual','XTick',n1,'FontSize',8);
print -deps2 ../EPSFILES/P0201a;
```

The plots of $x_1(n)$ is shown in Figure 2.1.

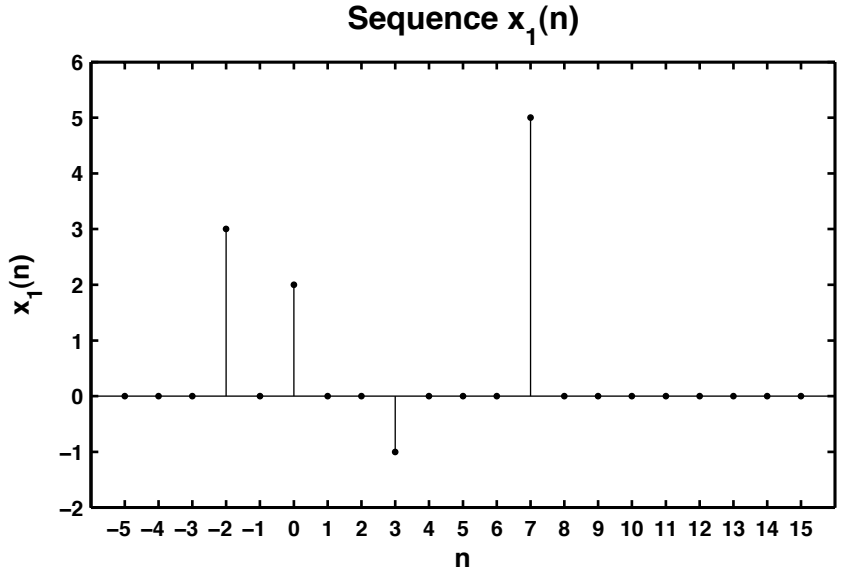


Figure 2.1: Problem P2.1.1 sequence plot

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2. $x_2(n) = \sum_{k=-5}^{5} e^{-|k|}\delta(n-2k), -10 \le n \le 10.$

```
% P0201b: x2(n) = sum_{k = -5}^{5} e^{-|k|}*delta(n - 2k), -10 <= n <= 10
clc; close all;

n2 = [-10:10]; x2 = zeros(1,length(n2));
for k = -5:5
    x2 = x2 + exp(-abs(k))*impseq(2*k ,-10,10);
end
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0201b');
Hs = stem(n2,x2,'filled'); set(Hs,'markersize',2);
axis([min(n2)-1,max(n2)+1,min(x2)-1,max(x2)+1]);
xlabel('n','FontSize',LFS); ylabel('x_2(n)','FontSize',LFS);
title('Sequence x_2(n)','FontSize',TFS);
set(gca,'XTickMode','manual','XTick',n2);
print -deps2 ../EPSFILES/P0201b;
```

The plots of $x_2(n)$ is shown in Figure 2.2.

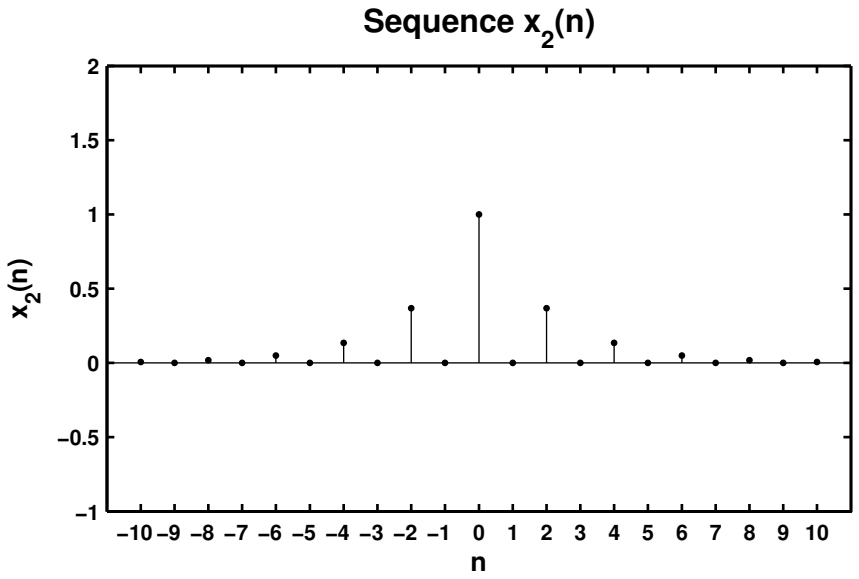


Figure 2.2: Problem P2.1.2 sequence plot

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3. $x_3(n) = 10u(n) - 5u(n-5) - 10u(n-10) + 5u(n-15)$.

```
% P0201c: x3(n) = 10u(n) - 5u(n - 5) + 10u(n - 10) + 5u(n - 15).
clc; close all;

x3 = 10*stepseq(0,0,20) - 5*stepseq(5,0,20) - 10*stepseq(10,0,20) ...
     + 5*stepseq(15,0,20);
n3 = [0:20];
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0201c');
Hs = stem(n3,x3,'filled'); set(Hs,'markersize',2);
axis([min(n3)-1,max(n3)+1,min(x3)-1,max(x3)+2]);
ytick = [-6:2:12];
xlabel('n','FontSize',LFS); ylabel('x_3(n)','FontSize',LFS);
title('Sequence x_3(n)','FontSize',TFS);
set(gca,'XTickMode','manual','XTick',n3);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../EPSFILES/P0201c;
```

The plots of $x_3(n)$ is shown in Figure 2.3.

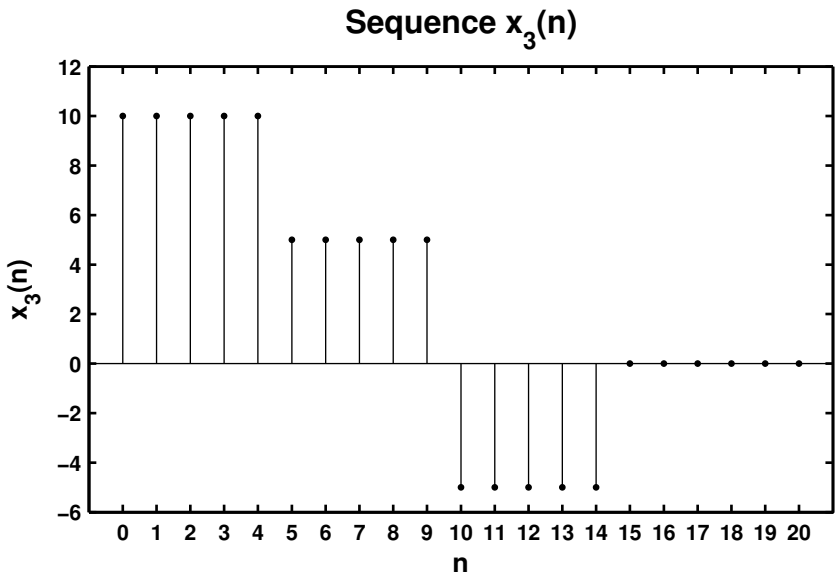


Figure 2.3: Problem P2.1.3 sequence plot

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4. $x_4(n) = e^{0.1n}[u(n+20) - u(n-10)]$.

```
% P0201d: x4(n) = e ^ {0.1n} [u(n + 20) - u(n - 10)].
clc; close all;

n4 = [-25:15];
x4 = exp(0.1*n4).*(stepseq(-20,-25,15) - stepseq(10,-25,15));

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0201d');
Hs = stem(n4,x4,'filled'); set(Hs,'markersize',2);
axis([min(n4)-2,max(n4)+2,min(x4)-1,max(x4)+1]);
xlabel('n','FontSize',LFS); ylabel('x_4(n)','FontSize',LFS);
title('Sequence x_4(n)','FontSize',TFS); ntick = [n4(1):5:n4(end)];
set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0201d; print -deps2 ../../Latex/P0201d;
```

The plots of $x_4(n)$ is shown in Figure 2.4.

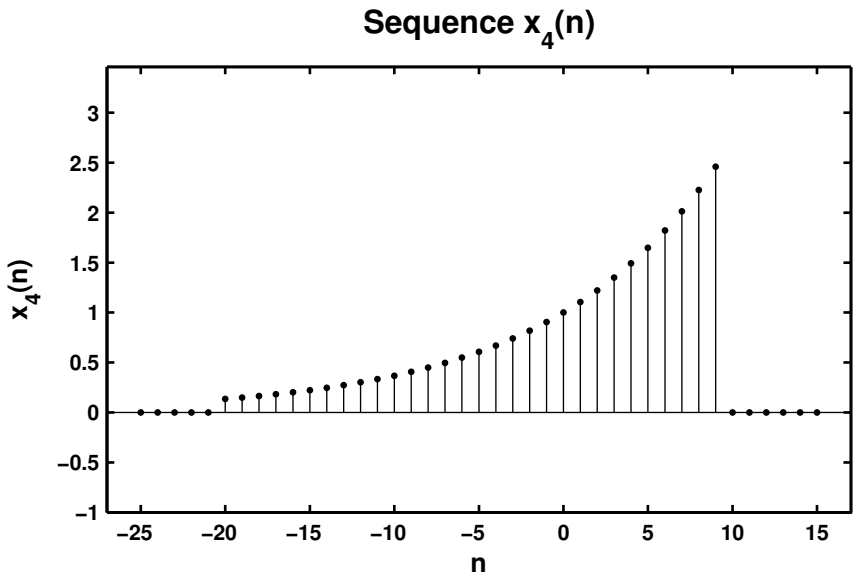


Figure 2.4: Problem P2.1.4 sequence plot

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5. $x_5(n) = 5[\cos(0.49\pi n) + \cos(0.51\pi n)]$, $-200 \le n \le 200$. Comment on the waveform shape.

```
% P0201e: x5(n) = 5[cos(0.49*pi*n) + cos(0.51*pi*n)], -200 <= n <= 200.
clc; close all;

n5 = [-200:200]; x5  = 5*(cos(0.49*pi*n5) + cos(0.51*pi*n5));

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0201e');
Hs = stem(n5,x5,'filled'); set(Hs,'markersize',2);
axis([min(n5)-10,max(n5)+10,min(x5)-2,max(x5)+2]);
xlabel('n','FontSize',LFS); ylabel('x_5(n)','FOntSize',LFS);
title('Sequence x_5(n)','FontSize',TFS);
ntick = [n5(1): 40:n5(end)]; ytick = [-12 -10:5:10 12];
set(gca,'XTickMode','manual','XTick',ntick);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../CHAP2_EPSFILES/P0201e; print -deps2 ../../Latex/P0201e;
```

The plots of $x_5(n)$ is shown in Figure 2.5.

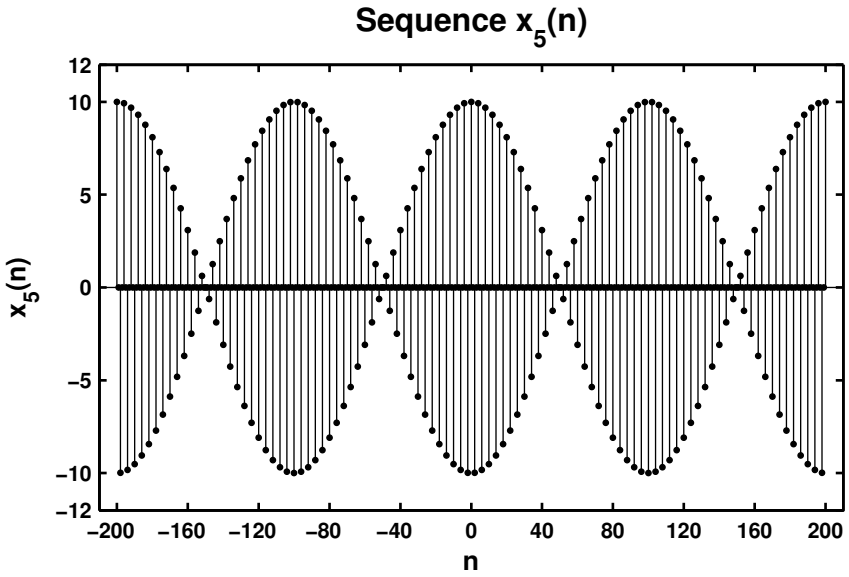


Figure 2.5: Problem P2.1.5 sequence plot

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6. $x_6(n) = 2\sin(0.01\pi n)\cos(0.5\pi n),\ -200 \le n \le 200.$

```
%P0201f: x6(n) = 2 sin(0.01*pi*n) cos(0.5*pi*n), -200 <= n <= 200.
clc; close all;

n6 = [-200:200]; x6 = 2*sin(0.01*pi*n6).*cos(0.5*pi*n6);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0201f');
Hs = stem(n6,x6,'filled'); set(Hs,'markersize',2);
axis([min(n6)-10,max(n6)+10,min(x6)-1,max(x6)+1]);
xlabel('n','FontSize',LFS); ylabel('x_6(n)','FontSize',LFS);
title('Sequence x_6(n)','FontSize',TFS);
ntick = [n6(1): 40:n6(end)];
set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0201f; print -deps2 ../../Latex/P0201f;
```

The plots of $x_6(n)$ is shown in Figure 2.6.

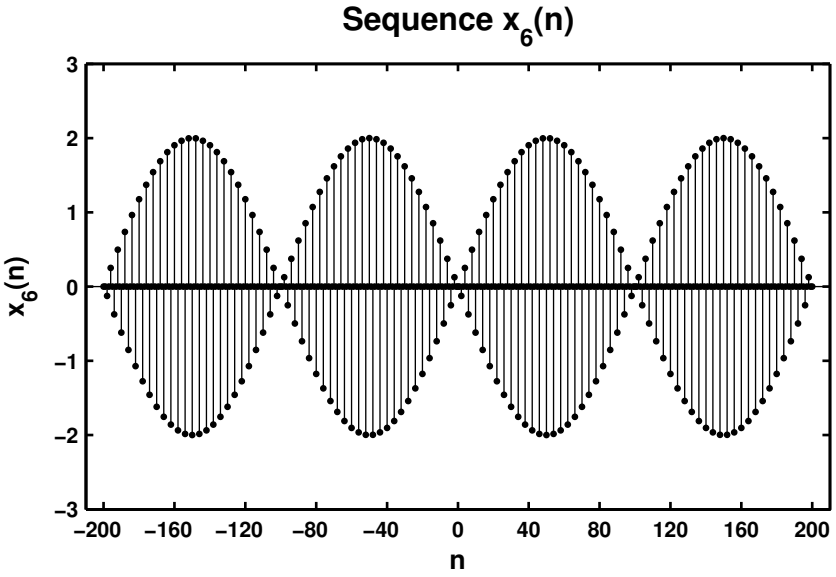


Figure 2.6: Problem P2.1.6 sequence plot

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7. $x_7(n) = e^{-0.05n}\sin(0.1\pi n + \pi/3),\ 0 \le n \le 100.$

```
% P0201g: x7(n) = e ^ {-0.05*n}*sin(0.1*pi*n + pi/3), 0 <= n <=100.
clc; close all;

n7 = [0:100]; x7  = exp(-0.05*n7).*sin(0.1*pi*n7 + pi/3);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0201g');
Hs = stem(n7,x7,'filled'); set(Hs,'markersize',2);
axis([min(n7)-5,max(n7)+5,min(x7)-1,max(x7)+1]);
xlabel('n','FontSize',LFS); ylabel('x_7(n)','FontSize',LFS);
title('Sequence x_7(n)','FontSize',TFS);
ntick = [n7(1): 10:n7(end)]; set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0201g;
```

The plots of $x_7(n)$ is shown in Figure 2.7.

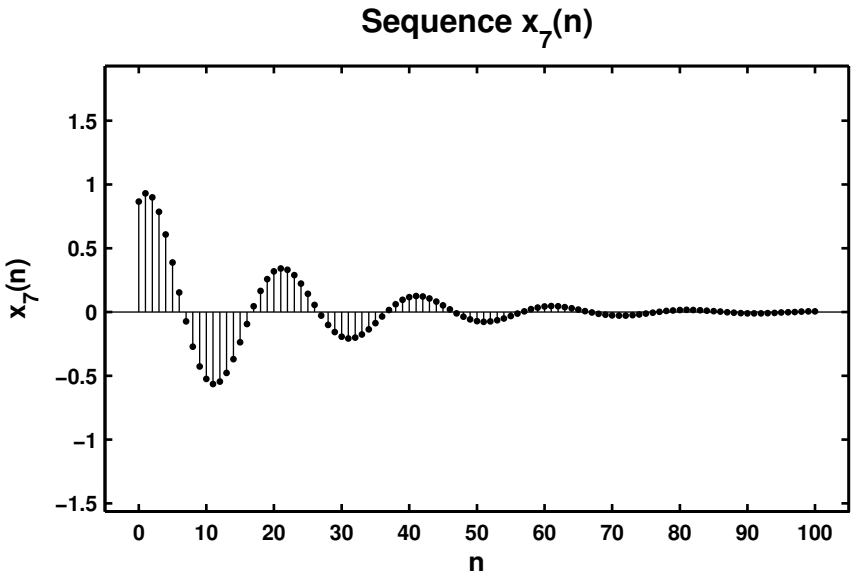


Figure 2.7: Problem P2.1.7 sequence plot

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8. $x_8(n) = e^{0.01n}\sin(0.1\pi n),\ 0 \le n \le 100.$

```
% P0201h: x8(n) = e ^ {0.01*n}*sin(0.1*pi*n), 0 <= n <=100.
clc; close all;

n8 = [0:100]; x8  = exp(0.01*n8).*sin(0.1*pi*n8);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0201h');
Hs = stem(n8,x8,'filled'); set(Hs,'markersize',2);
axis([min(n8)-5,max(n8)+5,min(x8)-1,max(x8)+1]);
xlabel('n','FontSize',LFS); ylabel('x_8(n)','FontSize',LFS);
title('Sequence x_8(n)','FontSize',TFS);
ntick = [n8(1): 10:n8(end)]; set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0201h
```

The plots of $x_8(n)$ is shown in Figure 2.8.

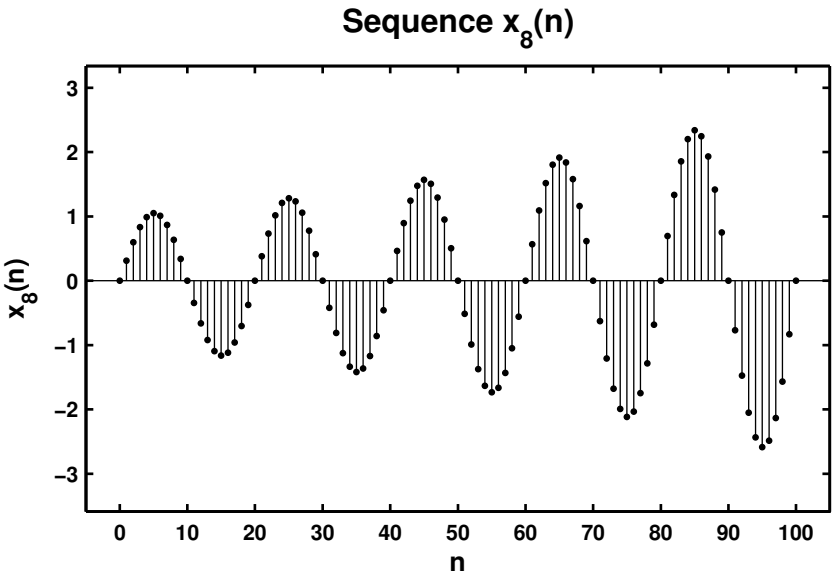


Figure 2.8: Problem P2.1.8 sequence plot

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P2.2 Generate the following random sequences and obtain their histogram using the `hist` function with 100 bins. Use the `bar` function to plot each histogram.

1. $x_1(n)$ is a random sequence whose samples are independent and uniformly distributed over $[0, 2]$ interval. Generate 100,000 samples.

```
% P0202a: x1(n) = uniform[0,2]
clc; close all;

n1 = [0:100000-1]; x1 = 2*rand(1,100000);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0202a');
[h1,x1out] = hist(x1,100); bar(x1out, h1);
axis([-0.1 2.1 0 1200]);
xlabel('interval','FontSize',LFS);
ylabel('number of elements','FontSize',LFS);
title('Histogram of sequence x_1(n) in 100 bins','FontSize',TFS);
print -deps2 ../CHAP2_EPSFILES/P0202a;
```

The plots of $x_1(n)$ is shown in Figure 2.9.

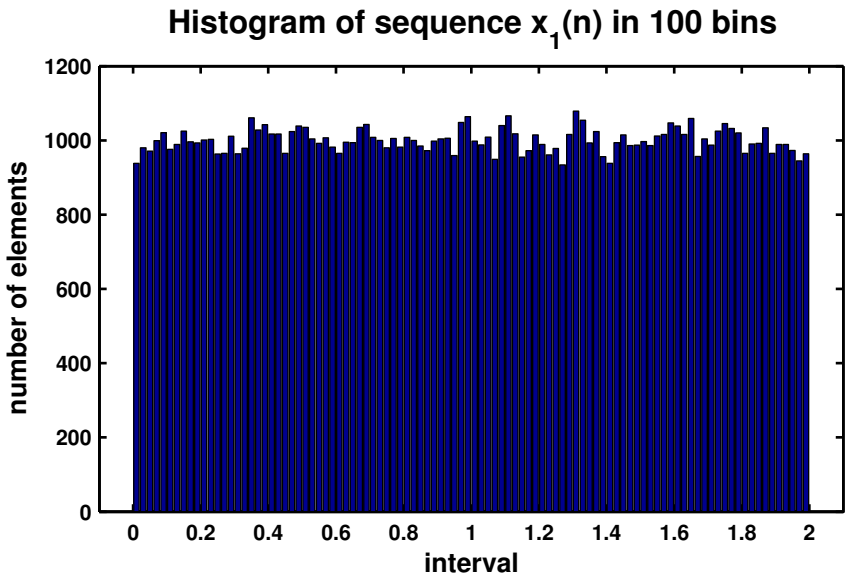


Figure 2.9: Problem P2.2.1 sequence plot

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2. $x_2(n)$ is a Gaussian random sequence whose samples are independent with mean 10 and variance 10. Generate 10,000 samples.

```
% P0202b: x2(n) = gaussian{10,10}
clc; close all;

n2 = [1:10000]; x2 = 10 + sqrt(10)*randn(1,10000);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0202b');
[h2,x2out] = hist(x2,100); bar(x2out,h2);
xlabel('interval','FontSize',LFS);
ylabel('number of elements','FontSize',LFS);
title('Histogram of sequence x_2(n) in 100 bins','FontSize',TFS);
print -deps2 ../CHAP2_EPSFILES/P0202b;
```

The plots of $x_2(n)$ is shown in Figure 2.10.

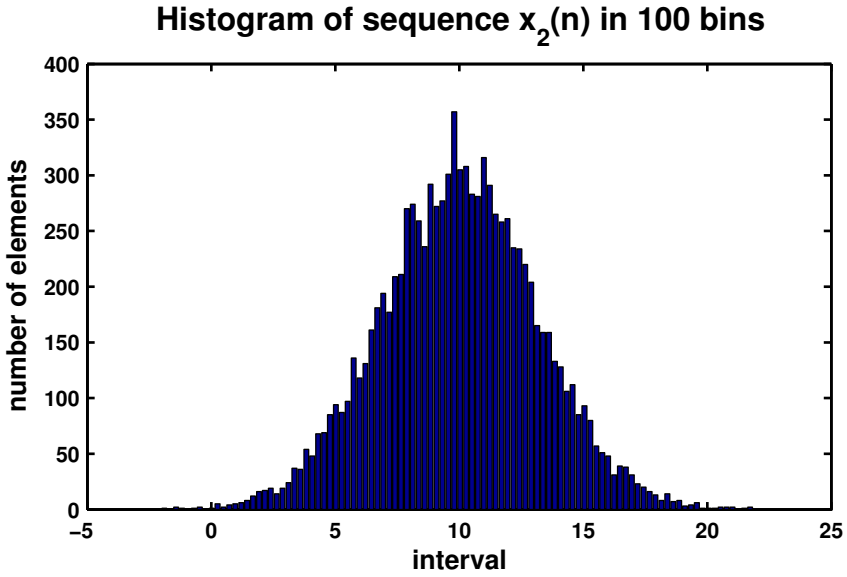


Figure 2.10: Problem P2.2.2 sequence plot

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3. $x_3(n) = x_1(n) + x_1(n-1)$ where $x_1(n)$ is the random sequence given in part 1 above. Comment on the shape of this histogram and explain the shape.

```
% P0202c: x3(n) = x1(n) + x1(n - 1) where  x1(n) = uniform[0,2]
clc; close all;

n1 = [0:100000-1]; x1 = 2*rand(1,100000);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0202c');
[x11,n11] = sigshift(x1,n1,1);
[x3,n3] = sigadd(x1,n1,x11,n11);
[h3,x3out] = hist(x3,100);
bar(x3out,h3); axis([-0.5 4.5 0 2500]);
xlabel('interval','FontSize',LFS);
ylabel('number of elements','FontSize',LFS);
title('Histogram of sequence x_3(n) in 100 bins','FontSize',TFS);
print -deps2 ../CHAP2_EPSFILES/P0202c;
```

The plots of $x_3(n)$ is shown in Figure 2.11.

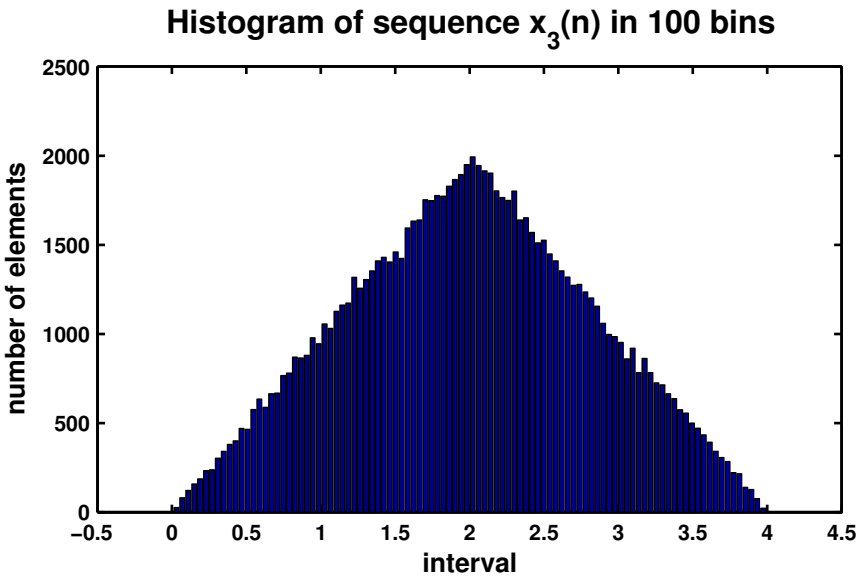


Figure 2.11: Problem P2.2.3 sequence plot

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4. $x_4(n) = \sum_{k=1}^{4} y_k(n)$ where each random sequence $y_k(n)$ is independent of others with samples uniformly distributed over $[-0.5, 0.5]$. Comment on the shape of this histogram.

```
%P0202d: x4(n) = sum_{k=1} ^ {4} y_k(n), where each independent of others
%        with samples uniformly distributed over [-0.5,0.5];
clc; close all;

y1 = rand(1,100000) - 0.5; y2 = rand(1,100000) - 0.5;
y3 = rand(1,100000) - 0.5; y4 = rand(1,100000) - 0.5;
x4 = y1 + y2 + y3 + y4;

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0202d');
[h4,x4out] = hist(x4,100); bar(x4out,h4);
xlabel('interval','FontSize',LFS);
ylabel('number of elements','FontSize',LFS);
title('Histogram of sequence x_4(n) in 100 bins','FontSize',TFS);
print -deps2 ../CHAP2_EPSFILES/P0202d;
```

The plots of $x_4(n)$ is shown in Figure 2.12.

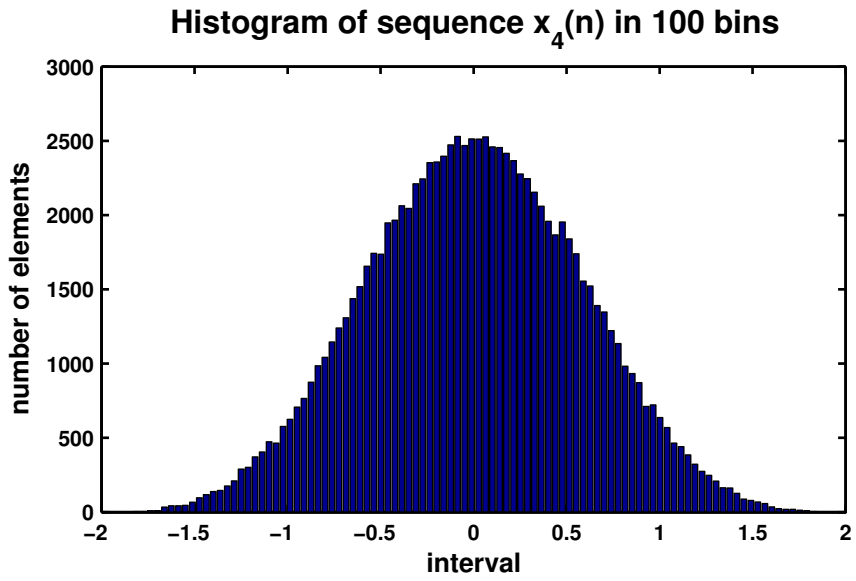


Figure 2.12: Problem P2.2.4 sequence plot

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P2.3 Generate the following periodic sequences and plot their samples (using the `stem` function) over the indicated number of periods.

1. $\tilde{x}_1(n) = \{\ldots, -2, -1, \underset{\uparrow}{0}, 1, 2, \ldots\}_{\text{periodic}}$. Plot 5 periods.

```
% P0203a: x1(n) = {...,-2,-1,0,1,2,-2,-1,0,1,2...} periodic. 5 periods
clc; close all;

n1 = [-12:12]; x1 = [-2,-1,0,1,2];
x1 = x1'*ones(1,5); x1 = (x1(:))';

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0203a');
Hs = stem(n1,x1,'filled'); set(Hs,'markersize',2);
axis([min(n1)-1,max(n1)+1,min(x1)-1,max(x1)+1]);
xlabel('n','FontSize',LFS); ylabel('x_1(n)','FontSize',LFS);
title('Sequence x_1(n)','FontSize',TFS);
ntick = [n1(1):2:n1(end)]; ytick = [min(x1) - 1:max(x1) + 1];
set(gca,'XTickMode','manual','XTick',ntick);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../CHAP2_EPSFILES/P0203a
```

The plots of $\tilde{x}_1(n)$ is shown in Figure 2.13.

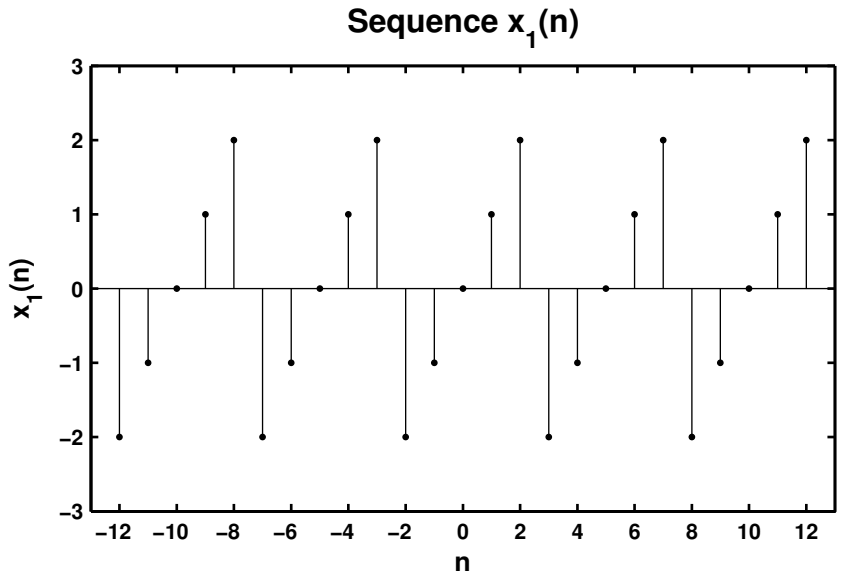


Figure 2.13: Problem P2.3.1 sequence plot

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2. $\tilde{x}_2(n) = e^{0.1n}[u(n) - u(n-20]_{\text{periodic}}$. Plot 3 periods.

```
% P0203b: x2 = e ^ {0.1n} [u(n) - u(n-20)] periodic. 3 periods
clc; close all;

n2 = [0:21]; x2 = exp(0.1*n2).*(stepseq(0,0,21)-stepseq(20,0,21));
x2 = x2'*ones(1,3); x2 = (x2(:))'; n2 = [-22:43];

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0203b');
Hs = stem(n2,x2,'filled'); set(Hs,'markersize',2);
axis([min(n2)-2,max(n2)+4,min(x2)-1,max(x2)+1]);
xlabel('n','FontSize',LFS); ylabel('x_2(n)','FontSize',LFS);
title('Sequence x_2(n)','FontSize',TFS);
ntick = [n2(1):4:n2(end)-5 n2(end)];
set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../Chap2_EPSFILES/P0203b;
```

The plots of $\tilde{x}_2(n)$ is shown in Figure 2.14.

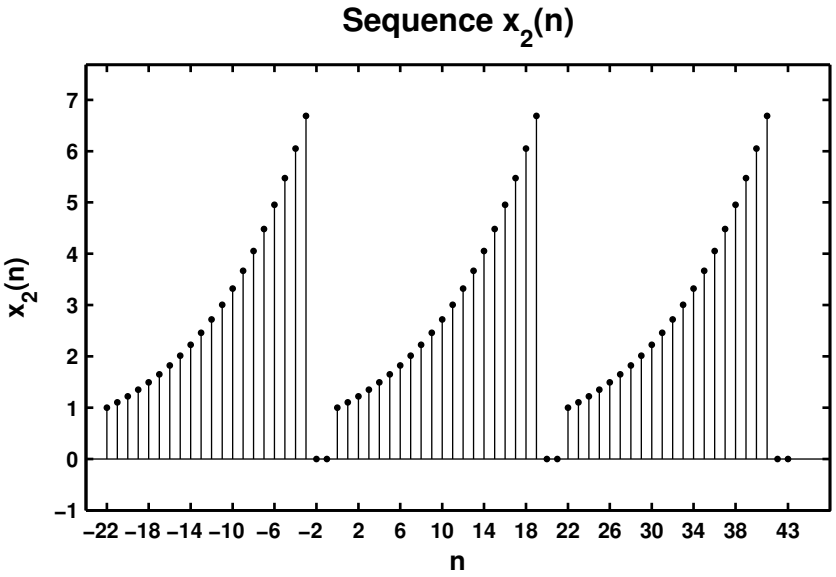


Figure 2.14: Problem P2.3.2 sequence plot

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3. $\tilde{x}_3(n) = sin(0.1\pi n)[u(n) - u(n-10)]$. Plot 4 periods.

```
% P0203c: x1(n) = {...,-2,-1,0,1,2,-2,-1,0,1,2...} periodic. 5 periods
clc; close all;

n3 = [0:11]; x3 = sin(0.1*pi*n3).*(stepseq(0,0,11)-stepseq(10,0,11));
x3 = x3'*ones(1,4); x3 = (x3(:))'; n3 = [-12:35];

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0203c');
Hs = stem(n3,x3,'filled'); set(Hs,'markersize',2);
axis([min(n3)-1,max(n3)+1,min(x3)-0.5,max(x3)+0.5]);
xlabel('n','FontSize',LFS); ylabel('x_3(n)','FontSize',LFS);
title('Sequence x_3(n)','FontSize',TFS);
ntick = [n3(1):4:n3(end)-3 n3(end)];
set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0203c;
```

The plots of $\tilde{x}_3(n)$ is shown in Figure 2.15.

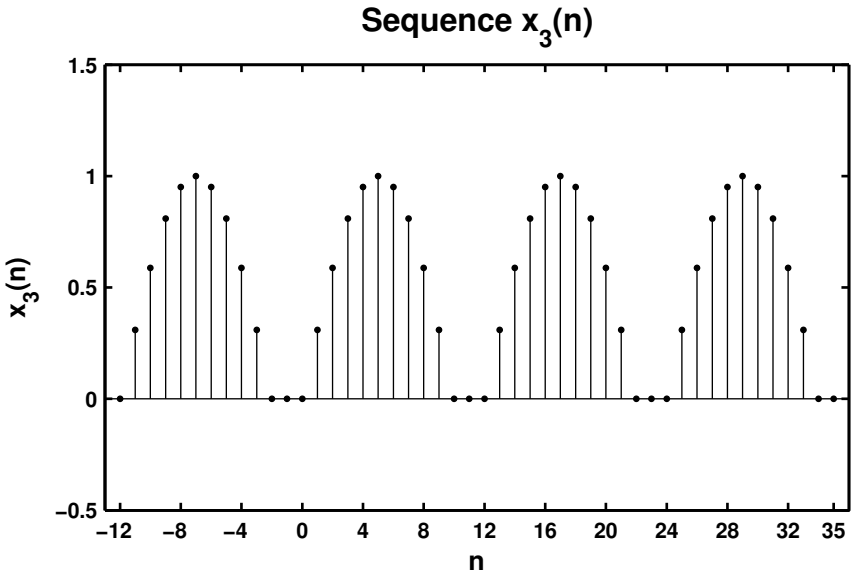


Figure 2.15: Problem P2.3.3 sequence plot

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4. $\tilde{x}_4(n) = \{\ldots, \underset{\uparrow}{1}, 2, 3, \ldots\}_{\text{periodic}} + \{\ldots, \underset{\uparrow}{1}, 2, 3, 4, \ldots\}_{\text{periodic}}$, $0 \le n \le 24$. What is the period of $\tilde{x}_4(n)$?

```
% P0203d x1(n) = {...,-2,-1,0,1,2,-2,-1,0,1,2...} periodic. 5 periods
clc; close all;

n4 = [0:24]; x4a = [1 2 3]; x4a = x4a'*ones(1,9); x4a = (x4a(:))';
x4b = [1 2 3 4]; x4b = x4b'*ones(1,7); x4b = (x4b(:))';
x4 = x4a(1:25) + x4b(1:25);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0203d');
Hs = stem(n4,x4,'filled'); set(Hs,'markersize',2);
axis([min(n4)-1,max(n4)+1,min(x4)-1,max(x4)+1]);
xlabel('n', 'FontSize', LFS); ylabel('x_4(n)','FontSize',LFS);
title('Sequence x_4(n):Period = 12','FontSize',TFS);
ntick = [n4(1) :2:n4(end)]; set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0203d;
```

The plots of $\tilde{x}_4(n)$ is shown in Figure 2.16. From the figure, the fundamental period of $\tilde{x}_4(n)$ is 12.

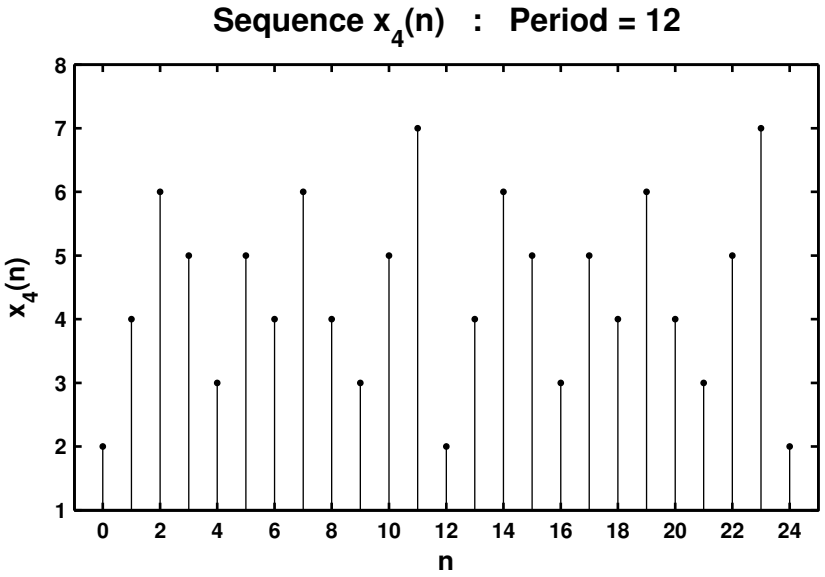


Figure 2.16: Problem P2.3.4 sequence plot

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P2.4 Let $x(n) = \{2, 4, -3, \underset{\uparrow}{1}, -5, 4, 7\}$. Generate and plot the samples (use the `stem` function) of the following sequences.

1. $x_1(n) = 2x(n-3) + 3x(n+4) - x(n)$

```
% P0204a: x(n) = [2,4,-3,1,-5,4,7]; -3 <=n <= 3;
% x1(n) = 2x(n - 3) + 3x(n + 4) - x(n)
clc; close all;

n = [-3:3]; x = [2,4,-3,1,-5,4,7];
[x11,n11] = sigshift(x,n,3);                          % shift by 3
[x12,n12] = sigshift(x,n,-4);                         % shift by -4
[x13,n13] = sigadd(2*x11,n11,3*x12,n12); % add two sequences
[x1,n1] = sigadd(x13,n13,-x,n);                % add two sequences

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0204a');
Hs = stem(n1,x1,'filled'); set(Hs,'markersize',2);
axis([min(n1)-1,max(n1)+1,min(x1)-3,max(x1)+1]);
xlabel('n','FontSize',LFS);
ylabel('x_1(n)','FontSize',LFS);
title('Sequence x_1(n)','FontSize',TFS); ntick = n1;
ytick = [min(x1)-3:5:max(x1)+1];
set(gca,'XTickMode','manual','XTick',ntick);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../CHAP2_EPSFILES/P0204a;
```

The plots of $x_1(n)$ is shown in Figure 2.17.

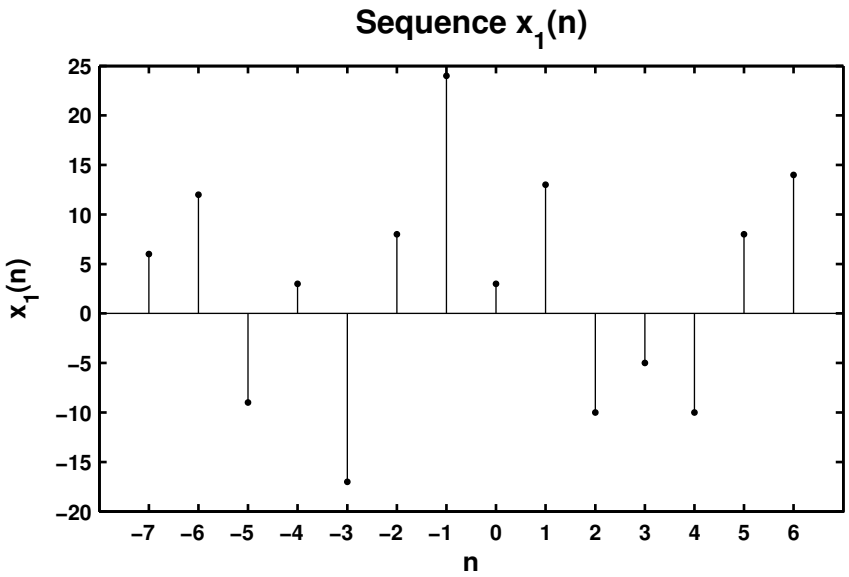


Figure 2.17: Problem P2.4.1 sequence plot

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2. $x_2(n) = 4x(4+n) + 5x(n+5) + 2x(n)$

```
% P0204b: x(n) = [2,4,-3,1,-5,4,7]; -3 <=n <= 3;
% x2(n) = 4x(4 + n) + 5x(n + 5) + 2x(n)
clc; close all;
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0204b');
n = [-3:3]; x = [2,4,-3,1,-5,4,7];

[x21,n21] = sigshift(x,n,-4);                      % shift by -4
[x22,n22] = sigshift(x,n,-5);                      % shift by -5
[x23,n23] = sigadd(4*x21,n21,5*x22,n22); % add two sequences
[x2,n2] = sigadd(x23,n23,2*x,n);           % add two sequences

Hs = stem(n2,x2,'filled'); set(Hs,'markersize',2);
axis([min(n2)-1,max(n2)+1,min(x2)-4,max(x2)+6]);
xlabel('n','FontSize',LFS); ylabel('x_2(n)','FontSize',LFS);
title('Sequence x_2(n)','FontSize',TFS); ntick = n2;
ytick = [-25 -20:10:60 65];
set(gca,'XTickMode','manual','XTick',ntick);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../CHAP2_EPSFILES/P0204b;
```

The plots of $x_2(n)$ is shown in Figure 2.18.

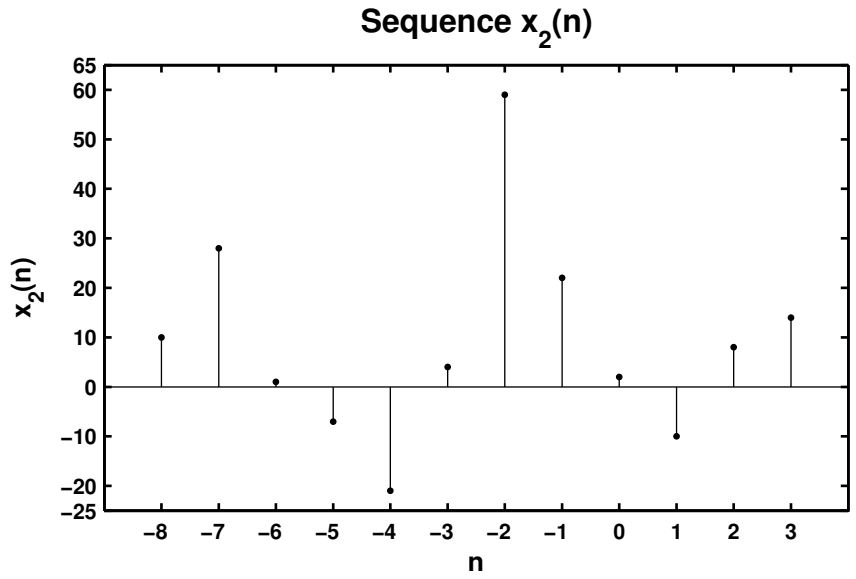


Figure 2.18: Problem P2.4.2 sequence plot

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3. $x_3(n) = x(n+3)x(n-2) + x(1-n)x(n+1)$

```
% P0204c: x(n) = [2,4,-3,1,-5,4,7]; -3 <=n <= 3;
%         x3(n) = x(n + 3)x(n - 2) + x(1 - n)x(n + 1)
clc; close all;

n = [-3:3]; x = [2,4,-3,1,-5,4,7];    % given sequence x(n)
[x31,n31] = sigshift(x,n,-3);           % shift sequence by -3
[x32,n32] = sigshift(x,n,2);            % shift sequence by 2
[x33,n33] = sigmult(x31,n31,x32,n32);   % multiply 2 sequences
[x34,n34] = sigfold(x,n);               % fold x(n)
[x34,n34] = sigshift(x34,n34,1);        % shift x(-n) by 1
[x35,n35] = sigshift(x,n,-1);           % shift x(n) by -1
[x36,n36] = sigmult(x34,n34,x35,n35);   % multiply 2 sequences
  [x3,n3] = sigadd(x33,n33,x36,n36);    % add 2 sequences

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0204c');
Hs = stem(n3,x3,'filled'); set(Hs,'markersize',2);
axis([min(n3)-1,max(n3)+1,min(x3)-10,max(x3)+10]);
xlabel('n','FontSize',LFS); ylabel('x_3(n)','FontSize',LFS);
title('Sequence x_3(n)','FontSize',TFS);
ntick = n3; ytick = [-30:10:60];
set(gca,'XTickMode','manual','XTick',ntick);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../CHAP2_EPSFILES/P0204c;
```

The plots of $x_3(n)$ is shown in Figure 2.19.

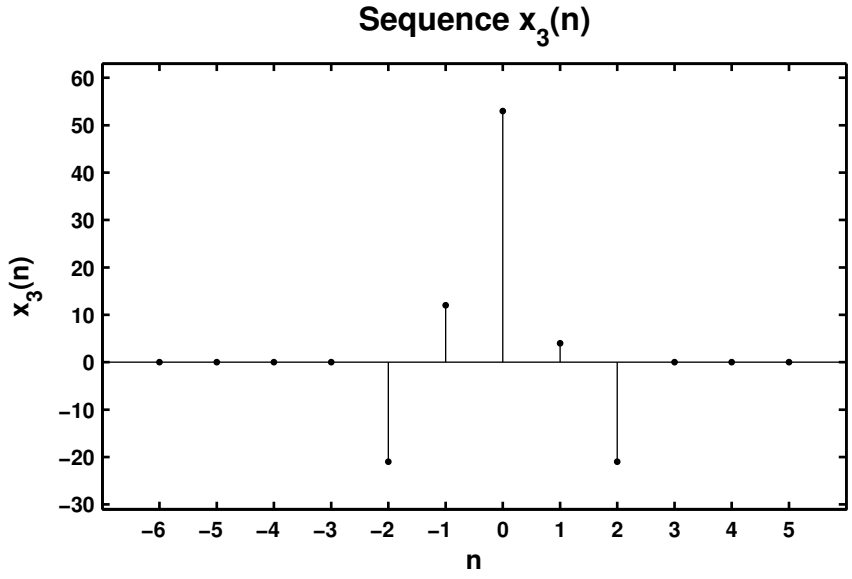


Figure 2.19: Problem P2.4.3 sequence plot

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4. $x_4(n) = 2e^{0.5n}x(n) + \cos(0.1\pi n)\,x(n+2)\,,\ -10 \le n \le 10$

```
% P0204d: x(n) = [2,4,-3,1,-5,4,7]; -3 <=n <= 3;
%         x4(n) = 2*e^{0.5n}*x(n)+cos(0.1*pi*n)*x(n+2), -10 <=n< =10
clc; close all;

n = [-3:3]; x = [2,4,-3,1,-5,4,7];        % given sequence x(n)
n4 = [-10:10]; x41 = 2*exp(0.5*n4); x412 = cos(0.1*pi*n4);
[x42,n42] = sigmult(x41,n4,x,n);
[x43,n43] = sigshift(x,n,-2);
[x44,n44] = sigmult(x412,n42,x43,n43);
  [x4,n4] = sigadd(x42,n42,x44,n44);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0204d');
Hs = stem(n4,x4,'filled'); set(Hs,'markersize',2);
axis([min(n4)-1,max(n4)+1,min(x4)-11,max(x4)+10]);
xlabel('n','FontSize',LFS); ylabel('x_4(n)','FontSize',LFS);
title('Sequence x_4(n)','FontSize',TFS);
ntick = n4; ytick = [ -20:10:70];
set(gca,'XTickMode','manual','XTick',ntick);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../CHAP2_EPSFILES/P0204d;
```

The plot of $x_4(n)$ is shown in Figure 2.20.

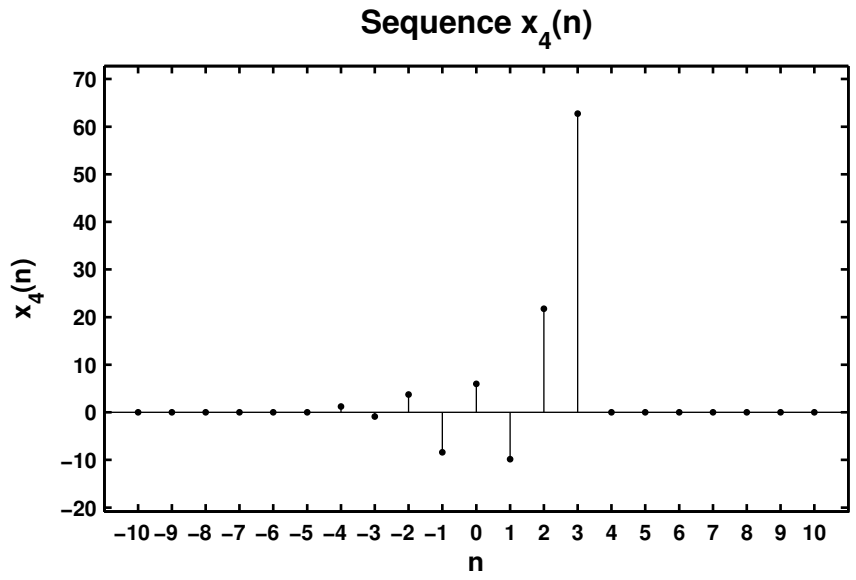


Figure 2.20: Problem P2.4.4 sequence plot

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P2.5 The complex exponential sequence $e^{j\omega_0 n}$ or the sinusoidal sequence $\cos(\omega_0 n)$ are periodic if the *normalized* frequency $f_0 \triangleq \dfrac{\omega_0}{2\pi}$ is a rational number; that is, $f_0 = \dfrac{K}{N}$, where K and N are integers.

1. Analytical proof: The exponential sequence is periodic if

$$e^{j2\pi f_0(n+N)} = e^{j2\pi f_0 n} \text{ or } e^{j2\pi f_0 N} = 1 \Rightarrow f_0 N = K \text{ (an integer)}$$

which proves the result.

2. $x_1 = \exp(0.1\pi n),\ -100 \le n \le 100.$

```
% P0205b: x1(n) = e^{0.1*j*pi*n} -100 <=n <=100
clc; close all;
n1 = [-100:100]; x1 = exp(0.1*j*pi*n1);
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0205b');
subplot(2,1,1); Hs1 = stem(n1,real(x1),'filled'); set(Hs1,'markersize',2);
axis([min(n1)-5,max(n1)+5,min(real(x1))-1,max(real(x1))+1]);
xlabel('n','FontSize',LFS); ylabel('Real(x_1(n))','FontSize',LFS);
title(['Real part of sequence x_1(n) = ' ...
       'exp(0.1 \times j \times pi \times n) ' char(10) ...
       ' Period = 20, K = 1, N = 20'],'FontSize',TFS);
ntick = [n1(1):20:n1(end)]; set(gca,'XTickMode','manual','XTick',ntick);
subplot(2,1,2); Hs2 = stem(n1,imag(x1),'filled'); set(Hs2,'markersize',2);
axis([min(n1)-5,max(n1)+5,min(real(x1))-1,max(real(x1))+1]);
xlabel('n','FontSize',LFS); ylabel('Imag(x_1(n))','FontSize',LFS);
title(['Imaginary part of sequence x_1(n) = ' ...
       'exp(0.1 \times j \times pi \times n) ' char(10) ...
       ' Period = 20, K = 1, N = 20'],'FontSize',TFS);
ntick = [n1(1):20:n1(end)]; set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0205b; print -deps2 ../../Latex/P0205b;
```

The plots of $x_1(n)$ is shown in Figure 2.21. Since $f_0 = 0.1/2 = 1/20$ the sequence is periodic. From the plot in Figure 2.21 we see that in one period of 20 samples $x_1(n)$ exhibits cycle. This is true whenever K and N are relatively prime.

3. $x_2 = \cos(0.1n),\ -20 \le n \le 20.$

```
% P0205c: x2(n) = cos(0.1n), -20 <= n <= 20
clc; close all;
n2 = [-20:20]; x2 = cos(0.1*n2);
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0205c');
Hs = stem(n2,x2,'filled'); set(Hs,'markersize',2);
axis([min(n2)-1,max(n2)+1,min(x2)-1,max(x2)+1]);
xlabel('n','FontSize',LFS); ylabel('x_2(n)','FontSize',LFS);
title(['Sequence x_2(n) = cos(0.1 \times n)' char(10) ...
       'Not periodic since f_0 = 0.1 / (2 \times \pi)' ...
       ' is not a rational number'], 'FontSize',TFS);
ntick = [n2(1):4:n2(end)]; set(gca,'XTickMode','manual','XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0205c;
```

The plots of $x_1(n)$ is shown in Figure 2.22. In this case f_0 is not a rational number and hence the sequence $x_2(n)$ is not periodic. This can be clearly seen from the plot of $x_2(n)$ in Figure 2.22.

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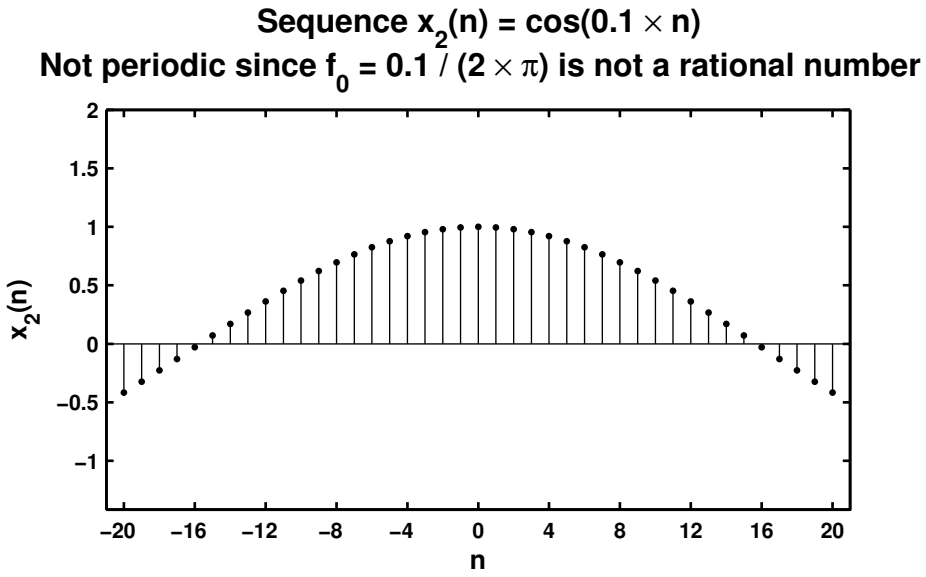


Figure 2.21: Problem P2.5.2 sequence plots

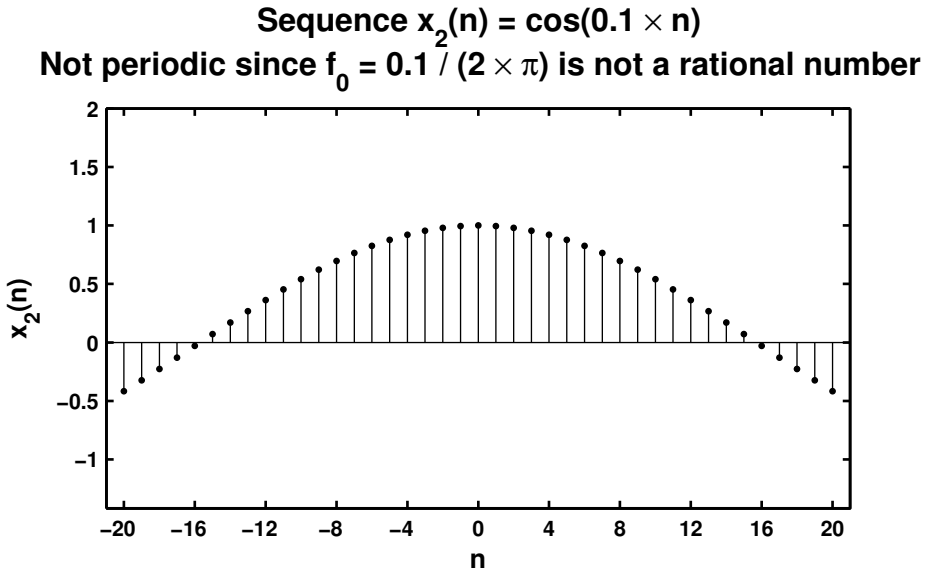


Figure 2.22: Problem P2.5.3 sequence plots

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P2.6 Using the `evenodd` function decompose the following sequences into their even and odd components. Plot these components using the `stem` function.

1. $x_1(n) = \{\underset{\uparrow}{0}, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$.

```
% P0206a: % Even odd decomposition of x1(n) = [0 1 2 3 4 5 6 7 8 9];
%                                        n  = 0:9;
clc; close all;

x1 = [0 1 2 3 4 5 6 7 8 9]; n1  = [0:9]; [xe1,xo1,m1] = evenodd(x1,n1);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0206a');
subplot(2,1,1); Hs = stem(m1,xe1,'filled'); set(Hs,'markersize',2);
axis([min(m1)-1,max(m1)+1,min(xe1)-1,max(xe1)+1]);
xlabel('n','FontSize',LFS); ylabel('x_e(n)','FontSize',LFS);
title('Even part of x_1(n)','FontSize',TFS);
ntick = [m1(1):m1(end)]; ytick = [-1:5];
set(gca,'XTick',ntick);set(gca,'YTick',ytick);
subplot(2,1,2); Hs = stem(m1,xo1,'filled'); set(Hs,'markersize',2);
axis([min(m1)-1,max(m1)+1,min(xo1)-2,max(xo1)+2]);
xlabel('n','FontSize',LFS); ylabel('x_o(n)','FontSize',LFS);
title('Odd part of x_1(n)','FontSize',TFS);
ntick = [m1(1):m1(end)]; ytick = [-6:2:6];
set(gca,'XTick',ntick);set(gca,'YTick',ytick);
print -deps2 ../CHAP2_EPSFILES/P0206a; print -deps2 ../../Latex/P0206a;
```

The plots of $x_1(n)$ is shown in Figure 2.23.

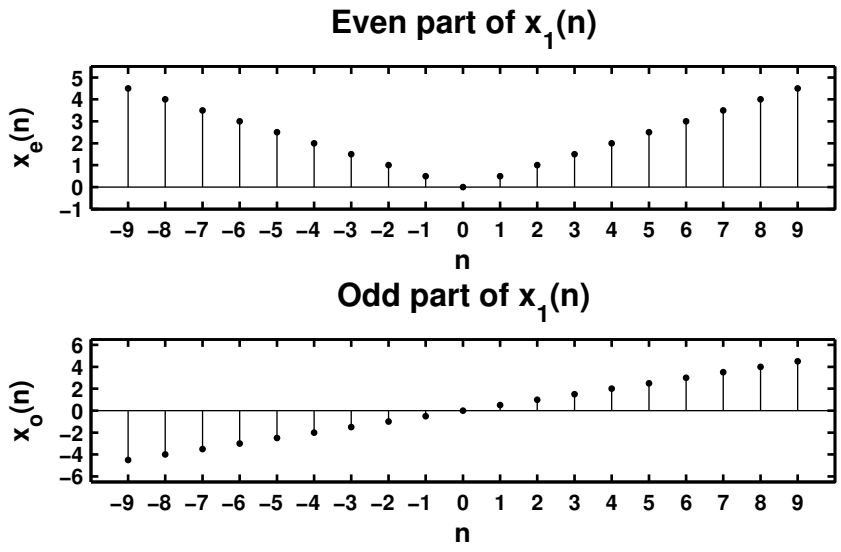


Figure 2.23: Problem P2.6.1 sequence plot

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2. $x_2(n) = e^{0.1n}[u(n+5) - u(n-10)]$.

```
% P0206b: Even odd decomposition of x2(n) = e ^ {0.1n} [u(n + 5) - u(n - 10)];
clc; close all;

n2 = [-8:12]; x2 = exp(0.1*n2).*(stepseq(-5,-8,12) - stepseq(10,-8,12));
[xe2,xo2,m2] = evenodd(x2,n2);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0206b');
subplot(2,1,1); Hs = stem(m2,xe2,'filled'); set(Hs,'markersize',2);
axis([min(m2)-1,max(m2)+1,min(xe2)-1,max(xe2)+1]);
xlabel('n','FontSize',LFS); ylabel('x_e(n)','FontSize',LFS);
title('Even part of x_2(n) = exp(0.1n) [u(n + 5) - u(n - 10)]',...
      'FontSize',TFS);
ntick = [m2(1):2:m2(end)]; set(gca,'XTick',ntick);
subplot(2,1,2); Hs = stem(m2,xo2,'filled'); set(Hs,'markersize',2);
axis([min(m2)-1,max(m2)+1,min(xo2)-1,max(xo2)+1]);
xlabel('n','FontSize',LFS); ylabel('x_o(n)','FontSize',LFS);
title('Odd part of x_2(n) = exp(0.1n) [u(n + 5) - u(n - 10)]',...
      'FontSize',TFS);
ntick = [m2(1) :2:m2(end)]; set(gca,'XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0206b; print -deps2 ../../Latex/P0206b;
```

The plots of $x_2(n)$ is shown in Figure 2.24.

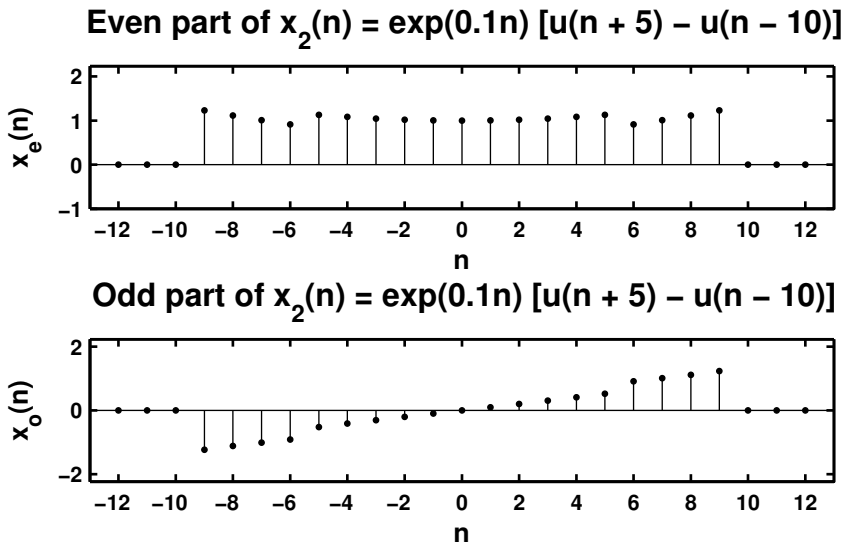


Figure 2.24: Problem P2.6.2 sequence plot

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3. $x_3(n) = \cos(0.2\pi n + \pi/4),\ -20 \le n \le 20.$

```
% P0206c: Even odd decomposition of x2(n) = cos(0.2*pi*n + pi/4);
%                                   -20 <= n <= 20;
clc; close all;

n3 = [-20:20]; x3 = cos(0.2*pi*n3 + pi/4);
[xe3,xo3,m3] = evenodd(x3,n3);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0206c');
subplot(2,1,1); Hs = stem(m3,xe3,'filled'); set(Hs,'markersize',2);
axis([min(m3)-2,max(m3)+2,min(xe3)-1,max(xe3)+1]);
xlabel('n','FontSize',LFS); ylabel('x_e(n)','FontSize',LFS);
title('Even part of x_3(n)  =  cos(0.2 \times \pi \times n + \pi/4)',...
      'FontSize',TFS);
ntick = [m3(1):4:m3(end)]; set(gca,'XTick',ntick);
subplot(2,1,2); Hs = stem(m3,xo3,'filled'); set(Hs,'markersize',2);
axis([min(m3)-2,max(m3)+2,min(xo3)-1,max(xo3)+1]);
xlabel('n','FontSize',LFS); ylabel('x_o(n)','FontSize',LFS);
title('Odd part of x_3(n)  =  cos(0.2 \times \pi \times n + \pi/4)',...
      'FontSize',TFS);
ntick = [m3(1):4 :m3(end)]; set(gca,'XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0206c; print -deps2 ../../Latex/P0206c;
```

The plots of $x_3(n)$ is shown in Figure 2.25.

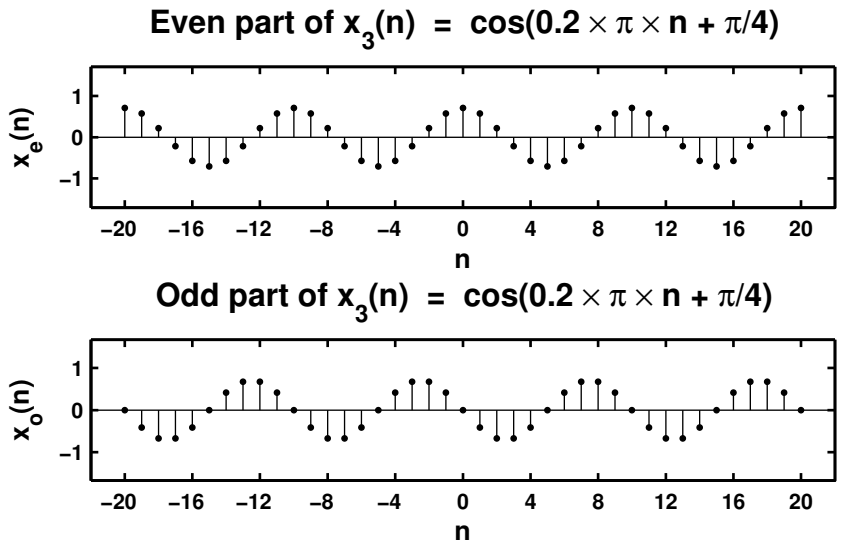


Figure 2.25: Problem P2.6.3 sequence plot

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4. $x_4(n) = e^{-0.05n}\sin(0.1\pi n + \pi/3),\ 0 \le n \le 100.$

```
% P0206d: x4(n) = e ^ {-0.05*n}*sin(0.1*pi*n + pi/3), 0 <= n <= 100
clc; close all;

n4 = [0:100]; x4 = exp(-0.05*n4).*sin(0.1*pi*n4 + pi/3);
[xe4,xo4,m4] = evenodd(x4,n4);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0206d');
subplot(2,1,1); Hs = stem(m4,xe4,'filled'); set(Hs,'markersize',2);
axis([min(m4)-10,max(m4)+10,min(xe4)-1,max(xe4)+1]);
xlabel('n','FontSize',LFS); ylabel('x_e(n)','FontSize',LFS);
title(['Even part of x_4(n) = ' ...
       'exp(-0.05 \times n) \times sin(0.1 \times \pi \times n + ' ...
       '\pi/3)'],'FontSize',TFS);
ntick = [m4(1):20:m4(end)]; set(gca,'XTick',ntick);

subplot(2,1,2); Hs = stem(m4,xo4,'filled'); set(Hs,'markersize',2);
axis([min(m4)-10,max(m4)+10,min(xo4)-1,max(xo4)+1]);
xlabel('n','FontSize',LFS); ylabel('x_o(n)','FontSize',LFS);
title(['Odd part of x_4(n) = ' ...
       'exp(-0.05 \times n) \times sin(0.1 \times \pi \times n + ' ...
       '\pi/3)'],'FontSize',TFS);
ntick = [m4(1):20 :m4(end)]; set(gca,'XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0206d; print -deps2 ../../Latex/P0206d;
```

The plots of $x_1(n)$ are shown in Figure 2.26.

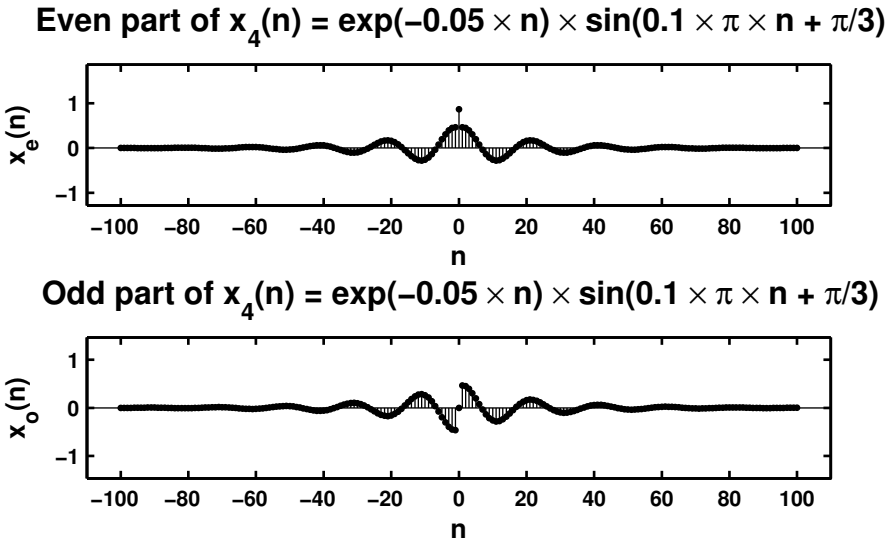


Figure 2.26: Problem P2.6.1 sequence plot

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P2.7 A complex-valued sequence $x_e(n)$ is called *conjugate-symmetric* if $x_e(n) = x_e^*(-n)$ and a complex-valued sequence $x_o(n)$ is called *conjugate-antisymmetric* if $x_o(n) = -x_o^*(-n)$. Then any arbitrary complex-valued sequence $x(n)$ can be decomposed into $x(n) = x_e(n) + x_o(n)$ where $x_e(n)$ and $x_o(n)$ are given by

$$x_e(n) = \tfrac{1}{2}\left[x(n) + x^*(-n)\right] \qquad \text{and} \qquad x_o(n) = \tfrac{1}{2}\left[x(n) - x^*(-n)\right] \tag{2.1}$$

respectively.

1. Modify the evenodd function discussed in the text so that it accepts an arbitrary sequence and decomposes it into its conjugate-symmetric and conjugate-antisymmetric components by implementing (2.1).

```
function [xe , xo , m] = evenodd_c(x , n)
% Complex-valued signal decomposition into even and odd parts (version-2)
% ------------------------------------------------------------------------
%[xe , xo , m] = evenodd_c(x , n);
%
[xc , nc] = sigfold(conj(x) , n);
[xe , m] = sigadd(0.5 * x , n , 0.5 * xc , nc);
[xo , m] = sigadd(0.5 * x , n , -0.5 * xc , nc);
```

2. $x(n) = 10\exp([-0.1 + \jmath 0.2\pi]n), \quad 0 \le n \le 10$

```
% P0207b: Decomposition of x(n) = 10*e ^ {(-0.1 + j*0.2*pi)*n},
%                                                  0 < = n <= 10
% into its conjugate symmetric and conjugate antisymmetric parts.
clc; close all;

n = [0:10]; x = 10*exp((-0.1+j*0.2*pi)*n); [xe,xo,neo] = evenodd(x,n);
Re_xe = real(xe); Im_xe = imag(xe); Re_xo = real(xo); Im_xo = imag(xo);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0207b');
subplot(2,2,1); Hs = stem(neo,Re_xe); set(Hs,'markersize',2);
ylabel('Re[x_e(n)]','FontSize',LFS); xlabel('n','FontSize',LFS);
axis([min(neo)-1,max(neo)+1,-5,12]);
ytick = [-5:5:15]; set(gca,'YTick',ytick);
title(['Real part of' char(10) 'even sequence x_e(n)'],'FontSize',TFS);

subplot(2,2,3); Hs = stem(neo,Im_xe); set(Hs,'markersize',2);
ylabel('Im[x_e(n)]','FontSize',LFS); xlabel('n','FontSize',LFS);
axis([min(neo)-1,max(neo)+1,-5,5]);
ytick = [-5:1:5]; set(gca,'YTick',ytick);
title(['Imaginary part of' char(10) 'even sequence x_e(n)'],'FontSize',TFS);

subplot(2,2,2); Hs = stem(neo,Re_xo); set(Hs,'markersize',2);
ylabel('Re[x_o(n)]','FontSize',LFS); xlabel('n','FontSize',LFS);
axis([min(neo)-1,max(neo)+1,-5,+5]);
ytick = [-5:1:5]; set(gca,'YTick',ytick);
title(['Real part of' char(10) 'odd sequence x_o(n)'],'FontSize',TFS);

subplot(2,2,4); Hs = stem(neo,Im_xo); set(Hs,'markersize',2);
ylabel('Im[x_o(n)]','FontSize',LFS); xlabel('n','FontSize',LFS);
axis([min(neo)-1,max(neo)+1,-5,5]);
ytick = [-5:1:5]; set(gca,'YTick',ytick);
title(['Imaginary part of' char(10) 'odd sequence x_o(n)'],'FontSize',TFS);
print -deps2 ../EPSFILES/P0207b;%print -deps2 ../../Latex/P0207b;
```

The plots of $x(n)$ are shown in Figure 2.27.

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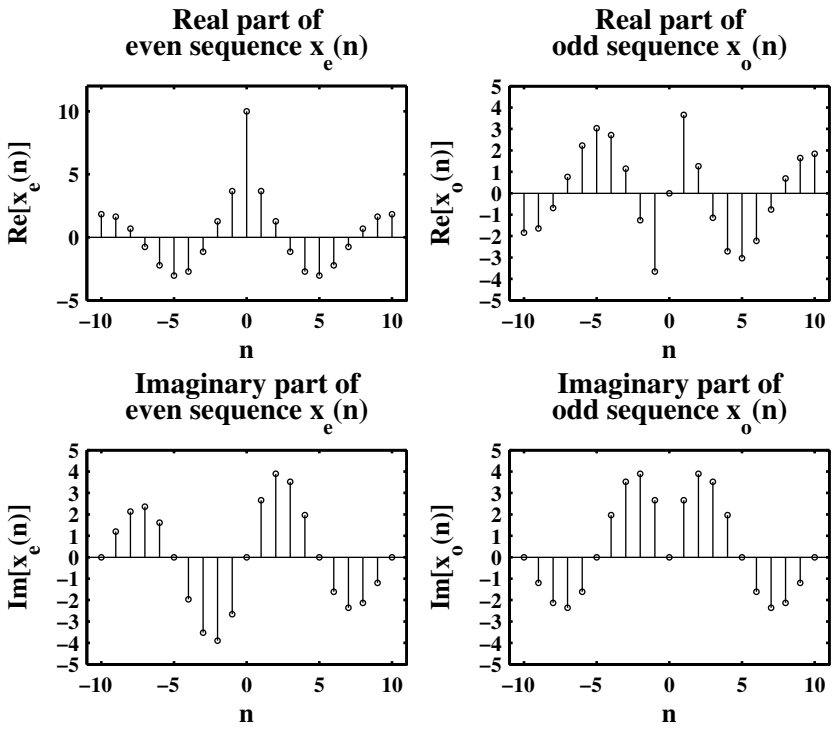


Figure 2.27: Problem P2.7.2 sequence plot

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P2.8 The operation of *signal dilation* (or *decimation* or *down-sampling*) is defined by $y(n) = x(nM)$ in which the sequence $x(n)$ is down-sampled by an integer factor M.

1. MATLAB function:

```
function [y,m] = dnsample(x,n,M)
% [y,m] = dnsample(x,n,M)
% Downsample sequence x(n) by a factor M to obtain y(m)
mb = ceil(n(1)/M)*M; me = floor(n(end)/M)*M;
nb = find(n==mb); ne = find(n==me);
y = x(nb:M:ne); m = fix((mb:M:me)/M);
```

2. $x_1(n) = \sin(0.125\pi n), \quad -50 \le n \le 50$. Decimation by a factor of 4.

```
% P0208b: x1(n) = sin(0.125*pi*n),-50 <= n <= 50
%         Decimate x(n) by a factor of 4 to obtain y(n)
clc; close all;
n1 = [-50:50]; x1 = sin(0.125*pi*n1); [y1,m1] = dnsample(x1,n1,4);
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0208b');
subplot(2,1,1); Hs = stem(n1,x1); set(Hs,'markersize',2);
xlabel('n','FontSize',LFS); ylabel('x(n)','FontSize',LFS);
title('Original sequence x_1(n)','FontSize',TFS);
axis([min(n1)-5,max(n1)+5,min(x1)-0.5,max(x1)+0.5]);
ytick = [-1.5:0.5:1.5]; ntick = [n1(1):10:n1(end)];
set(gca,'XTick',ntick); set(gca,'YTick',ytick);
subplot(2,1,2); Hs = stem(m1,y1); set(Hs,'markersize',2);
xlabel('n','FontSize',LFS); ylabel('y(n) = x(4n)','FontSize',LFS);
title('y_1(n)  =  Original sequence x_1(n) decimated by a factor of 4',...
      'FontSize',TFS);
axis([min(m1)-2,max(m1)+2,min(y1)-0.5,max(y1)+0.5]);
ytick = [-1.5:0.5:1.5]; ntick = [m1(1):2:m1(end)];
set(gca,'XTick',ntick); set(gca,'YTick',ytick);
print -deps2 ../CHAP2_EPSFILES/P0208b;
```

   The plots of $x_1(n)$ and $y_1(n)$ are shown in Figure 2.28. Observe that the original signal $x_1(n)$ can be recovered.

3. $x(n) = \sin(0.5\pi n), \quad -50 \le n \le 50$. Decimation by a factor of 4.

```
% P0208c: x2(n) = sin(0.5*pi*n),-50 <= n <= 50
%         Decimate x2(n) by a factor of 4 to obtain y2(n)
clc; close all;
n2 = [-50:50]; x2 = sin(0.5*pi*n2); [y2,m2] = dnsample(x2,n2,4);
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0208c');
subplot(2,1,1); Hs = stem(n2,x2); set(Hs,'markersize',2);
xlabel('n','FontSize',LFS); ylabel('x(n)','FontSize',LFS);
axis([min(n2)-5,max(n2)+5,min(x2)-0.5,max(x2)+0.5]);
title('Original sequence x_2(n)','FontSize',TFS);
ytick = [-1.5:0.5:1.5]; ntick = [n2(1):10:n2(end)];
set(gca,'XTick',ntick); set(gca,'YTick',ytick);
subplot(2,1,2); Hs = stem(m2,y2); set(Hs,'markersize',2);
xlabel('n','FontSize',LFS); ylabel('y(n) = x(4n)','FontSize',LFS);
axis([min(m2)-1,max(m2)+1,min(y2)-1,max(y2)+1]);
title('y_2(n) = Original sequence x_2(n) decimated by a factor of 4',...
      'FontSize',TFS);
ntick = [m2(1):2:m2(end)]; set(gca,'XTick',ntick);
print -deps2 ../CHAP2_EPSFILES/P0208c; print -deps2 ../../Latex/P0208c;
```

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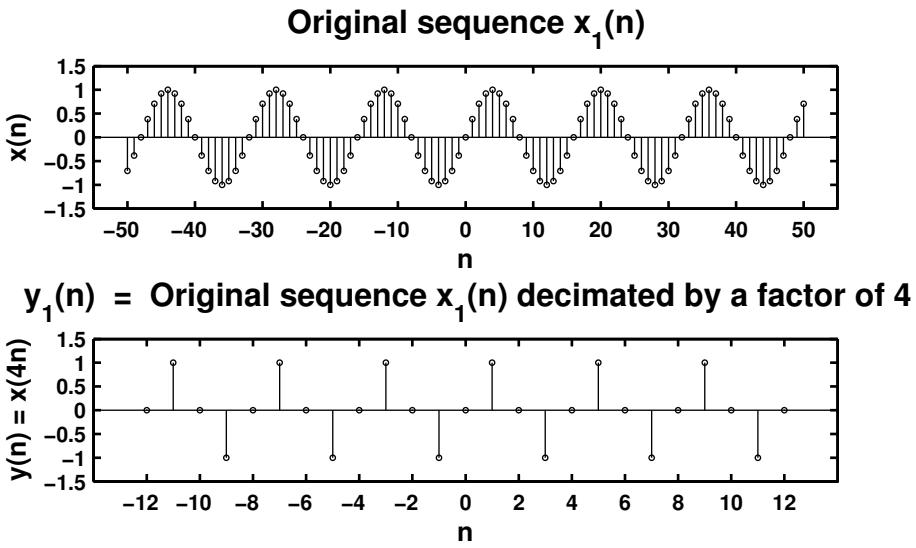


Figure 2.28: Problem P2.8.2 sequence plot

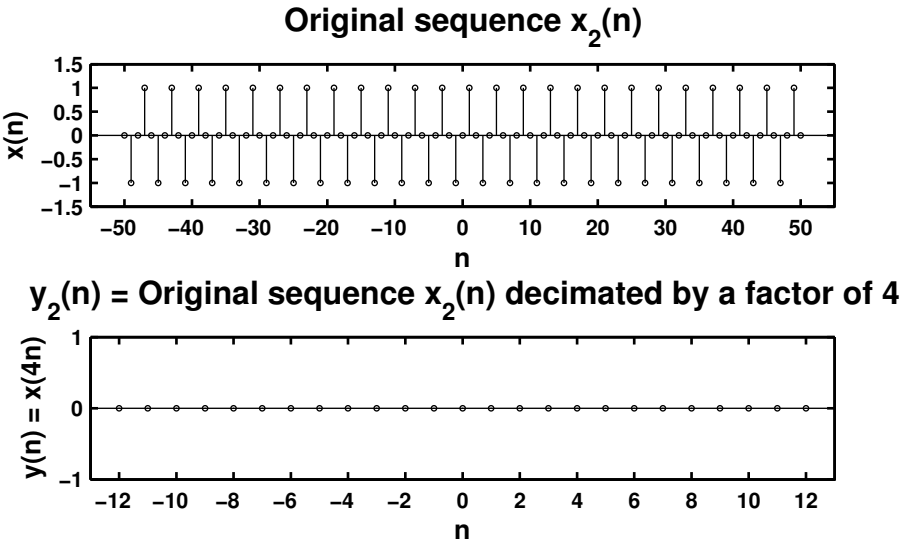


Figure 2.29: Problem P2.8.3 sequence plot

The plots of $x_2(n)$ and $y_2(n)$ are shown in Figure 2.29. Observe that the downsampled signal is a signal with zero frequency. Thus the original signal $x_2(n)$ is lost.

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P2.9 The autocorrelation sequence $r_{xx}(\ell)$ and the crosscorrelation sequence $r_{xy}(\ell)$ for the sequences:

$$x(n) = (0.9)^n\,, \quad 0 \le n \le 20; \qquad y(n) = (0.8)^{-n}, \quad -20 \le n \le 0$$

```
% P0209a: autocorrelation of sequence x(n) = 0.9 ^ n,  0 <= n <= 20
% using the conv_m function
clc; close all;

nx = [0:20]; x = 0.9 .^ nx; [xf,nxf] = sigfold(x,nx);
[rxx,nrxx] = conv_m(x,nx,xf,nxf);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0209a');
Hs = stem(nrxx,rxx); set(Hs,'markersize',2);
xlabel('n','FontSize',LFS); ylabel('r_x_x(n)','FontSize',LFS);
title('Autocorrelation of x(n)','FontSize',TFS);
axis([min(nrxx)-1,max(nrxx)+1,min(rxx),max(rxx)+1]);
ntick = [nrxx(1):4:nrxx(end)]; set(gca,'XTick',ntick);
%print -deps2 ../CHAP2_EPSFILES/P0209a;
```

The plot of the autocorrelation is shown in Figure 2.30.

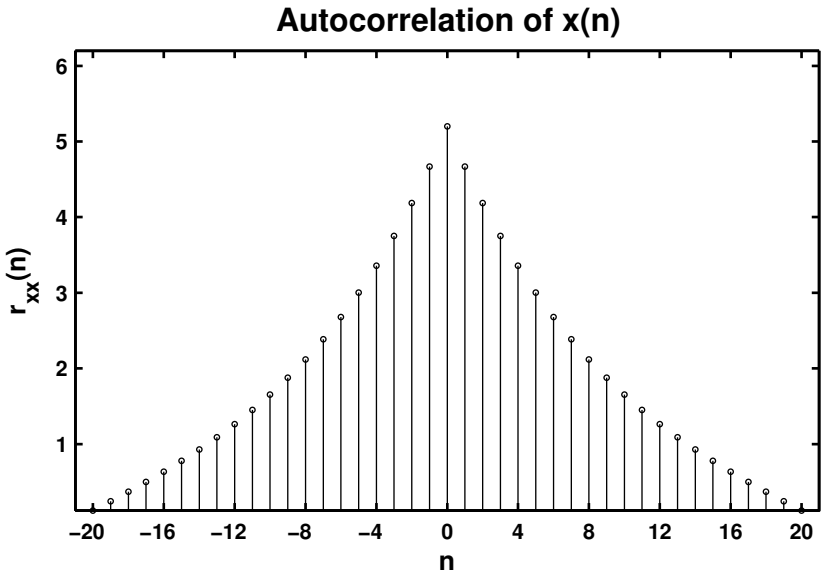


Figure 2.30: Problem P2.9 autocorrelation plot

```
% P0209b: crosscorrelation of sequence x(n) = 0.9 ^ n,  0 <= n <= 20
%         with sequence y = 0.8.^n,  -20 <=n <= 0 using the conv_m function
clc; close all;

nx = [0:20]; x = 0.9 .^ nx; ny = [-20:0]; y = 0.8 .^ (-ny);
[yf,nyf] = sigfold(y,ny); [rxy,nrxy] = conv_m(x,nx,yf,nyf);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0209b');
Hs = stem(nrxy,rxy); set(Hs,'markersize',3);
xlabel('n','FontSize',LFS); ylabel('r_x_y(n)','FontSize',LFS);
title('Crosscorrelation of x(n) and y(n)','FontSize',TFS);
```

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```
axis([min(nrxy)-1,max(nrxy)+1,floor(min(rxy)),ceil(max(rxy))]);
ytick = [0:1:4]; ntick = [nrxy(1):2:nrxy(end)];
set(gca,'XTick',ntick); set(gca,'YTick',ytick);
print -deps2 ../epsfiles/P0209b;
```

The plot of the crosscorrelation is shown in Figure 2.31.

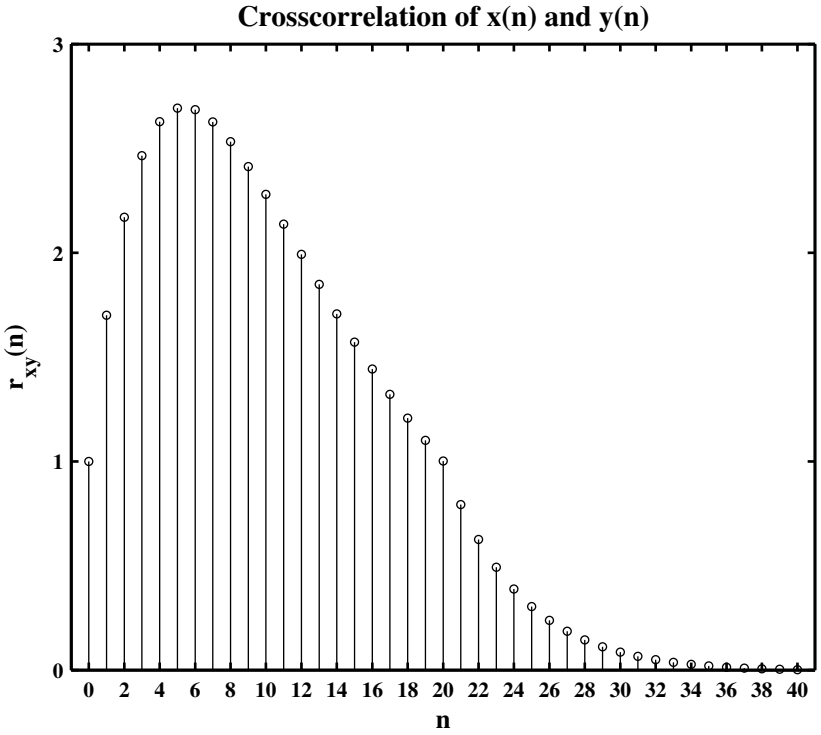


Figure 2.31: Problem P2.9 crosscorrelation plot

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P2.10 In a certain concert hall, echoes of the original audio signal $x(n)$ are generated due to the reflections at the walls and ceiling. The audio signal experienced by the listener $y(n)$ is a combination of $x(n)$ and its echoes. Let $y(n) = x(n) + \alpha x(n-k)$ where k is the amount of delay in samples and α is its relative strength. We want to estimate the delay using the correlation analysis.

1. Determine analytically the autocorrelation $r_{yy}(\ell)$ in terms of the autocorrelation $r_{xx}(\ell)$.
   Consider the autocorrelation $r_{yy}(\ell)$ of $y(n)$:

$$\begin{aligned} r_{yy}(\ell) &= \sum_{\ell} y(n)y(n-\ell) = \sum_{\ell} \{x(n) + \alpha x(n-k)\}\{x(n-\ell) + \alpha x(n-k-\ell)\} \\ &= \sum_{\ell} x(n)x(n-\ell) + \alpha \sum_{\ell} x(n)x(n-k-\ell) + \alpha \sum_{\ell} x(n-k)x(n-\ell) \\ &\quad + \alpha^2 \sum_{\ell} x(n-k)x(n-k-\ell) \\ &= r_{xx}(\ell) + \alpha r_{xx}(\ell+k) + \alpha r_{xx}(\ell-k) + \alpha^2 r_{xx}(\ell) \\ &= (1+\alpha^2) r_{xx}(\ell) + \alpha \big[r_{xx}(\ell+k) + r_{xx}(\ell-k) \big] \end{aligned}$$

2. Let $x(n) = \cos(0.2\pi n) + 0.5\cos(0.6\pi n)$, $\alpha = 0.1$, and $k = 50$. Generate 200 samples of $y(n)$ and determine its autocorrelation. Can you obtain α and k by observing $r_{yy}(\ell)$?
   MATLAB script:

```
% P0210c: autocorrelation of sequence y(n) = x(n) + alpha*x(n - k)
%                                          alpha = 0.1,k = 50
% x(n) = cos(0.2*pi*n) + 0.5*cos(0.6*pi*n)
clc; close all;
Hf_1 = figure;
set(Hf_1,'NumberTitle','off','Name','P0210c');
alpha = .1;
n = [-100:100];
%x = 3*rand(1,201)-1.5;
x = cos(0.2*pi*n) + 0.5*cos(0.6*pi*n);
[xf,nxf] = sigfold(x,n);
[rxx,nrxx] = conv_m(x,n,xf,nxf);

y = filter([1 zeros(1,49) alpha], 1, x);
[yf,nyf] = sigfold(y,n);
[ryx,nryx] = conv_m(y,n,xf,nxf);
[ryy,nryy] = conv_m(y,n,yf,nyf);

subplot(2,1,1);
Hs = stem(nrxx,rxx,'filled');
set(Hs,'markersize',2);
xlabel('n','FontSize',LFS);
ylabel('r_y_y(n)','FontSize',LFS);
title('autocorrelation of sequence x(n)','FontSize',TFS);
axis([-210, 210,-200,200]);
ntick = [-200:50:200];
ytick = [-200:50:200];
set(gca,'XTickMode','manual','XTick',ntick);
set(gca,'YTickMode','manual','YTick',ytick);

subplot(2,1,2);
Hs = stem(nryx,ryx,'filled');
```

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```
set(Hs,'markersize',2);
xlabel('n','FontSize',LFS);
ylabel('r_y_y(n)','FontSize',LFS);
title('autocorrelation of sequence y(n) = x(n) + 0.1 \times x(n - 50)' ,...
      'FontSize',TFS);
axis([-210,210,-200,200]);
ntick = [-200:50:200];
ytick = [-200:50:200];
set(gca,'XTickMode','manual','XTick',ntick);
set(gca,'YTickMode','manual','YTick',ytick);

print -deps2 ../CHAP2_EPSFILES/P0210b;
```

Stem plots of the autocorrelations are shown in Figure 2.32. We observe that it is not possible to visually separate components of $r_{xx}(\ell)$ In $r_{yy}(\ell)$ and hence it is not possible to estimate α or k.

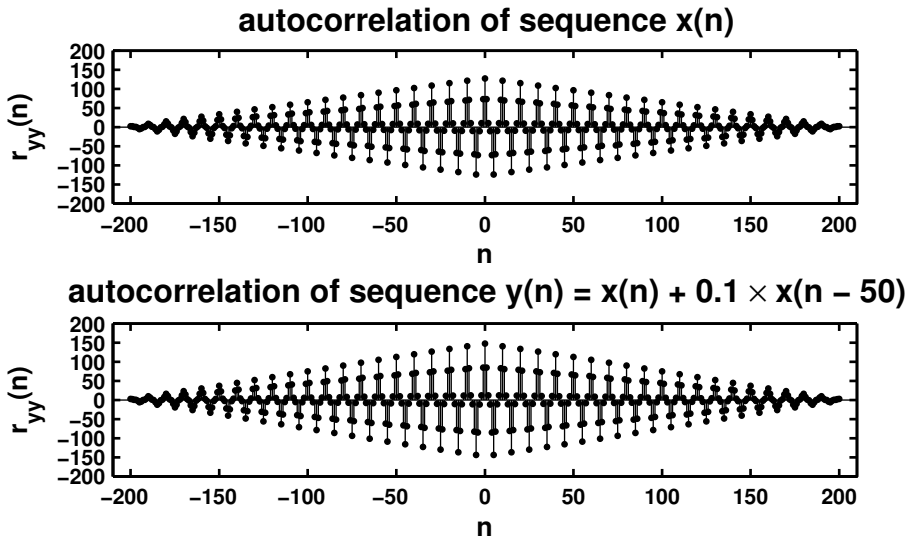


Figure 2.32: Problem P2.10 autocorrelation plot

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P2.11 Linearity of discrete-time systems.

System-1: $T_1[x(n)] = x(n)u(n)$

1. Analytic determination of linearity:

$$\begin{aligned} T_1[a_1x_1(n) + a_2x_2(n)] &= \{a_1x_1(n) + a_2x_2(n)\}u(n) = a_1x_1(n)u(n) + a_2x_2(n)u(n) \\ &= a_1T_1[x_1(n)] + a_2T_1[x_2(n)] \end{aligned}$$

   Hence the system $T_1[x(n)]$ is **linear**.

2. MATLAB script:

```
% P0211a: To prove that the system T1[x(n)] = x(n)u(n) is linear
clear; clc; close all;

n = 0:100; x1 = rand(1,length(n));
x2 = sqrt(10)*randn(1,length(n)); u = stepseq(0,0,100);
y1 = x1.*u; y2 = x2.*u; y = (x1 + x2).*u;
diff = sum(abs(y - (y1 + y2)));
if (diff < 1e-5)
    disp(' *** System-1 is Linear *** ');
else
    disp(' *** System-1 is NonLinear *** ');
end
```

   MATLAB verification:

```
>> *** System-1 is Linear ***
```

System-2: $T_2[x(n)] = x(n) + n\,x(n+1)$

1. Analytic determination of linearity:

$$\begin{aligned} T_2[a_1x_1(n) + a_2x_2(n)] &= \{a_1x_1(n) + a_2x_2(n)\} + n\,\{a_1x_1(n+1) + a_2x_2(n+1)\} \\ &= a_1\{x_1(n) + n\,x_1(n+1)\} + a_2\{x_2(n) + n\,x_2(n+1)\} \\ &= a_1T_2[x_1(n)] + a_2T_2[x_2(n)] \end{aligned}$$

   Hence the system is $T_2[x(n)]$ **linear**.

2. MATLAB script:

```
% P0211b: To prove that the system T2[x(n)] = x(n) + n*x(n+1) is linear
clear; clc; close all;

n = 0:100; x1 = rand(1,length(n)); x2 = sqrt(10)*randn(1,length(n));
z  = n; [x11,nx11] = sigshift(x1,n,-1);
[x111,nx111] = sigmult(z,n,x11,nx11); [y1,ny1] = sigadd(x1,n,x111,nx111);

[x21,nx21] = sigshift(x2,n,-1); [x211,nx211] = sigmult(z,n,x21,nx21);
[y2,ny2] = sigadd(x2,n,x211,nx211);
xs = x1 + x2; [xs1,nxs1] = sigshift(xs,n,-1);
[xs11,nxs11] = sigmult(z,n,xs1,nxs1); [y,ny] = sigadd(xs,n,xs11,nxs11);
diff = sum(abs(y - (y1 + y2)));
if (diff < 1e-5)
    disp(' *** System-2 is Linear *** ');
else
    disp(' *** System-2 is NonLinear *** ');
end
```

   MATLAB verification:

```
>> *** System-2 is Linear ***
```

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System-3: $T_3[x(n)] = x(n) + \frac{1}{2}x(n-2) - \frac{1}{3}x(n-3)x(2n)$

1. Analytic determination of linearity:

$$\begin{aligned} T_3[a_1x_1(n) + a_2x_2(n)] &= a_1x_1(n) + a_2x_2(n) + \tfrac{1}{2}\{a_1x_1(n-2) + a_2x_2(n-2)\} \\ &\quad - \tfrac{1}{3}\{a_1x_1(n-3) + a_2x_2(n-3)\}\{a_1x_1(2n) + a_2x_2(2n)\} \\ &= a_1\left\{x_1(n) + \tfrac{1}{2}x_1(n-2) - \tfrac{1}{3}a_1x_1(n-3)x_1(2n)\right\} \\ &\quad + a_2\left\{x_2(n) + \tfrac{1}{2}x_2(n-2) - \tfrac{1}{3}a_2x_2(n-3)x_2(2n)\right\} \\ &\quad + \tfrac{1}{3}\{a_1x_1(n-3)a_2x_2(2n) + a_2x_2(n-3)a_1x_1(2n)\} \end{aligned}$$

   which clearly is not equal to $a_1T_3[x_1(n)] + a_2T_3[x_2(n)]$. The product term in the input-output equation makes the system $T_3[x(n)]$ **nonlinear**.

2. MATLAB script:

```
% P0211c:  To prove that the system T3[x(n)] =   x(n) + 1/2*x(n - 2)
%                                        - 1/3*x(n - 3)*x(2n)
%          is linear
clear; clc; close all;

n = [0:100]; x1 = rand(1,length(n)); x2 = sqrt(10)*randn(1,length(n));
[x11,nx11] = sigshift(x1,n,2); x11 = 1/2*x11; [x12,nx12] = sigshift(x1,n,3);
x12 = -1/3*x12; [x13,nx13] = dnsample(x1,n,2);
[x14,nx14] = sigmult(x12,nx12,x13,nx13);
[x15,nx15] = sigadd(x11,nx11,x14,nx14);
[y1,ny1] = sigadd(x1,n,x15,nx15); [x21,nx21] = sigshift(x2,n,2);
x21 = 1/2*x21; [x22,nx22] = sigshift(x2,n,3);
x22 = -1/3*x22; [x23,nx23] = dnsample(x2,n,2);
[x24,nx24] = sigmult(x22,nx22,x23,nx23);
[x25,nx25] = sigadd(x21,nx21,x24,nx24); [y2,ny2] = sigadd(x2,n,x25,nx25);
xs = x1 + x2; [xs1,nxs1] = sigshift(xs,n,2);
xs1 = 1/2*xs1; [xs2,nxs2] = sigshift(xs,n,3); xs2 = -1/3*xs2;
[xs3,nxs3] = dnsample(xs,n,2); [xs4,nxs4] = sigmult(xs2,nxs2,xs3,nxs3);
[xs5,nxs5] = sigadd(xs1,nxs1,xs4,nxs4);
[y,ny] = sigadd(xs,n,xs5,nxs5); diff = sum(abs(y - (y1 + y2)));
if (diff < 1e-5)
    disp(' *** System-3 is Linear *** ');
else
    disp(' *** System-3 is NonLinear *** ');
end
```

   MATLAB verification:

```
>> *** System-3 is NonLinear ***
```

System-4: $T_4[x(n)] = \sum_{k=-\infty}^{n+5} 2x(k)$

1. Analytic determination of linearity:

$$\begin{aligned} T_4[a_1x_1(n) + a_2x_2(n)] &= \sum_{k=-\infty}^{n+5} 2\{a_1x_1(k) + a_2x_2(k)\} = a_1\sum_{k=-\infty}^{n+5} 2x_1(k) + a_2\sum_{k=-\infty}^{n+5} 2x_2(k) \\ &= a_1T_4[x_1(n)] + a_2T_4[x_2(n)] \end{aligned}$$

   Hence the system $T_4[x(n)]$ is **linear**.

2. MATLAB script:

```
% P0211d: To prove that the system T4[x(n)] = sum_{k=-infinity}^{n+5}2*x(k)
%         is linear
clear; clc; close all;
```

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```
n = [0:100]; x1 = rand(1,length(n)); x2 = sqrt(10)*randn(1,length(n));
y1 = cumsum(x1); ny1 = n - 5; y2 = cumsum(x2); ny2 = n - 5; xs = x1 + x2;
y = cumsum(xs); ny = n - 5; diff = sum(abs(y - (y1 + y2)));
if (diff < 1e-5)
    disp(' *** System-4 is Linear *** ');
else
    disp(' *** System-4 is NonLinear *** ');
end
```

MATLAB verification:

```
>> *** System-4 is Linear ***
```

System-5: $T_5[x(n)] = x(2n)$

1. Analytic determination of linearity:

$$T_5[a_1x_1(n) + a_2x_2(n)] = a_1x_1(2n) + a_2x_2(2n) = a_1T_5[x_1(n)] + a_2T_5[x_2(n)]$$

Hence the system $T_5[x(n)]$ is **linear**.

2. MATLAB script:

```
% P0211e: To prove that the system T5[x(n)] =   x(2n) is linear
clear; clc; close all;

n = 0:100; x1 = rand(1,length(n)); x2 = sqrt(10)*randn(1,length(n));
[y1,ny1] = dnsample(x1,n,2); [y2,ny2] = dnsample(x2,n,2); xs = x1 + x2;
[y,ny] = dnsample(xs,n,2); diff = sum(abs(y - (y1 + y2)));
if (diff < 1e-5)
    disp(' *** System-5 is Linear *** ');
else
    disp(' *** System-5 is NonLinear *** ');
end
```

MATLAB verification:

```
>> *** System-5 is Linear ***
```

System-6: $T_6[x(n)] = \text{round}[x(n)]$

1. Analytic determination of linearity:

$$T_6[a_1x_1(n) + a_2x_2(n)] = \text{round}[a_1x_1(n) + a_2x_2(n)] \neq a_1\,\text{round}[x_1(n)] + a_2\,\text{round}[x_2(n)]$$

Hence the system $T_6[x(n)]$ is **nonlinear**.

2. MATLAB script:

```
% P0211f: To prove that the system T6[x(n)] =   round(x(n)) is linear
clear; clc; close all;

n = 0:100; x1 = rand(1,length(n)); x2 = sqrt(10)*randn(1,length(n));
y1 = round(x1); y2 = round(x2); xs = x1 + x2;
y  = round(xs); diff = sum(abs(y - (y1 + y2)));
if (diff < 1e-5)
    disp(' *** System-6 is Linear *** ');
else
    disp(' *** System-6 is NonLinear *** ');
end
```

MATLAB verification:

```
>> *** System-6 is NonLinear ***
```

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P2.12 Time-invariance of discrete-time systems.

System-1: $T_1[x(n)] \triangleq y(n) = x(n)u(n)$

1. Analytic determination of time-invariance:

$$T_1[x(n-k)] = x(n-k)u(n) \neq x(n-k)u(n-k) = y(n-k)$$

Hence the system $T_1[x(n)]$ is **time-varying**.

2. MATLAB script:

```
% P0212a: To determine whether T1[x(n)] = x(n)u(n) is time invariant
clear; clc; close all;

n = 0:100; x = sqrt(10)*randn(1,length(n)); u = stepseq(0,0,100);
y = x.*u; [y1,ny1] = sigshift(y,n,1); [x1,nx1] = sigshift(x,n,1);
[y2,ny2] = sigmult(x1,nx1,u,n); [diff,ndiff] = sigadd(y1,ny1,-y2,ny2);
diff = sum(abs(diff));
if (diff < 1e-5)
    disp(' *** System-1 is Time-Invariant *** ');
else
    disp(' *** System-1 is Time-Varying *** ');
end
```

MATLAB verification:

```
>> *** System-1 is Time-Varying ***
```

System-2: $T_2[x(n)] \triangleq y(n) = x(n) + n\,x(n+1)$

1. Analytic determination of time-invariance:

$$T_2[x(n-k)] = x(n-k) + n\,x(n-k+1) \neq x(n-k) + (n-k)\,x(n-k+1) = y(n-k)$$

Hence the system is $T_2[x(n)]$ **time-varying**.

2. MATLAB script:

```
% P0212b: To determine whether the system T2[x(n)] = x(n) + n*x(n + 1) is
%         time-invariant
clear; clc; close all;

n = 0:100; x = sqrt(10)*randn(1,length(n));
z  = n; [x1,nx1] = sigshift(x,n,-1);
[x11,nx11] = sigmult(z,n,x1,nx1); [y,ny] = sigadd(x,n,x11,nx11);
[y1,ny1] = sigshift(y,ny ,1); [xs,nxs]  = sigshift(x,n,1);
[xs1,nxs1] = sigshift(xs,nxs,-1); [xs11,nxs11] = sigmult(z,n,xs1,nxs1);
[y2,ny2] = sigadd(xs,nxs,xs11,nxs11); [diff,ndiff] = sigadd(y1,ny1,-y2,ny2);
diff = sum(abs(diff));
if (diff < 1e-5)
    disp(' *** System-2 is Time-Invariant *** ');
else
    disp(' *** System-2 is Time-Varying *** ');
end
```

MATLAB verification:

```
>> *** System-1 is Time-Varying ***
```

System-3: $T_3[x(n)] \triangleq y(n) = x(n) + \frac{1}{2}x(n-2) - \frac{1}{3}x(n-3)x(2n)$

1. Analytic determination of time-invariance:

$$\begin{aligned} T_3[x(n-k)] &= x(n-k) + \frac{1}{2}x(n-k-2) - \frac{1}{3}x(n-k-3)x(2n-k) \\ &\neq x(n-k) + \frac{1}{2}x(n-k-2) - \frac{1}{3}x(n-k-3)x(2n-2k) = y(n-k) \end{aligned}$$

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Hence the system is $T_3[x(n)]$ **time-varying**.

2. MATLAB script:

```
% P0212c: To find whether the system T3[x(n)] =   x(n) + 1/2*x(n - 2)
%                                        - 1/3*x(n - 3)*x(2n)
%                                          is time invariant
clear; clc; close all;

n = 0:100; x = sqrt(10)*randn(1,length(n)); [x1,nx1] = sigshift(x,n,2);
 x1 = 1/2*x1; [x2,nx2] = sigshift(x,n,3);  x2 = -1/3*x2;
[x3,nx3] = dnsample(x,n,2); [x4,nx4] = sigmult(x2,nx2,x3,nx3);
[x5,nx5] = sigadd(x1,nx1,x4,nx4); [y,ny]   = sigadd(x,n,x5,nx5);
[y1,ny1] = sigshift(y,ny,1); [xs,nxs] = sigshift(x,n,1);
[xs1,nxs1] = sigshift(xs,nxs,2); xs1 = 1/2*xs1;
[xs2,nxs2] = sigshift(xs,nxs,3); xs2 = -1/3*xs2;
[xs3,nxs3] = dnsample(xs,nxs,2); [xs4,nxs4] = sigmult(xs2,nxs2,xs3,nxs3);
[xs5,nxs5] = sigadd(xs1,nxs1,xs4,nxs4); [y2,ny2] = sigadd(xs,nxs,xs5,nxs5);
[diff,ndiff] = sigadd(y1,ny1,-y2,ny2); diff = sum(abs(diff));
if (diff < 1e-5)
    disp(' *** System-3 is Time-Invariant *** ');
else
    disp(' *** System-3 is Time-Varying *** ');
end
```

MATLAB verification:

```
>> *** System-3 is Time-Varying ***
```

System-4: $T_4[x(n)] \triangleq y(n) = \sum_{k=-\infty}^{n+5} 2x(k)$

1. Analytic determination of time-invariance:

$$T_4[x(n-\ell)] = \sum_{k=-\infty}^{n+5} 2x(k-\ell) = \sum_{k=-\infty}^{n-\ell+5} 2x(k) = y(n-\ell)$$

Hence the system $T_4[x(n)]$ is **time-invariant**.

2. MATLAB script:

```
% P0212d: To find whether the system T4[x(n)]=sum_{k=-infinity}^{n+5}2*x(k)
%         is time-invariant
clear; clc; close all;
n = 0:100; x = sqrt(10)*randn(1,length(n)); y = cumsum(x); ny = n - 5;
[y1,ny1] = sigshift(y,ny,-1); [xs,nxs] = sigshift(x,n,-1); y2 = cumsum(xs);
ny2 = nxs - 5; [diff,ndiff] = sigadd(y1,ny1,-y2,ny2); diff = sum(abs(diff));
if (diff < 1e-5)
    disp(' *** System-4 is Time-Invariant *** ');
else
    disp(' *** System-4 is Time-Varying *** ');
end
```

MATLAB verification:

```
>> *** System-4 is Time-Invariant ***
```

System-5: $T_5[x(n)] \triangleq y(n) = x(2n)$

1. Analytic determination of time-invariance:

$$T_5[x(n-k)] = x(2n-k) \neq x[2(n-k)] = y(n-k)$$

Hence the system $T_5[x(n)]$ is **time-varying**.

2. MATLAB script:

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```
% P0212e: To determine whether the system T5[x(n)] = x(2n) is time-invariant
clear; clc; close all;
n = 0:100; x = sqrt(10)*randn(1,length(n)); [y,ny] = dnsample(x,n,2);
[y1,ny1] = sigshift(y,ny,1); [xs,nxs] = sigshift(x,n,1);
[y2,ny2] = dnsample(xs,nxs,2); [diff,ndiff] = sigadd(y1,ny1,-y2,ny2);
diff = sum(abs(diff));
if (diff < 1e-5)
    disp(' *** System-5 is Time-Invariant *** ');
else
    disp(' *** System-5 is Time-Varying *** ');
end
```

MATLAB verification:

```
>> *** System-5 is Time-Varying ***
```

System-6: $T_6[x(n)] \triangleq y(n) = \text{round}[x(n)]$

1. Analytic determination of time-invariance:

$$T_6[x(n-k)] = \text{round}[x(n-k)] = y(n-k)$$

Hence the system $T_6[x(n)]$ is **time-invariant**.

2. MATLAB script:

```
% P0212f: To determine if the system T6[x(n)]=round(x(n)) is time-invariant
clear; clc; close all;
n = 0:100; x = sqrt(10)*randn(1,length(n)); y = round(x); ny = n;
[y1,ny1] = sigshift(y,ny,1); [xs,nxs] = sigshift(x,n,1); y2  = round(xs);
ny2 = nxs; [diff,ndiff] = sigadd(y1,ny1,-y2,ny2); diff = sum(abs(diff));
if (diff < 1e-5)
    disp(' *** System-6 is Time-Invariant *** ');
else
    disp(' *** System-6 is Time-Varying *** ');
end
```

MATLAB verification:

```
>> *** System-6 is Time-Invariant ***
```

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P2.13 Stability and Causality of Discrete-time Systems

System-1: $T_1[x(n)] \triangleq y(n) = x(n)u(n)$: This system is **stable** since $|y(n)| = |x(n)|$. It is also **causal** since the output depends only on the present value of the input.

System-2: $T_2[x(n)] \triangleq y(n) = x(n) + n\,x(n+1)$: This system is **unstable** since

$$|y(n)| \leq |x(n)| + |n|\,|x(n+1)| \nearrow \infty \text{ as } n \nearrow \infty \text{ for } |x(n)| < \infty$$

It is also **noncausal** since the output $y(n)$ depends on the future input value $x(n+1)$ for $n > 0$.

System-3: $T_3[x(n)] \triangleq y(n) = x(n) + \frac{1}{2}x(n-2) - \frac{1}{3}x(n-3)x(2n)$: This system is **stable** since

$$|y(n)| \leq |x(n)| + \tfrac{1}{2}|x(n-2)| + \tfrac{1}{3}|x(n-3)|\,|x(2n)| < \infty \text{ for } |x(n)| < \infty$$

It is however is **noncausal** since $y(1)$ needs $x(2)$ which is a future input value.

System-4: $T_4[x(n)] \triangleq y(n) = \sum_{k=-\infty}^{n+5} 2x(k)$: This system is **unstable** since

$$|y(n)| \leq 2 \sum_{k=-\infty}^{n+5} |x(k)| \nearrow \infty \text{ as } n \nearrow \infty \text{ for } |x(n)| < \infty$$

It is also **noncausal** since the output $y(n)$ depends on the future input value $x(n+5)$ for $n > 0$.

System-5: $T_5[x(n)] \triangleq y(n) = x(2n)$: This system is **stable** since $|y(n)| = |x(2n)| < \infty$ for $|x(n)| < \infty$. It is however **noncausal** since $y(1)$ needs $x(2)$ which is a future input value.

System-6: $T_6[x(n)] \triangleq y(n) = \text{round}[x(n)]$: This system is **stable** and **causal**.

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P2.14 Properties of linear convolution.

$$\begin{array}{rcll} x_1(n) * x_2(n) & = & x_2(n) * x_1(n) & : \text{ Commutation} \\ [x_1(n) * x_2(n)] * x_3(n) & = & x_1(n) * [x_2(n) * x_3(n)] & : \text{ Association} \\ x_1(n) * [x_2(n) + x_3(n)] & = & x_1(n) * x_2(n) + x_1(n) * x_3(n) & : \text{ Distribution} \\ x(n) * \delta(n - n_0) & = & x(n - n_0) & : \text{ Identity} \end{array}$$

1. Commutation:

$$\begin{aligned} x_1(n) * x_2(n) &= \sum_{k=-\infty}^{\infty} x_1(k)\, x_2(\underbrace{n-k}_{=m}) = \sum_{m=-\infty}^{\infty} x_1(n-m)\, x_2(m) \\ &= \sum_{m=-\infty}^{\infty} x_2(m)\, x_1(n-m) = x_2(n) * x_1(n) \end{aligned}$$

Association:

$$\begin{aligned} [x_1(n) * x_2(n)] * x_3(n) &= \left[\sum_{k=-\infty}^{\infty} x_1(k)\, x_2(n-k)\right] * x_3(n) \\ &= \sum_{m=-\infty}^{\infty} \sum_{k=-\infty}^{\infty} x_1(k)\, x_2(m-k)\, x_3(n-m) \\ &= \sum_{k=-\infty}^{\infty} x_1(k) \left[\sum_{m=-\infty}^{\infty} x_2(\underbrace{m-k}_{=\ell}) x_3(n-m)\right] \\ &= \sum_{k=-\infty}^{\infty} x_1(k) \left[\sum_{m=-\infty}^{\infty} x_2(\ell)\, x_3(n-k-\ell)\right] \\ &= \sum_{k=-\infty}^{\infty} x_1(k)\, [x_2(n-k) * x_3(n-k)] = x_1(n) * [x_2(n) * x_3(n)] \end{aligned}$$

Distribution:

$$\begin{aligned} x_1(n) * [x_2(n) + x_3(n)] &= \sum_{k=-\infty}^{\infty} x_1(k)\, [x_2(n-k) + x_3(n-k)] \\ &= \sum_{k=-\infty}^{\infty} x_1(k)\, x_2(n-k) + \sum_{k=-\infty}^{\infty} x_1(k)\, x_3(n-k) \\ &= x_1(n) * x_2(n) + x_1(n) * x_3(n) \end{aligned}$$

Identity:

$$x(n) * \delta(n - n_0) = \sum_{k=-\infty}^{\infty} x(k)\, \delta(n - n_0 - k) = x(n - n_0)$$

since $\delta(n - n_0 - k) = 1$ for $k = n - n_0$ and zero elsewhere.

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2. Verification using MATLAB:

Commutation MATLAB script:

```
% P0214a: To prove the Commutation property of convolution
%         i.e. conv(x1(n),x2(n)) = conv(x2(n), x1(n))
clear; clc; close all;

n1 = -10:30; n2 = 0:25; n3 = -10:10; x11 = cos(pi*n1 / 4);
n11 = n1; [x12,n12] = stepseq(-5,-10,30); [x13,n13] = stepseq(25,-10,30);
[x14,n14] = sigadd(x12,n12,-x13,n13); x1 = x11.*x14;
x21 = 0.9 .^ -n2; [x22,n22] = stepseq(0,0,25); [x23,n23] = stepseq(20,0,25);
x24 = x22 - x23; x2 = x21.*x24;
x3 = round((rand(1,21)*2 - 1)*5);

% Commutative property
[y1,ny1] = conv_m(x1,n1,x2,n2); [y2,ny2] = conv_m(x2,n2,x1,n1);
ydiff = max(abs(y1 - y2)), ndiff = max(abs(ny1 - ny2)),
```

MATLAB verification:

```
ydiff =
     0
ndiff =
     0
```

Association MATLAB script:

```
% P0214b: To prove the Association property of convolution
%         i.e. conv(conv(x1(n),x2(n)),x3(n)) = conv(x1(n),conv(x2(n),x3(n)))
clear; clc; close all;

n1 = -10:30; n2 = 0:25; n3 = -10:10; x11 = cos(pi*n1 / 4); n11 = n1;
[x12,n12] = stepseq(-5,-10,30); [x13,n13] = stepseq(25,-10,30);
[x14,n14] = sigadd(x12,n12,-x13,n13); x1 = x11.*x14;
x21 = 0.9 .^ -n2; [x22,n22] = stepseq(0,0,25); [x23,n23] = stepseq(20,0,25);
x24 = x22 - x23; x2 = x21.*x24; x3 = round((rand(1,21)*2 - 1)*5);

% Association property
[y1,ny1] = conv_m(x1,n1,x2,n2); [y1,ny1] = conv_m(y1,ny1,x3,n3);
[y2,ny2] = conv_m(x2,n2,x3,n3); [y2,ny2] = conv_m(x1,n1,y2,ny2);
ydiff = max(abs(y1 - y2)), ndiff = max(abs(ny1 - ny2)),
```

MATLAB verification:

```
ydiff =
     0
ndiff =
     0
```

Distribution MATLAB script:

```
% P0214c: To prove the Distribution property of convolution
%         i.e. conv(x1(n),(x2(n)+x3(n)))=conv(x1(n),x2(n))+conv(x1(n),x3(n))
clear; clc; close all;

n1 = -10:30; n2 = 0:25; n3 = -10:10; x11 = cos(pi*n1 / 4); n11 = n1;
[x12,n12] = stepseq(-5,-10,30); [x13,n13] = stepseq(25,-10,30);
[x14,n14] = sigadd(x12,n12,-x13,n13); x1 = x11.*x14; x21 = 0.9 .^ -n2;
[x22,n22] = stepseq(0,0,25); [x23,n23] = stepseq(20,0,25); x24 = x22 - x23;
x2 = x21.*x24; x3 = round((rand(1,21)*2 - 1)*5);

% Distributive property
```

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```
[y1,ny1] = sigadd(x2,n2,x3,n3); [y1,ny1] = conv_m(x1,n1,y1,ny1);
[y2,ny2] = conv_m(x1,n1,x2,n2); [y3,ny3] = conv_m(x1,n1,x3,n3);
[y4,ny4] = sigadd(y2,ny2,y3,ny3); ydiff = max(abs(y1 - y4)),
ndiff = max(abs(ny1 - ny4)),
```

MATLAB verification:

```
ydiff =
     0
ndiff =
     0
```

Identity MATLAB script:

```
% P0214d: To prove the Identity property of convolution
%         i.e. conv(x(n),delta(n - n0))  = x(n - n0)
clear; clc; close all;

n1 = -10:30; n2 = 0:25; n3 = -10:10; x11 = cos(pi*n1 / 4); n11 = n1;
[x12,n12] = stepseq(-5,-10,30); [x13,n13] = stepseq(25,-10,30);
[x14,n14] = sigadd(x12,n12,-x13,n13); x1 = x11.*x14; x21 = 0.9 .^ -n2;
[x22,n22] = stepseq(0,0,25); [x23,n23] = stepseq(20,0,25); x24 = x22 - x23;
x2 = x21.*x24; x3 = round((rand(1,21)*2 - 1)*5);

% Identity property
n0 = fix(100*rand(1,1)-0.5); [dl,ndl] = impseq(n0,n0,n0);
[y11,ny11] = conv_m(x1,n1,dl,ndl); [y12,ny12] = sigshift(x1,n1,n0);
y1diff = max(abs(y11 - y12)), ny1diff = max(abs(ny11 - ny12)),

[y21,ny21] = conv_m(x2,n2,dl,ndl); [y22,ny22] = sigshift(x2,n2,n0);
y2diff = max(abs(y21 - y22)), ny2diff = max(abs(ny21 - ny22)),

[y31,ny31] = conv_m(x3,n3,dl,ndl); [y32,ny32] = sigshift(x3,n3,n0);
y3diff = max(abs(y31 - y32)), ny3diff = max(abs(ny31 - ny32)),
```

MATLAB verification:

```
ydiff =
     0
ndiff =
     0
```

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P2.15 Convolutions using `conv_m` function.

1. $x(n) = \{2, -4, 5, \underset{\uparrow}{3}, -1, -2, 6\}$, $h(n) = \{1, \underset{\uparrow}{-1}, 1, -1, 1\}$: MATLAB script:

```
n1  = -3:3; x = [2 -4 5 3 -1 -2 6]; n2 = -1:3; h = [1 -1 1 -1 1];
[y,n] = conv_m(x,n1,h,n2); y, n
y =
     2    -6    11    -8     7    -7     9    -4     7    -8     6
n =
    -4    -3    -2    -1     0     1     2     3     4     5     6
```

2. $x(n) = \{1, 1, \underset{\uparrow}{0}, 1, 1\}$, $h(n) = \{1, -2, -3, \underset{\uparrow}{4}\}$: MATLAB script:

```
n1  = -3:3; x = [1 1 0 1 1]; n2 = -3:0; h = [1 -2  -3 4];
[y,n] = conv_m(x,n1,h,n2); y, n,
y =
     1    -1    -5     2     3    -5     1     4
n =
    -6    -5    -4    -3    -2    -1     0     1
```

3. $x(n) = (1/4)^{-n}[u(n+1) - u(n-4)]$, $h(n) = u(n) - u(n-5)$: MATLAB script:

```
n1 = -2:5; [x11,nx11] = stepseq(-1,-2,5); [x12,nx12] = stepseq(4,-2,5);
[x13,n13] = sigadd(x11,nx11,-x12,nx12); x14 = 0.25 .^ -n1; n14 = n1;
x = x14 .* x13;
n2 = 0:6; [h11,nh11] = stepseq(0,0,6); [h12,nh12] = stepseq(5,0,6); h=h11-h12;
[y,n] = conv_m(x,n1,h,n2); y, n,
y =  0    0.2500    1.2500    5.2500   21.2500   85.2500   85.0000   84.0000
    80.0000   64.0000         0         0         0         0
n = -2    -1     0     1     2     3     4     5     6     7     8     9    10
    11
```

4. $x(n) = n/4[u(n) - u(n-6)]$, $h(n) = 2[u(n+2) - u(n-3)]$: MATLAB script:

```
n1 = 0:7; [x11,nx11] = stepseq(0,0,7); [x12,nx12] = stepseq(6,0,7);
[x13,n13] = sigadd(x11,nx11,-x12,nx12); x14 = n1/4; n14 = n1; x = x14 .* x13;
n2 = -3:4; [h11,nh11] = stepseq(-2,-3,4); [h12,nh12] = stepseq(3,-3,4);
h = 2 * (h11 - h12); [y,n] = conv_m(x,n1,h,n2); y, n,
y = 0         0    0.5000    1.5000    3.0000    5.0000    7.5000    7.0000
    6.0000    4.5000    2.5000         0         0         0         0
n = -3    -2    -1     0     1     2     3     4     5     6     7     8     9
    10    11
```

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P2.16 Let $x(n) = (0.8)^n u(n)$, $h(n) = (-0.9)^n u(n)$, and $y(n) = h(n) * x(n)$.

1. Convolution $y(n) = h(n) * x(n)$:

$$\begin{aligned} y(n) &= \sum_{k=-\infty}^{\infty} h(k)x(n-k) = \sum_{k=0}^{\infty}(-0.9)^k(0.8)^{n-k}u(n-k) \\ &= \left[\sum_{k=0}^{n}(-0.9)^k(0.8)^n(0.8)^{-k}\right]u(n) = (0.8)^n\left[\sum_{k=0}^{n}\left(-\frac{9}{8}\right)^k\right]u(n) \\ &= \frac{0.8^{n+1}-(-0.9)^{n+1}}{1.7} \end{aligned}$$

   MATLAB script:

```
clc; close all;run defaultsettings;
n = [0:50]; x = 0.8.^n; h = (-0.9).^n;
Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0216');

% (a) Plot of the analytical convolution
y1 = ((0.8).^(n+1) - (-0.9).^(n+1))/(0.8+0.9);
subplot(1,3,1); Hs1 = stem(n,y1,'filled'); set(Hs1,'markersize',2);
title('Analytical'); xlabel('n'); ylabel('y(n)');
```

2. Computation using convolution of truncated sequences: MATLAB script

```
% (b) Plot using the conv function and truncated sequences
x2 = x(1:26); h2 = h(1:26); y2 = conv(h2,x2);
subplot(1,3,2); Hs2 = stem(n,y2,'filled'); set(Hs2,'markersize',2);
title('Using conv function'); xlabel('n'); %ylabel('y(n)');
```

3. To use the MATLAB's `filter` function we have to represent the $h(n)$ sequence by coefficients an equivalent difference equation. MATLAB script:

```
% (c) Plot of the convolution using the filter function
y3 = filter([1],[1,0.9],x);
subplot(1,3,3); Hs3 = stem(n,y3,'filled'); set(Hs3,'markersize',2);
title('Using filter function'); xlabel('n'); %ylabel('y(n)');
```

The plots of this solution are shown in Figure 2.33. The analytical solution to the convolution in 1 is the exact answer. In the `filter` function approach of 2, the infinite-duration sequence $x(n)$ is exactly represented by coefficients of an equivalent filter. Therefore, the filter solution should be exact except that it is evaluated up to the length of the input sequence. The truncated-sequence computation in 3 is correct up to the first 26 samples and then it degrades rapidly.

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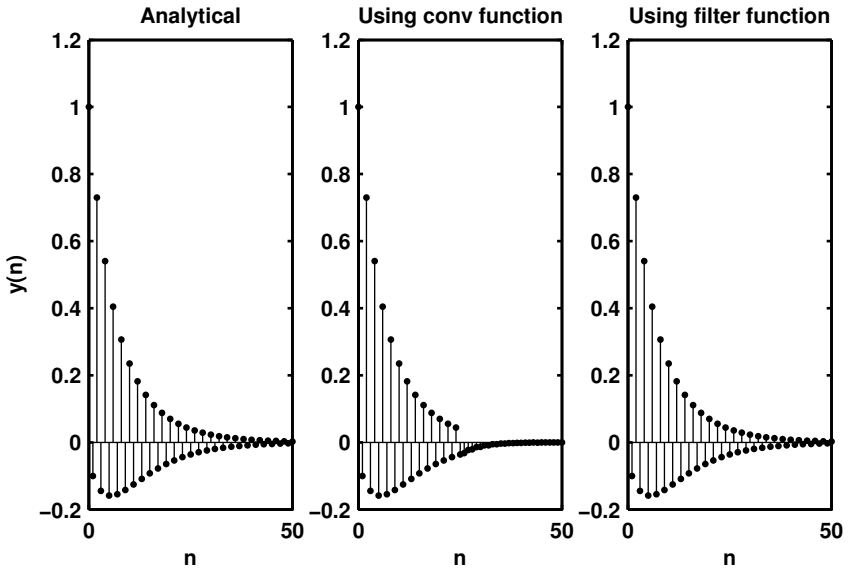


Figure 2.33: Problem P2.16 convolution plots

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P2.17 Linear convolution as a matrix-vector multiplication. Consider the sequences

$$x(n) = \{1, 2, 3, 4, 5\} \text{ and } h(n) = \{6, 7, 8, 9\}$$

1. The linear convolution of the above two sequences is

$$y(n) = \{6, 19, 40, 70, 100, 94, 76, 45\}$$

2. The vector representation of the above operation is:

$$\underbrace{\begin{bmatrix} 6 \\ 19 \\ 40 \\ 70 \\ 100 \\ 94 \\ 76 \\ 45 \end{bmatrix}}_{\mathbf{y}} = \underbrace{\begin{bmatrix} 6 & 0 & 0 & 0 & 0 \\ 7 & 6 & 0 & 0 & 0 \\ 8 & 7 & 6 & 0 & 0 \\ 9 & 8 & 7 & 6 & 0 \\ 0 & 9 & 8 & 7 & 6 \\ 0 & 0 & 9 & 8 & 7 \\ 0 & 0 & 0 & 9 & 8 \\ 0 & 0 & 0 & 0 & 9 \end{bmatrix}}_{\mathbf{H}} \underbrace{\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}}_{\mathbf{x}}$$

(a) Note that the matrix **H** has an interesting structure. Each diagonal of **H** contains the same number. Such a matrix is called a Toeplitz matrix. It is characterized by the following property

$$[\mathbf{H}]_{i,j} = [\mathbf{H}]_{i-j}$$

which is similar to the definition of time-invariance.

(b) Note carefully that the first column of **H** contains the impulse response vector $h(n)$ followed by number of zeros equal to the number of $x(n)$ values minus one. The first row contains the first element of $h(n)$ followed by the same number of zeros as in the first column. Using this information and the above property we can generate the whole Topelitz matrix.

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P2.18 MATLAB function conv_tp:

(a) The MATLAB function conv_tp:

```
function [y,H]=conv_tp(h,x)
% Linear Convolution using Toeplitz Matrix
% ----------------------------------------
% [y,H] = conv_tp(h,x)
% y = output sequence in column vector form
% H = Toeplitz matrix corresponding to sequence h so that y = Hx
% h = Impulse response sequence in column vector form
% x = input sequence in column vector form
%
Nx = length(x); Nh = length(h);
hc = [h; zeros(Nx-1, 1)]; hr = [h(1),zeros(1,Nx-1)];
H = toeplitz(hc,hr); y = H*x;
```

(b) MATLAB verification:

```
x = [1,2,3,4,5]'; h = [6,7,8,9]';
[y,H] = conv_tp(h,x); y = y', H
y =
     6    19    40    70   100    94    76    45
H =
     6     0     0     0     0
     7     6     0     0     0
     8     7     6     0     0
     9     8     7     6     0
     0     9     8     7     6
     0     0     9     8     7
     0     0     0     9     8
     0     0     0     0     9
```

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P2.19 A linear and time-invariant system is described by the difference equation

$$y(n) - 0.5y(n-1) + 0.25y(n-2) = x(n) + 2x(n-1) + x(n-3)$$

(a) Impulse response using the Using the `filter` function.

```
% P0219a: System response using the filter function
clc; close all;

b = [1 2 0 1]; a = [1 -0.5 0.25]; [delta,n] = impseq(0,0,100);
h = filter(b,a,delta);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0219a');
Hs = stem(n,h,'filled'); set(Hs,'markersize',2);
axis([min(n)-5,max(n)+5,min(h)-0.5,max(h)+0.5]);
xlabel('n','FontSize',LFS); ylabel('h(n)','FontSize',LFS);
title('Impulse response','FontSize',TFS);
print -deps2 ../EPSFILES/P0219a.eps;
```

The plots of the impulse response $h(n)$ is shown in Figure 2.34.

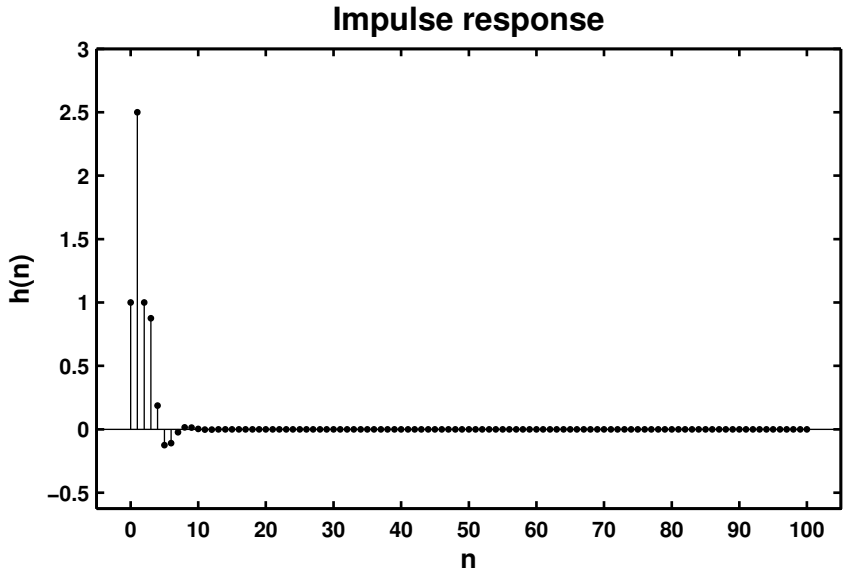


Figure 2.34: Problem P2.19.1 impulse response plot

(b) Clearly from Figure 2.34 the system is stable.

(c) Response $y(n)$ when the input is $x(n) = [5 + 3\cos(0.2\pi n) + 4\sin(0.6\pi n)]\,u(n)$:

```
% P0219c: Output response of a system using the filter function.
clc; close all;

b = [1 2 0 1]; a = [1 -0.5 0.25]; n = 0:200;
x = 5*ones(size(n))+3*cos(0.2*pi*n)+4*sin(0.6*pi*n); y = filter(b,a,x);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0219c');
Hs = stem(n,y,'filled'); set(Hs,'markersize',2); axis([-10,210,0,50]);
xlabel('n','FontSize',LFS); ylabel('y(n)','FontSize',LFS);
title('Output response','FontSize',TFS);
print -deps2 ../EPSFILES/P0219c.eps;
```

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The plots of the response $y(n)$ is shown in Figure 2.35.

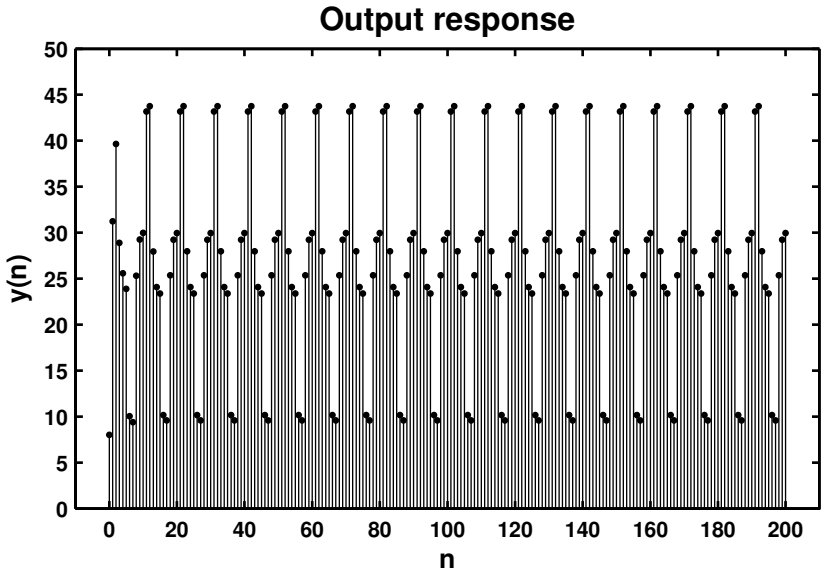


Figure 2.35: Problem P2.19.3 response plot

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P2.20 A "simple" *digital differentiator*: $y(n) = x(n) - x(n-1)$

(a) Response to a rectangular pulse $x(n) = 5\,[u(n) - u(n-20)]$:

```
% P0220a: Simple Differentiator response to a rectangular pulse
clc; close all;

a = 1; b = [1 -1]; n1 = 0:22;
[x11,nx11] = stepseq(0,0,22); [x12,nx12] = stepseq(20,0,22);
x1 = 5*(x11 - x12); y1 = filter(b,a,x1);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0220a');
Hs = stem(n1,y1,'filled'); set(Hs,'markersize',2); axis([-1,23,-6,6]);
xlabel('n','FontSize',LFS); ylabel('y(n)','FontSize',LFS); ytick = [-6:6];
title('Output response for rectangular pulse ','FontSize',TFS);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../EPSFILES/P0220a.eps;
```

The plots of the response $y(n)$ is shown in Figure 2.36.

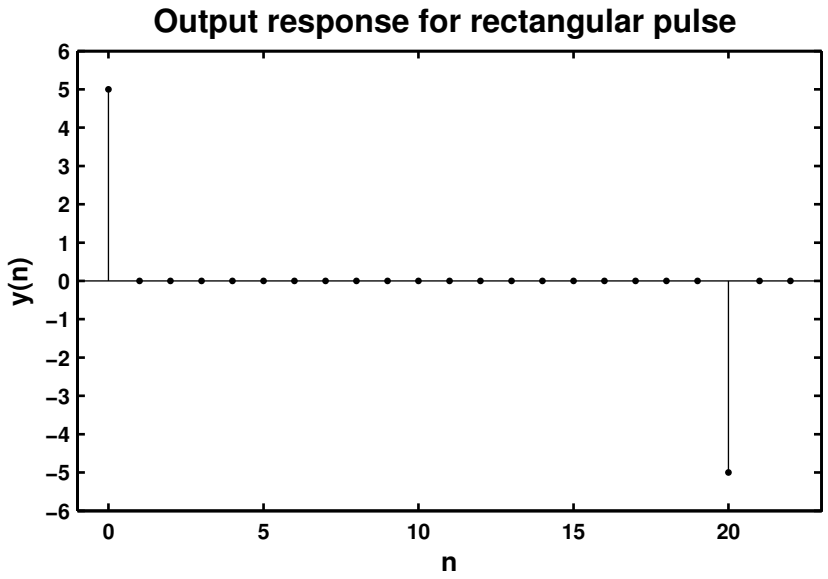


Figure 2.36: Problem P2.20.1 response plot

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(b) Response to a triangular pulse $x(n) = n\,[u(n) - u(n-10)] + (20-n)\,[u(n-10) - u(n-20)]$:

```
% P0220b: Simple Differentiator response to a triangular pulse
clc; close all;

a = 1; b = [1 -1]; n2 = 0:21; [x11,nx11] = stepseq(0,0,21);
[x12,nx12] = stepseq(10,0,21); [x13,nx13] = stepseq(20,0,21);
x2  =  n2.*(x11 - x12) + (20 - n2).*(x12 - x13); y2 = filter(b,a,x2);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0220b');
Hs = stem(n2,y2,'filled'); set(Hs,'markersize',2);
axis([min(n2)-1,max(n2)+1,min(y2)-0.5,max(y2) + 0.5]);
xlabel('n','FontSize',LFS); ylabel('y(n)','FontSize',LFS);
title('Output response for triangular pulse','FontSize',TFS);
print -deps2 ../EPSFILES/P0220b.eps;
```

The plots of the response $y(n)$ is shown in Figure 2.37.

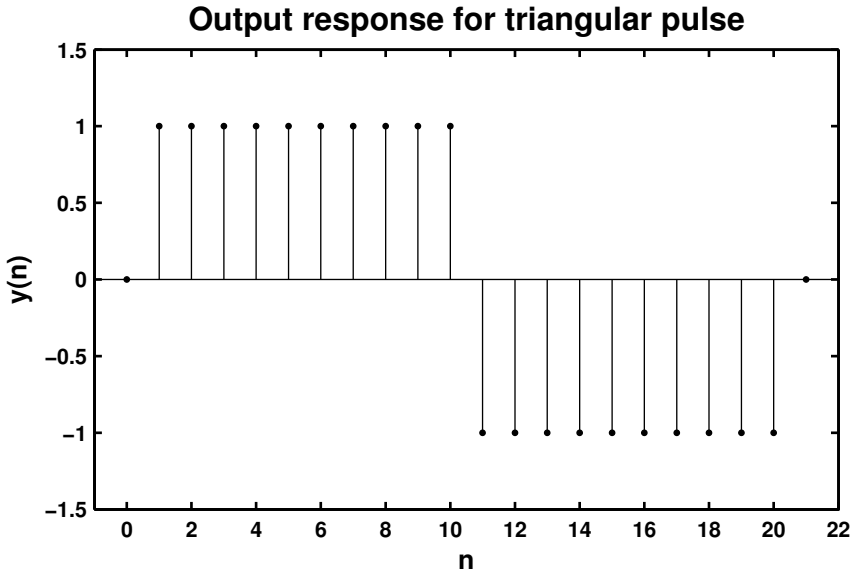


Figure 2.37: Problem P2.20.2 response plot

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(c) Response to a sinusoidal pulse $x(n) = \sin\left(\frac{\pi n}{25}\right)[u(n) - u(n-100)]$:

```
% P0220cSimple Differentiator response to a sinusoidal pulse
clc; close all;

a = 1; b = [1 -1]; n3 = 0:101; [x11,nx11] = stepseq(0,0,101);
[x12,nx12] = stepseq(100,0,101); x13 = x11-x12; x3 = sin(pi*n3/25).*x13;
y3 = filter(b,a,x3);

Hf_1 = figure; set(Hf_1,'NumberTitle','off','Name','P0220c');
Hs = stem(n3,y3,'filled'); set(Hs,'markersize',2);
axis([-5,105,-0.15,0.15]); ytick = [-0.15:0.05:0.15];
xlabel('n','FontSize',LFS); ylabel('y(n)','FontSize',LFS);
title('Output response for sinusoidal pulse','FontSize',TFS);
set(gca,'YTickMode','manual','YTick',ytick);
print -deps2 ../EPSFILES/P0220c.eps;
```

The plots of the response $y(n)$ is shown in Figure 2.38.

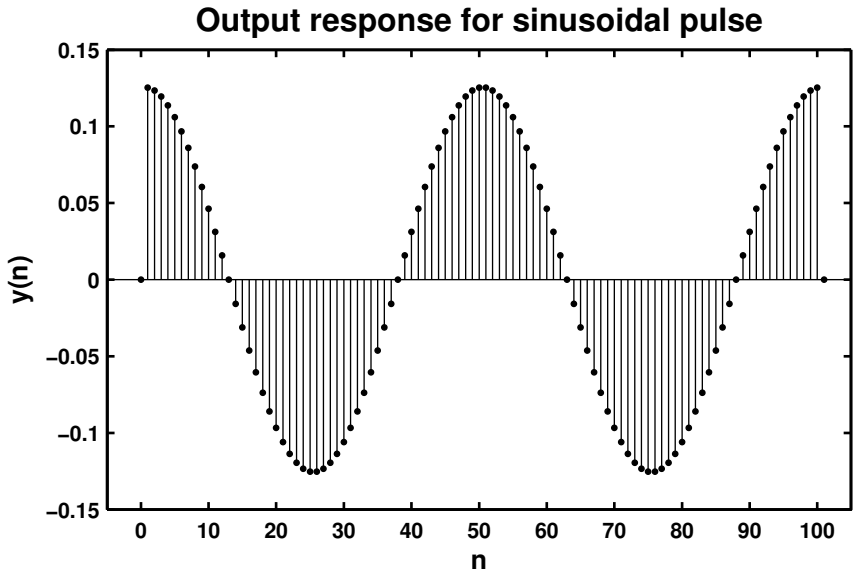


Figure 2.38: Problem P2.20.3 response plot

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